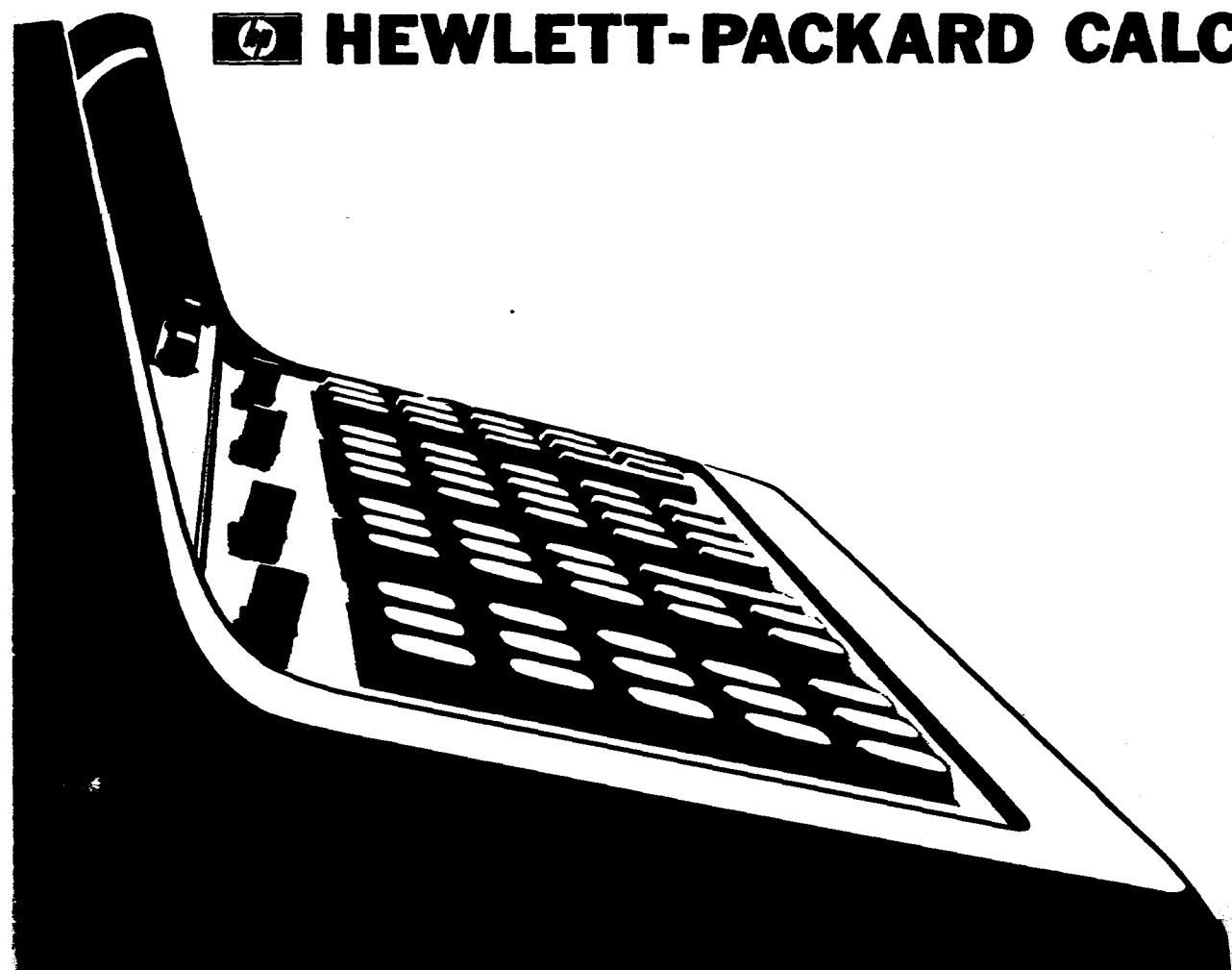


ANIMAL
ECOLOGY

 **HEWLETT-PACKARD CALCULATOR**



HEWLETT  **PACKARD**

INTER-OFFICE CORRESPONDENCE

FROM: Pat Welch

DATE:

TO: CALCULATOR SALESMEN

SUBJECT: Animal Ecology

The enclosed programs are some examples of how Dr. J. D. Weintraub at California State College in Fullerton, California has employed the 9100 in teaching and research in the field of Animal Ecology.

In addition to these examples, Animal Ecologists use general statistics, so, the STAT-PAC should be useful to them.

If you have any inputs regarding other general purpose programs or specific examples of how the 9100 is being used in this field, let us know.

