

HEWLETT-PACKARD

HP67 HP97

M.E. Pac I



The program material contained herein is supplied without representation or warranty of any kind. Hewlett-Packard Company therefore assumes no responsibility and shall have no liability, consequential or otherwise, of any kind arising from the use of this program material or any part thereof.

Introduction

The 23 programs of ME Pac I have been drawn from the fields of statics, dynamics, stress analysis, machine design, and thermodynamics.

Each program in this pac is represented by one or more magnetic cards and a section in this manual. The manual provides a description of the program with relevant equations, a set of instructions for using the program, and one or more example problems, each of which includes a list of the actual keystrokes required for its solution. Program listings for all the programs in the pac appear at the back of this manual. Explanatory comments have been incorporated in the listings to facilitate your understanding of the actual working of each program. Thorough study of a commented listing can help you to expand your programming repertoire since interesting techniques can often be found in this way.

On the face of each magnetic card are various mnemonic symbols which provide shorthand instructions to the use of the program. You should first familiarize yourself with a program by running it once or twice while following the complete User Instructions in the manual. Thereafter, the mnemonics on the cards themselves should provide the necessary instructions, including what variables are to be input, which user-definable keys are to be pressed, and what values will be output. A full explanation of the mnemonic symbols for magnetic cards may be found in appendix A.

If you have already worked through a few programs in Standard Pac, you will understand how to load a program and how to interpret the User Instructions form. If these procedures are not clear to you, take a few minutes to review the sections, Loading a Program and Format of User Instructions, in your Standard Pac.

We hope that ME Pac I will assist you in the solution of numerous problems in your discipline. We would very much appreciate knowing your reactions to the programs in this pac, and to this end we have provided a questionnaire inside the front cover of this manual. Would you please take a few minutes to give us your comments on these programs? It is in the comments we receive from you that we learn how best to increase the usefulness of programs like these.

Contents

1.	Vector Statics	01-01
	Performs basic vector operations of addition, cross product, and dot product, and finds angles between vectors.	
2.	Section Properties (2 cards)	02-01
	The area, centroid, and moments of an arbitrarily complex polygon may be calculated using this program.	
3.	Stress on an Element	03-01
	Reduces data from rosette strain gage measurement and performs Mohr circle analysis.	
4.	Soderberg's Equation for Fatigue	04-01
	Solves for any one of the seven variables of Soderberg's equation for fatigue.	
5.	Cantilever Beams	05-01
	Calculates deflection, slope, moment and shear for point, distributed, and moment loads applied to cantilever beams.	
6.	Simply Supported Beams	06-01
	Calculates deflection, slope, moment and shear for point, distributed, and moment loads applied to simply supported beams.	
7.	Beams Fixed at Both Ends	07-01
	Calculates deflection, slope, moment, and shear for point, distributed, and moment loads applied to beams fixed at both ends.	
8.	Propped Cantilever Beams	08-01
	Calculates deflection, slope, moment, and shear for point, distributed, and moment loads applied to propped cantilever beams.	
9.	Helical Spring Design	09-01
	Performs one or two point design for helical compression springs.	
10.	Four Bar Function Generator (2 cards)	10-01
	Program designs four bar systems which will approximate an arbitrary function of one variable.	
11.	Progression of Four Bar System	11-01
	Calculates angular displacement, velocity, and acceleration for the output link of a four bar system.	
12.	Progression of Slider Crank	12-01
	Calculates displacement, velocity, and acceleration of the slider and angular velocity and acceleration of the connecting rod for the progression of a slider crank system.	
13.	Circular Cams	13-01
	Computes parameters necessary for design of harmonic, cycloidal, circular cams with roller, flat or point followers.	
14.	Linear Cams	14-01
	Computes the parameters necessary for design of harmonic, cycloidal, or parabolic profiles for linear cams with roller followers.	