Go get 'em!!!!

Regards,

Pat

PW/bd

ANIMAL ECOLOGY PROGRAM LISTING

- 1 -- "K" Value of the Negative Binomial-Trial and Error
- 2 -- Expected Values for Negative Binomial Distribution
- 3 -- Logistic Versus Exponential Curves for Population Growth
- 4 -- Species Diversity Index Based on Information Theory
- 5 -- Expected Number from a Poisson Series
- 6 -- Mann-Whitney Ranking Statistic
- 7 -- Population Estimate and Confidence Limits of a Simple Capture - Recapture Index
- 8 -- Population Estimate and Confidence Limits of Removal Trapping

"K" VALUE OF THE NEGATIVE
BINOMIAL-TRIAL AND ERROR

If the distribution of animals or plants in space or time does not fit a Poisson series, then the negative binomial may be compared with the observed data. This program calculates an index of aggregation, k, by a trial and error method.

The equation used in this calculation is:

$$\text{Log}_{10} \left(\frac{N}{N_0} \right) = K \text{Log}_{10} \left(\frac{1 + M}{K} \right)$$

N = Total number of sample quadrants

N_0 = Number having 0 items

M = Mean

This is good for means below 10.

EXAMPLE

With 100 quadrants sampled, of which 15 had no animals, and a mean for the entire sample of 4.25 animals per quadrant?
What is the K value?

ANSWER: 1.58

Reference: Ecological Methods,
by T. R. E. Southwood, 1961,
Methuen and Company, Ltd.

ANIMAL
ECOLOGY
Program 1

X X X

X

X

5

1. PRESS: END
2. ENTER PROGRAM
3. PRESS: CONTINUE
4. ENTER DATA
5. PRESS: CONTINUE
6. ENTER estimated K Value
7. PRESS: CONTINUE
8. If $Z = Y$, K is correct
If $Z \neq Y$
9. PRESS: CONTINUE
Reestimate K
Return to Step 6

1	0	0
M	N_0	N
2	0	0
K	0	0
0	$\log(\frac{N}{N_0})$	K

EXAMPLE

N
N_O
M

Estimated K
 $\text{Log} \left(\frac{N}{N_O} \right)$
 $K \text{ Log } 10 \left(\frac{I+M}{K} \right)$

A

100.
15.
4.25

0.
0.
1.4
- 80364
- 82391
0.

0.
0.
1.5
- 81610
- 82391
0.

0.
0.
1.58
- 82397
- 82391
0.

ANIMAL ECOLOGY -- 1

00 CLR 20
01 1 01
02 STP 41
03 PNT 45
04 PNT 45
05 XTO 23
06 a 13
07 RDN 31
08 DIV 35
09 DN 25
0a LOG 75
0b XTO 23
0c b 14
0d CLR 20

10 2 02
11 STP 41
12 PNT 45
13 RDN 31
14 a 13
15 XEY 30
16 1 01
17 + 33
18 DN 25
19 XEY 30
1a DIV 35
1b XEY 30
1c LOG 75
1d RUP 22

20 X 36
21 b 14
22 RUP 22
23 CLX 37
24 STP 41
25 PNT 45
26 PNT 45
27 CLX 37
28 GTO 44
29 0 00
2a d 17
2b END 46

EXPECTED VALUES FOR NEGATIVE BINOMIAL DISTRIBUTION

Knowing the value of 'k' from Program 1, this program calculates expected values of the negative binomial. One application is to find the number of quadrants containing 0, 1, 2 ... n animals in a sampling area.

The equation used in this calculation is:

$$N \cdot f(x_i) = N \left[\frac{\gamma(K+x_i)}{x_i! \gamma(K)} \right] \cdot \left[\frac{M}{M+K} \right]^{x_i} \cdot \left[\frac{K}{K+M} \right]^K$$

N = Number of quadrants

K = Aggregation index

x_i = Number of items per quadrant

γ and T = Constants

M = Mean

EXAMPLE

Given a 'k' value of 1.58, a mean of 4.25, and 100 quadrants sampled, calculate the expected number of quadrants containing 0, 1, 2 ... n number of animals using the negative binomial distribution.

$\gamma K = .891$

$T(K + x_i)$	$x_i!$	x_i
$T(K + 0) = .891$	$x_0! = 1$	0
$T(K + 1) = 1.408$	$x_1! = 1$	1
$T(K + 2) = 3.634$	$x_2! = 2$	2
$T(K + 3) = 13.009$	$x_3! = 6$	3
$T(K + 4) = 59.581$	$x_4! = 24$	4
$T(K + 5) = 332.462$	$x_5! = 120$	5

Answers:

<u>x</u>	<u>values of the negative binomial</u>
0	12.71
1	14.64
2	13.77
3	11.98
4	10.00
5	8.14

ANIMAL
ECOLOGY
Program 2

X X X

X

X

5

1. PRESS: END
2. ENTER PROGRAM
3. PRESS: CONTINUE
4. ENTER DATA
5. PRESS: CONTINUE
6. ENTER DATA
7. PRESS: CONTINUE
8. ENTER DATA
9. PRESS: CONTINUE
10. PRESS: CONTINUE (Recycle to Step 8)

For new data

PRESS: END

PRESS: CONTINUE

1	0	0
M	K	
2	0	0
γ (K)	N	
3	0	0
x_i	$x_i!$	$T(K + x_i)$
x_i	0	$N \cdot f(x_i)$

ANIMAL
ECOLOGY
Program 2

EXAMPLE

K	0.
Mean	1.58
	4.25
Quadrants	0.
γK	100.
	.891
$T(K + 0)$.891
$x_0!$	1.
x_0	0.
Negative Binomial	12.70931
	0.
	0.
$T(K + 1)$	1.408
$x_1!$	1.
x_1	1.
Negative Binomial	14.64088
	0.
	1.
	3.634
	2.
	2.
	13.77336
	0.
	2.
	13.009
	5.
	3.
	11.98114
	0.
	3.

ANIMAL ECOLOGY -- 2

00	CLR	20	40	RUP	22
01	1	01	41	X	36
02	STP	41	42	CLX	37
03	PNT	45	43	RUP	22
04	PNT	45	44	f	15
05	AC+	60	45	PNT	45
06	+	33	46	PNT	45
07	KEY	30	47	GTO	44
08	DIV	35	48	2	02
09	KEY	30	49	7	07
0a	LN	65	4a	END	46
0b	XTO	23			
0c	a	13			
0d	RCL	61			
10	KEY	30			
11	+	33			
12	UP	27			
13	RUP	22			
14	DIV	35			
15	RDN	31			
16	LN	65			
17	X	36			
18	KEY	30			
19	EXP	74			
1a	XTO	23			
1b	b	14			
1c	CLR	20			
1d	2	02			
20	STP	41			
21	PNT	45			
22	PNT	45			
23	XTO	23			
24	c	16			
25	YTO	40			
26	d	17			
27	CLR	20			
28	3	03			
29	STP	41			
2a	PNT	45			
2b	PNT	45			
2c	AC+	60			
2d	c	16			
30	X	36			
31	RDN	31			
32	DIV	35			
33	d	17			
34	X	36			
35	b	14			
36	X	36			
37	RUP	22			
38	f	15			
39	KEY	30			
3a	a	13			
3b	X	36			
3c	KEY	30			
3d	EXP	74			

LOGISTIC VERSUS EXPONENTIAL CURVES
FOR POPULATION GROWTH

Population increase of yeast, protozoa, etc., will not continue indefinitely, but will reach a plateau. The first part of the growth curve may resemble the exponential curve, while the overall growth pattern will be more closely related to the logistic curve. This program calculates both curves, mainly for teaching comparison.

The equations used in these calculations are:

$$(1) \text{ Exponential } N_t = N_0 e^{rt}$$

N_t = Population at time t

N_0 = Population at time 0

$$(2) \text{ Logistic } N_t = \frac{K}{1 + e^{a - rt}}$$

K = Upper limit of population

r = Innate rate of increase

a = Constant of integration defining position
of the curve related to the origin

Reference: Laboratory Manual of General Ecology
by George W. Cox

**ANIMAL
ECOLOGY
Program 3**

EXAMPLE

Given an innate rate of increase (r) of 1.022 individuals per day, a population ceiling (K) of 450 individuals per .5 ml. and an 'a' value of 5.041, compare the logistics and exponentials curve of population growth that starts with 2 individuals per .5 ml.