15.	Gear Forces	15-01
	Computes the reaction forces resulting from torque applied to helical, bevel, and worm gears.	
16.	Standard External Involute Spur Gears	16-01
	Calculates parameters necessary for the design, manufacture, and testing of standard, external, involute, spur gears.	
17.	Belt Length	17-01
	Computes belt length around an arbitrary set of pulleys.	
18.	Free Vibrations	18-01
	Calculates an exact solution to the differential equation for a damped oscillator vibrating freely.	
19.	Vibration Forced by $F_0 \cos \omega t$	19-01
	Finds the steady-state solution for a damped oscillator forced by $F_0 \cos \omega t$.	
20.	Equations of State	20-01
	Ideal gas relation plus Redlich-Kwong model of real gas behavior.	
21.	Isentropic Flow for Ideal Gases	21-01
	Replaces isentropic flow tables for ideal gases in converging-diverging passages.	
22.	Conduit Flow	22-01
	Calculates velocity or pressure drop for incompressible viscous flow in conduits.	
23.	Heat Exchangers (2 cards)	23-01
	Performs analysis of counter-flow, parallel-flow, parallel-counter-flow and cross-flow (fluids unmixed) heat exchangers.	
	Program Listings	L00-01
	Appendix A—Card Mnemonic	A1

A WORD ABOUT PROGRAM USAGE

This application pac has been designed for both the HP-97 Programmable Printing Calculator and the HP-67 Programmable Pocket Calculator. The most significant difference between the HP-67 and the HP-97 calculators is the printing capability of the HP-97. The two calculators also differ in a few minor ways. The purpose of this section is to discuss the ways that the programs in this pac are affected by the difference in the two machines and to suggest how you can make optimal use of your machine, be it an HP-67 or an HP-97.

Many of the computed results in this pac are output by PRINT statements; on the HP-97 these results will be output on the printer. On the HP-67 each PRINT command will be interpreted as a PAUSE: the program will halt, display the result for about five seconds, then continue execution. The term "PRINT/PAUSE" is used to describe this output condition.

If you own an HP-67, you may want more time to copy down the number displayed by a PRINT/PAUSE. All you need to do is press any key on the keyboard. If the command being executed is PRINTx (eight rapid blinks of the decimal point), pressing a key will cause the program to halt. Execution of the halted program may be re-initiated by pressing **R/S**.

HP-97 users may also want to keep a permanent record of the values input to a certain program. A convenient way to do this is to set the Print Mode switch to NORMAL before running the program. In this mode all input values and their corresponding user-definable keys will be listed on the printer, thus providing a record of the entire operation of the program.

Another area that could reflect differences between the HP-67 and the HP-97 is in the keystroke solutions to example problems. It is sometimes necessary in these solutions to include operations that involve prefix keys, namely, **f** on the HP-97 and **f**, **g**, and **h** on the HP-67. For example, the operation 10^x is performed on the HP-97 as **f** 10^x and on the HP-67 as **g** 10^x . In such cases, the keystroke solution omits the prefix key and indicates only the operation (as here, 10^x). As you work through the example problems, take care to press the appropriate prefix keys (if any) for your calculator.

Also in keystroke solutions, those values that are output by the PRINT command will be followed by three asterisks (***)

Notes

VECTOR STATICS

VECTOR STATICS

$$r_1 + \theta_1$$

$$r_2 + \theta_2$$

$$-\vec{V}_1 + \vec{V}_2$$

$$+\vec{V}_1 + \vec{V}_2$$

$$+\vec{V}_1 + \vec{V}_2 \cdot \gamma$$

Part I of this program performs the basic two dimensional vector operations of addition, cross product and dot, scalar, or inner product. In addition, the angle between vectors may be found. Vectors may be input in polar form (r, θ) or rectangular form (x_1, y_1).