ANSWER:

<u>Time (t)</u>	<u>Exponential ($N_0 e^{rt}$)</u>	<u>Logistics $\frac{K}{1 + e^{a-rt}}$</u>
0	2	2.9
1	5.6	7.9
2	15.4	21.4
3	42.9	54.8
4	119.2	125.2
5	331.3	232.8
6	920.7	336.9
7	2558.4	401.5
8	7109.2	431.2
9	19754.7	443.1
10	54893.3	447.5

ANIMAL
ECOLOGY
Program 3

X X X

X

X

5

- | | | | |
|--|---|--------------------------------|------------------------|
| 1. PRESS: END | | | |
| 2. ENTER PROGRAM | | | |
| 3. PRESS: CONTINUE | 0 | 1 | 0 |
| 4. ENTER DATA | r | N ₀ | 1 |
| 5. PRESS: CONTINUE | 0 | 2 | 0 |
| 6. ENTER DATA | a | K | 2 |
| 7. PRESS: CONTINUE | 3 | 0 | 0 |
| 8. ENTER: t | t | 0 | 0 |
| 9. PRESS: CONTINUE
DISPLAY | t | N ₀ e ^{rt} | $\frac{K}{1+e^{a-rt}}$ |
| 10. PRESS: CONTINUE (return to step 7) | | | |
| 11. PRESS: END, CONTINUE for new data set (return to step 3) | | | |

ANIMAL
ECOLOGY
Program 3

EXAMPLE

Data Entry	1.
N_0	2.
R	1.022
Data Entry	2.
K	450.
a	5.041
$\frac{K}{1+ea-rt}$	2.89157
$N_0 e^{rt}$	2.00000
t	0.
	7.94415
	5.55749
	1.
	21.40271
	15.44287
	2.
	54.83378
	42.91181
	3.
	125.22685
	119.24106
	4.
	232.75942
	331.34071
	5.
	336.85849
	320.71190
	6.

ANIMAL ECOLOGY -- 3

00	CLR	20	40	GTO	44
01	1	01	41	1	01
02	XKEY	30	42	6	06
03	STP	41	43	END	46
04	PNT	45			
05	PNT	45			
06	XTO	23			
07	a	13			
08	YTO	40			
09	b	14			
0a	CLR	20			
0b	2	02			
0c	XKEY	30			
0d	STP	41			
10	PNT	45			
11	PNT	45			
12	XTO	23			
13	c	16			
14	YTO	40			
15	d	17			
16	CLR	20			
17	3	03			
18	STP	41			
19	UP	27			
1a	a	13			
1b	XKEY	30			
1c	X	36			
1d	XTO	23			
20	9	11			
21	AC+	60			
22	b	14			
23	LN	65			
24	+	33			
25	XKEY	30			
26	EXP	74			
27	XTO	23			
28	f	15			
29	c	16			
2a	XKEY	30			
2b	e	12			
2c	-	34			
2d	XKEY	30			
30	EXP	74			
31	UP	27			
32	1	01			
33	+	33			
34	d	17			
35	XKEY	30			
36	DIV	35			
37	f	15			
38	UP	27			
39	YE	24			
3a	9	11			
3b	XKEY	30			
3c	PNT	45			
3d	PNT	45			

SPECIES DIVERSITY INDEX
BASED ON INFORMATION THEORY

This program calculates the expected species diversity in a given area.
The equation used in this calculation is:

$$H \approx 3.3219 \left[\log_{10} N - \frac{1}{N} (\sum N_i \log_{10} N_i) \right]$$

N = Total number of species

N_i = Number of individuals of i^{th} species

H = Species diversity index

EXAMPLE

A collection of invertebrates yielded the following number of individuals:

Species A = 300
Species B = 150
Species C = 10
Species D = 5
Species E = 2
Species F = 1

What is the species diversity?

Answer:

Diversity = 1.1785

Number of individuals = 468

Number of species = 6

Reference: Ecological Methods
by T. R. F. Southwood,
1966, Methuen & Company, Ltd.

ANIMAL
ECOLOGY
Program 4

X X

X

X

5

- | | | | |
|--|----------------|---|--|
| 1. PRESS: END | | | |
| 2. ENTER PROGRAM | | | |
| 3. PRESS: CONTINUE | 0 | 1 | |
| 4. ENTER DATA | N _i | | |
| 5. PRESS: CONTINUE | | | |
| 6. PRESS: SET FLAG (after last data point) | | | |
| 7. PRESS: CONTINUE | N | i | |
| 8. PRESS: CONTINUE (ready for new data) | H | 0 | |

ANIMAL
ECOLOGY
Program 4

i	1.
N _i	300.
	2.
	150.
	3.
	10.
	4.
	5.
	5.
	2.
	6.
	1.
N	469.
i	6.
H	0.
	1. 17848