Equations:

for addition: $\vec{V}_1 + \vec{V}_2 = (x_1 + x_2) \hat{i} + (y_1 + y_2) \hat{j}$

for cross products: $\vec{V}_1 \times \vec{V}_2 = (x_1 y_2 - x_2 y_1) \hat{k}$

for dot, scalar, or inner product: $\vec{V}_1 \cdot \vec{V}_2 = x_1 x_2 + y_1 y_2$

for the angle between vectors: $\gamma = \cos^{-1} \frac{\vec{V}_1 \cdot \vec{V}_2}{|\vec{V}_1| |\vec{V}_2|}$

where:

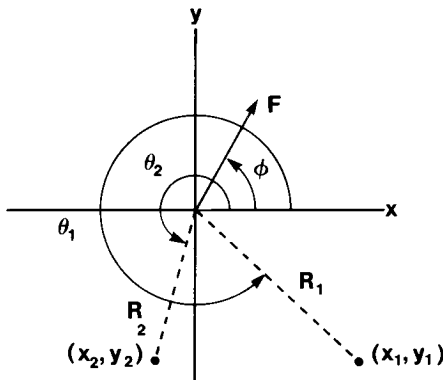
x_1 is the x component of $\vec{V}_1$ ($x_1 = r_1 \cos \theta_1$);

x_2 is the x component of $\vec{V}_2$ ($x_2 = r_2 \cos \theta_2$);

y_1 is the y component of $\vec{V}_1$ ($y_1 = r_1 \sin \theta_1$);

y_2 is the y component of $\vec{V}_2$ ($y_2 = r_2 \sin \theta_2$);

Part II of this program calculates the two reaction forces necessary to balance a given two-dimensional force vector. The direction of the reaction forces may be specified as a vector of arbitrary length or by Cartesian coordinates using the point of force application as the origin.



Equations:

$$R_1 \cos \theta_1 + R_2 \cos \theta_2 = F \cos \phi$$

$$R_1 \sin \theta_1 + R_2 \sin \theta_2 = F \sin \phi$$

where:

F is the known force;

ϕ is the direction of the known force;

R_1 is one reaction force;

θ_1 is the direction of R_1 ;

R_2 is the second reaction force;

θ_2 is the direction of R_2 .

The coordinates x_1 and y_1 are referenced from the point where F is applied to the end of the member along which R_1 acts; x_2 and y_2 are the coordinates referenced from the point where F is applied to the end of the member along which R_2 acts.

Remarks:

Registers $R_0 - R_3$; $R_{S0} - R_{S9}$ and I are available for user storage.

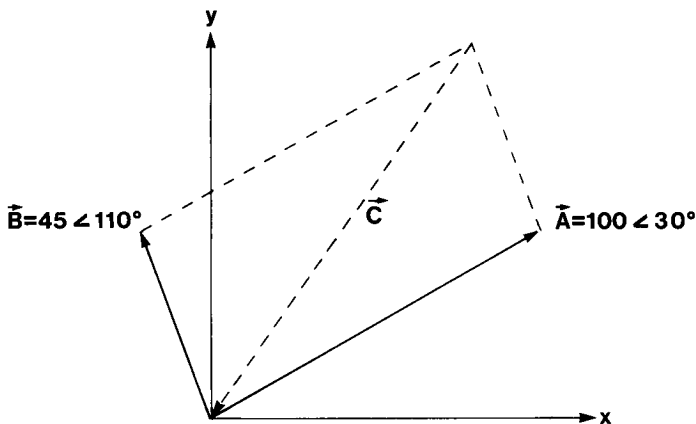
STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
1	Load side 1 and side 2.			
2	To resolve a force in two known directions, go to step 6.			
	For vector addition, cross product, or dot product continue with step 3.			
3	Input $\vec{V}_1$ and $\vec{V}_2$:			
	$\vec{V}_1$ in polar form	r_1	ENTER	r_1
		θ_1	A	y_1
	or			
	$\vec{V}_1$ in rectangular form	x_1	ENTER	x_1
		y_1	I A	y_1
	and			
	$\vec{V}_2$ in polar form	r_2	ENTER	r_2
		θ_2	B	y_2
	or			