ANIMAL ECOLOGY -- 4

00	CLR	20	40	RUP	22
01	XTO	23	41	PNT	45
02	d	17	42	PNT	45
03	1	01	43	END	46
04	XEY	30			
05	STP	41			
06	IFG	43			
07	2	02			
08	3	03			
09	PNT	45			
0a	PNT	45			
0b	YTO	40			
0c	d	17			
0d	UP	27			
10	UP	27			
11	LOG	75			
12	X	36			
13	RDN	31			
14	AC+	60			
15	CLX	37			
16	RDN	31			
17	d	17			
18	UP	27			
19	1	01			
1a	+	33			
1b	0	00			
1c	UP	27			
1d	RDN	31			
20	GTO	44			
21	0	00			
22	5	05			
23	e	12			
24	UP	27			
25	LOG	75			
26	RDN	31			
27	XEY	30			
28	1	01			
29	XEY	30			
2a	DIV	35			
2b	f	15			
2c	X	36			
2d	RDN	31			
30	-	34			
31	3	03			
32	.	21			
33	3	03			
34	2	02			
35	1	01			
36	9	11			
37	X	36			
38	e	12			
39	RUP	22			
3a	d	17			
3b	PNT	45			
3c	PNT	45			
3d	CLX	37			

EXPECTED NUMBER FROM A POISSON SERIES

This program checks randomness of distribution of individual animals of a class in a sampling area. For ecological work, the Poisson series is used to check this assumption. Calculated values can be compared to measured values using a χ^2 goodness of fit test.

The equation used in this calculation is:

$$f(N; \lambda) = \frac{\lambda^N e^{-\lambda}}{N!}$$

EXAMPLE

If the mean number of beetles in (N) 100 sampling areas is (λ) 5.43, what is the expected areas that have 0, 1, 2 ... x beetles?

(0)	N _i	f(N _i ; λ)	N(N _i)
	1	.0238	2.38
	2	.0646	6.46
	3	.1170	11.70
	4	.1588	15.88
	5	.1724	17.24
	6	.1560	15.60
	7	.1210	12.10
	8	.0821	8.22

(0) Example Entry

ANIMAL
ECOLOGY
Program 5

X X X

X

X

5

1. PRESS: END
2. ENTER PROGRAM
3. PRESS: CONTINUE 0 0 0
4. ENTER DATA: λ (mean) N_i N
5. PRESS: CONTINUE
DISPLAY N_i $f(N_i; \lambda)$ $N(N_i)$
6. PRESS: CONTINUE
DISPLAY N_{i+1} $f(N_{i+1}; \lambda)$ $N(N_{i+1})$
- etc.
7. To reset, PRESS: END
PRESS: CONTINUE (return to step 4)

ANIMAL
ECOLOGY
Program 5

EXAMPLE

N	100.
N_i	1.
λ	5.43
$N(N_i)$	2.38002
$f(N_i; \lambda)$.02380
N_i	1.
	6.46176
	.06462
	2.
	11.69578
	.11696
	3.
	15.87702
	.15877
	4.
	17.24245
	.17242
	5.
	15.60441
	.15604
	6.
	12.10457
	.12105
	7.
	8.21597
	.08216
	8.

ANIMAL ECOLOGY -- 5

00	CLR	20		40	STP	41
01	STP	41		41	PNT	45
02	PNT	45		42	PNT	45
03	PNT	45		43	CLR	20
04	XTO	23		44	b	14
05	c	16		45	UP	27
06	YTO	40		46	1	01
07	b	14		47	+	33
08	RUP	22		48	YTO	40
09	XTO	23		49	b	14
0a	d	17		4a	c	16
0b	XKEY	30		4b	GTO	44
0c	CHS	32		4c	0	00
0d	EXP	74		4d	c	16
10	UP	27		50	END	46
11	c	16				
12	LN	65				
13	UP	27				
14	b	14				
15	X	36				
16	XKEY	30				
17	EXP	74				
18	RUP	22				
19	X	36				
1a	YTO	40				
1b	a	13				
1c	b	14				
1d	UP	27				
20	UP	27				
21	1	01				
22	-	34				
23	X>Y	53				
24	2	02				
25	c	16				
26	RDN	31				
27	X	36				
28	RUP	22				
29	GTO	44				
2a	2	02				
2b	2	02				
2c	a	13				
2d	RUP	22				
30	UP	27				
31	0	00				
32	XKEY	30				
33	X=Y	50				
34	CNT	47				
35	1	01				
36	XKEY	30				
37	DN	25				
38	DIV	35				
39	d	17				
3a	XKEY	30				
3b	X	36				
3c	RUP	22				
3d	b	14				

MANN-WHITNEY RANKING STATISTIC

This program is a significance test for differences in the medians of two samples, x and y. The distribution need not be normal. A rank is given to each x and y item, and the statistics U_1 and U_2 calculated. The values can be compared with the lowest U value in a suitable table to determine significance of the differences between medians.

The equations used in these calculations are:

$$U_1 = N_1 N_2 + 1/2 N_2 (N_2 + 1) - R_2$$

$$U_2 = N_1 N_2 + 1/2 N_1 (N_1 + 1) - R_1$$

$$U_2 = N_1 N_2 - U$$

$$R_1 = \text{Sum of ranks of } x$$

$$R_2 = \text{Sum of ranks of } y$$

EXAMPLE

Two species of insects were caught at a blacklight. Species x appeared at 1, 5, 8, 11, 20, 30, 35, and 40 minutes after 6:00 p. m. (each time represents one individual), and species y appeared at 3, 7, 9, 12, 13, 15, 18, and 22 minutes after 6:00 p. m. What is the U statistic?

x values	1	5	8	11	20	30	35	40
y values	3	7	9	12	13	15	18	22
Rank	x rank	1	3	5	7	12	14	15
	y rank	2	4	6	8	9	10	13

Answers:

$$U_x = 37 \quad U_y = 27 \quad N_x = 8 \quad N_y = 8$$

Reference: Statistics for Biologists
by R. C. Campbell
1967, Cambridge University Press

ANIMAL
ECOLOGY
Program 6

X

X

X X

5

- | | | | | |
|-----|---|-------|-----------|---|
| 1. | PRESS: END | | | |
| 2. | ENTER PROGRAM | | | |
| 3. | PRESS: CONTINUE | 0 | 1 | 0 |
| 4. | ENTER DATA (Rank of x) | x_i | i | 0 |
| 5. | PRESS: CONTINUE (Repeat for each x value) | | | |
| 6. | PRESS: SET FLAG after last data point | | | |
| 7. | PRESS: CONTINUE | 0 | 1 | 0 |
| 8. | ENTER DATA (Rank of y) | y_i | i | 0 |
| 9. | PRESS: CONTINUE (Repeat for each y value) | | | |
| 10. | PRESS: SET FLAG after last entry | | | |
| 11. | PRESS: CONTINUE | Ux | Uy | 0 |
| 12. | PRESS: CONTINUE (Return to Step 4) | Nx | <td></td> | |

ANIMAL
ECOLOGY
Program 6

EXAMPLE

x_i	1.
i	1.
.	2.
.	3.
.	3.
.	5.
.	4.
.	7.
.	12.
.	6.
.	14.
.	7.
.	15.
.	8.
.	16.
y_i	1.
i	2.
.	2.
.	4.
.	3.
.	6.
.	4.
.	9.
.	5.
.	9.
.	6.
.	10.
.	7.
.	11.
.	8.
.	13.
u_x	37.0
u_y	27.0
n_x	8.
n_y	8.

ANIMAL ECOLOGY -- 6

00	CLR	20	40	AC+	60
01	XTO	23	41	f	15
02	d	17	42	-	34
03	1	01	43	RUP	22
04	XKEY	30	44	b	14
05	STP	41	45	XKEY	30
06	IFG	43	46	1	01
07	1	01	47	+	33
08	b	14	48	b	14
09	PNT	45	49	X	36
0a	PNT	45	4a	.	21
0b	YTO	40	4b	5	05
0c	d	17	4c	X	36
0d	XKEY	30	4d	RDN	31
10	CLX	37	50	+	33
11	XKEY	30	51	XKEY	30
12	AC+	60	52	YE	24
13	d	17	53	e	12
14	UP	27	54	-	34
15	1	01	55	XKEY	30
16	+	33	56	UP	27
17	CLX	37	57	CLX	37
18	GTO	44	58	RDN	31
19	0	00	59	PNT	45
1a	5	05	5a	PNT	45
1b	f	15	5b	d	17
1c	XTO	23	5c	XKEY	30
1d	c	16	5d	b	14
20	CLR	20	60	PNT	45
21	1	01	61	PNT	45
22	XKEY	30	62	END	46
23	STP	41			
24	IFG	43			
25	3	03			
26	9	11			
27	PNT	45			
28	PNT	45			
29	YTO	40			
2a	b	14			
2b	XKEY	30			
2c	CLX	37			
2d	XKEY	30			
30	AC+	60			
31	b	14			
32	UP	27			
33	1	01			
34	+	33			
35	CLX	37			
36	GTO	44			
37	2	02			
38	3	03			
39	b	14			
3a	UP	27			
3b	d	17			
3c	X	36			
3d	CLX	37			

POPULATION ESTIMATE AND CONFIDENCE LIMITS OF
A SIMPLE CAPTURE - RECAPTURE INDEX

This program calculates the simple Lincoln Index estimate of population, with input data supplied by capture-recapture procedures. It also calculates limits of the estimate for a 95% confidence level.