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
	$\vec{V}_2$ in rectangular form.	x_2	ENTER	x_2
		y_2	f B	y_2
4	Perform vector operation:			
	add vectors		C	r, θ
	or			
	take cross product		D	$\vec{V}_1 \times \vec{V}_2$
	or			
	take dot (or scalar) product.		E	$\vec{V}_1 \cdot \vec{V}_2$
	(Optionally, calculate angle			
	between vectors after dot			
	product.)		R/S	γ
5	For a new case, go to step 3			
	and change $\vec{V}_1$ and/or $\vec{V}_2$.			
6	Define reaction directions as			
	Cartesian coordinates or as			
	vectors of arbitrary magnitude.			
	(Use the point of force appli-			
	cations as the origin):			
	define direction one in polar			
	form	1	ENTER	1.00
		θ_1	A	$\sin \theta_1$
	or			
	in rectangular form	x_1	ENTER	x_1
		y_1	f A	y_1
	and			
	define direction two in polar			
	form	1	ENTER	1.00
		θ_2	B	$\sin \theta_2$
	or			
	in rectangular form.	x_2	ENTER	x_2
		y_2	f B	y_2

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
7	Input known force:			
	magnitude	F	ENTER	F
	then direction.	ϕ	f D	$F \sin \phi$
8	Compute reactions		f E	R_1, R_2
9	To change force, go to step 7.			
	To change either or both			
	directions, go to step 6.			

Example 1:

Forces A and B are shown below. If static equilibrium exists, what is force C.

**Keystrokes:****Outputs:**

To obtain $\vec{C}$, add $\vec{A}$ and $\vec{B}$ using negative magnitudes for both.

45 **CHS** **ENTER** 110 **A** 100 **CHS**
ENTER 30 **B** **C** $\longrightarrow$

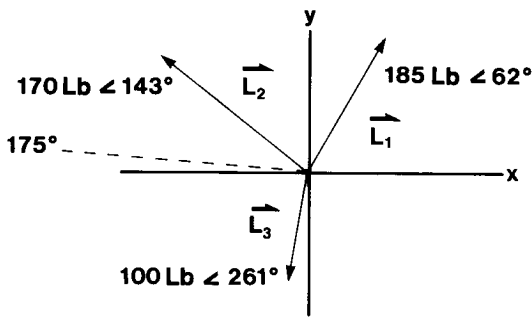
116.57 ***

-127.66 ***

$$\vec{C} = 116.57 \angle -127.66^\circ$$

Example 2:

Resolve the following three loads along a 175 degree line.



Keystrokes:

First add $\vec{L}_1$ and $\vec{L}_2$.

185 **ENTER** 62 **A** 170 **ENTER**
143 **B** **C** $\longrightarrow$

Define the result as $\vec{V}_1$ and add $\vec{L}_3$.

A 100 **ENTER** 261 **B** **C** $\longrightarrow$

To resolve the vector, just calculated
along the 175° line.

A 1 **ENTER** 175 **B** **E** $\longrightarrow$

What is the angle between the
vector and the line?

R/S $\longrightarrow$

Outputs:

270.12 *** (lb)
100.43 *** (deg)

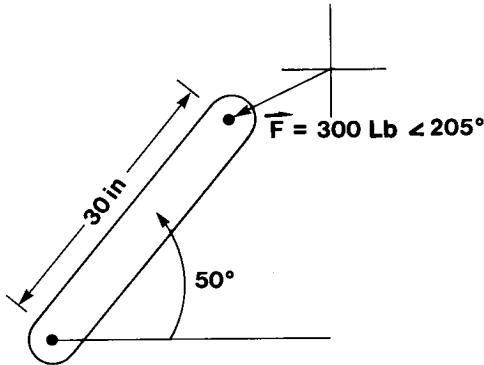
178.94 *** (lb)
111.15 *** (deg)

78.86 *** (lb)

63.85 *** (deg)

Example 3:

What is the moment at the shaft of the crank pictured below? What is the reaction force transmitted along the member?