The equations used in these calculations are:

$$\begin{aligned}\text{Population estimate} &= \frac{a n}{r} \\ \text{Standard error} &= \left[\frac{a^2 n(n-r)}{r^3} \right]^{1/2}\end{aligned}$$

a = number marked initially

n = number captured on 2nd occasion

r = number of marked animals recaptured

EXAMPLE

335 animals are marked and released on day 1. 150 are recaptured on day 2, of which 30 are marked. What is the estimated population on day 1?

Answer:

Population Estimate = 1675

95% Confident Limits = 1139 - 2211

Reference: Ecological Methods

by T. R. E. Southwood, 1966,
Methuen and Company, Ltd.

ANIMAL
ECOLOGY
Program 7

X X X

X

X

5

1. PRESS: END
2. ENTER PROGRAM
3. PRESS: CONTINUE
4. ENTER DATA
5. PRESS: CONTINUE
6. PRESS: CONTINUE for new set of data, return to Step 4.

$$\begin{array}{ccc} 1 & 0 & 0 \\ \frac{r}{r} & \frac{n}{r} & \frac{a}{r} \\ \frac{a_n}{r} & \frac{a_n}{r} - 1.96\sqrt{\frac{a_n}{r}} & \frac{a_n}{r} + 1.96\sqrt{\frac{a_n}{r}} \end{array}$$

EXAMPLE

	Data	
	a	335.
	n	150.
	r	30.
Answer:	Upper Limit	2211.11168
	Lower Limit	1138.88834
	Probable Error	1675.00000

ANIMAL ECOLOGY -- 7

00	CLR	20
01	1	01
02	STP	41
03	PNT	45
04	AC+	60
05	RDN	31
06	YTO	40
07	a	13
08	X	36
09	f	15
0a	DIV	35
0b	YTO	40
0c	b	14
0d	a	13
10	UP	27
11	X	36
12	e	12
13	X	36
14	RUP	22
15	f	15
16	-	34
17	RDN	31
18	X	36
19	DN	25
1a	RDN	31
1b	X	36
1c	X	36
1d	RDN	31
20	DIV	35
21	RDN	31
22	✓	76
23	UP	27
24	1	01
25	.	21
26	9	11
27	6	06
28	X	36
29	RDN	31
2a	UP	27
2b	RUP	22
2c	b	14
2d	+	33
30	RUP	22
31	-	34
32	b	14
33	PNT	45
34	PNT	45
35	END	46

POPULATION ESTIMATE AND CONFIDENCE LIMITS
OF REMOVAL TRAPPING

Animals are trapped and removed on a series of occasions, and it is expected that the number caught on subsequent occasions, (and it is expected that the number caught on subsequent occasions) will diminish in a predictable manner. This program uses data from this procedure to predict initial total population and limits for a 95% confidence level.

The equations used in these calculations are:

(1)

$$T = n_1 + n_2 + \dots + n_k = \sum_{i=1}^k n_i$$

T = total catch

n_i = number caught on i^{th} occasion

(2)

$$\sum_{i=1}^k (i - 1) y_i = (1 - 1)n_1 + (2 - 1)n_2 + \dots + (k - 1)n_k$$

k = number of occasions

y_i = the catch on the i^{th} occasion

(3)

$$R = \frac{\sum_{i=1}^k (i - 1) y_i}{T}$$

(4)

$$R = \frac{q^k}{p} = \frac{kq^k}{(1 - q)^k}$$

p = probability of capture
on a single occasion
 q = $1 - p$

(5)

$$P = \frac{T}{(1 - q^k)}$$

P = total population

(6)

$$S.E. \text{ of } P = \sqrt{\frac{P(P - T) T}{T^2 - P(P - T) [(kp)^2 / (1 - p)]}}$$

S.E. = standard error of population

EXAMPLE

In a laboratory experiment, 2,000 beetles were placed in a wheat medium and a removal trapping method was started. At ten minute intervals, for fifty minutes, beetles were removed from the wheat. The number of beetles removed in order of time were:

322, 241, 250, 214, 142

How many beetles were there initially in the box, calculated by the removal method?

$q = .8457$ (calculated by trial and error)

Estimated population: 2,060

Confidence limits (95%) 1727 to 2394

ANIMAL
ECOLOGY
Program 8

	X	X	X	
1.	PRESS: END			
2.	ENTER PROGRAM			
3.	PRESS: CONTINUE		1	0
4.	ENTER DATA		N _i	
5.	PRESS: CONTINUE (Return to step 4.)			
6.	PRESS: SET FLAG (after last data point)			
7.	PRESS: CONTINUE			
	DISPLAY		2	0
8.	PRESS: Y, Z on printer			
9.	ENTER DATA (estimate of less than 1)			
10.	PRESS: CONTINUE			
	DISPLAY		0	R data R q est
11.	If $y \neq z$, PRESS: CONTINUE and re-estimate q			
12.	If $y = z$, PRESS: SET FLAG			
13.	PRESS: CONTINUE			
	DISPLAY		0	0 P est
14.	PRESS: END			
15.	ENTER PROGRAM B			
16.	PRESS: CONTINUE			
	DISPLAY		0	P est P-1.96SE P+1.96SE

ANIMAL
ECOLOGY
Program 8

EXAMPLE

Input Data	{	322.
		241.
		250.
		214.
		142.
		5.
		0.
		0.
$(i + 1)$		8457
q_{est}		
R_{data}		1.66883
R_{calc}		1.66895
		0.
P_{est}		2060.25735
		0.
		0.
95% Confidence Limits	{	2393.60034
		1726.91437
P_{est}		2060.25735

00	CLR	20	40	RUP	22
01	1	01	41	LN	65
02	XTO	23	42	+	33
03	d	17	43	RDN	31
04	STP	41	44	EXP	74
05	PNT	45	45	XEY	30
06	IFG	43	46	EXP	74
07	2	02	47	UP	27
08	4	04	48	1	01
09	AC+	60	49	XEY	30
0a	RDN	31	4a	-	34
0b	d	17	4b	YTO	40
0c	XEY	30	4c	c	16
0d	1	01	4d	RDN	31
10	-	34	50	DIV	35
11	RDN	31	51	RUP	22
12	X	36	52	1	01
13	CLX	37	53	XEY	30
14	AC+	60	54	f	15
15	CLX	37	55	-	34
16	RDN	31	56	f	15
17	d	17	57	XEY	30
18	XEY	30	58	DIV	35
19	1	01	59	RDN	31
1a	+	33	5a	XEY	30
1b	YTO	40	5b	-	34
1c	d	17	5c	b	14
1d	CLX	37	5d	UP	27
20	XEY	30	60	CLX	37
21	GTO	44	61	STP	41
22	0	00	62	PNT	45
23	4	04	63	PNT	45
24	d	17	64	IFG	43
25	UP	27	65	6	06
26	1	01	66	b	14
27	-	34	67	CLR	20
28	YTO	40	68	GTO	44
29	d	17	69	3	03
2a	RCL	61	6a	4	04
2b	DIV	35	6b	a	13
2c	XTO	23	6c	UP	27
2d	a	13	6d	c	16
30	YTO	40	70	DIV	35
31	b	14	71	CLX	37
32	CLR	20	72	UP	27
33	2	02	73	PNT	45
34	STP	41	74	PNT	45
35	PNT	45	75	END	46
36	PNT	45			
37	AC+	60			
38	LN	65			
39	UP	27			
3a	d	17			
3b	X	36			
3c	XEY	30			
3d	UP	27			

00	RDN	31
01	AC+	60
02	a	13
03	-	34
04	X	36
05	e	12
06	X	36
07	YTO	40
08	b	14
09	1	01
0a	UP	27
0b	f	15
0c	-	34
0d	d	17

10	X	36
11	RDN	31
12	UP	27
13	X	36
14	f	15
15	DIV	35
16	RUP	22
17	XEY	30
18	a	13
19	DIV	35
1a	RDN	31
1b	X	36
1c	DN	25
1d	RDN	31

20	X	36
21	RDN	31
22	XEY	30
23	-	34
24	b	14
25	XEY	30
26	DIV	35
27	RDN	31
28	✓	76
29	UP	27
2a	1	01
2b	.	21
2c	9	11
2d	6	06

30	X	36
31	RUP	22
32	DN	25
33	e	12
34	+	33
35	RUP	22
36	-	34
37	e	12
38	PNT	45
39	END	46