**Keystrokes:**

Moment by cross product ($\vec{r}_1 \times \vec{F}$).

30 **ENTER** 50 **A** 300 **ENTER**

205 **B D** $\longrightarrow$

Resolution along crank

1 **ENTER** 50 **A E** $\longrightarrow$

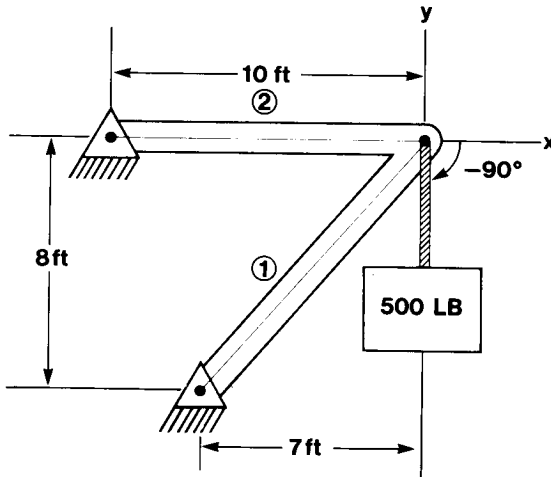
Outputs:

3803.56 in-lb

-271.89 lb

Example 4:

Find the reaction forces in the pin-jointed structure shown below.

**Keystrokes:**

```

7 CHS ENTER 8 CHS f A  →
10 CHS ENTER 0 f B  →
500 ENTER 90 CHS f D  →
f E  →

```

Outputs:

```

-8.00
0.00
-500.00
-664.38 *** (R1)
437.50 *** (R2)

```

Notes

SECTION PROPERTIES

SECTION PROPERTIES - INPUT	
$(x_i, y_i) x_{i+1}, y_{i+1}$	x_0, y_0, d

SECTION PROPERTIES - OUTPUT			
$\bar{x}, \bar{y}, A$	I_x, I_y, I_{xy}	$I_{\bar{x}}, I_{\bar{y}}, I_{\bar{xy}}$	$\Phi, I_{x\Phi}, I_{y\Phi}$

The properties of polygonal sections (see figure 1) may be calculated using this program. The (x, y) coordinates of the vertices of the polygon (which must be located entirely within the first quadrant) are input sequentially for a complete, clockwise path around the polygon. Holes in the cross section, which do not intersect the boundary, may be deleted by following a counter-clockwise path.

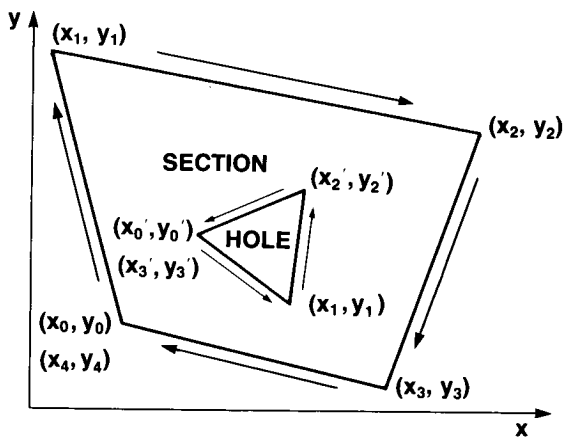


Figure 1 — Polygonal Sections

A special feature allows addition or deletion of circular areas. After the point by point traverse of the section has been completed, circular deletions or additions are specified by the (x, y) coordinates of the circle centers and by the circle diameters. If the diameter is specified as a positive number, the circular areas are added. A negative diameter causes circular areas to be deleted. Example 4 shows an application of this feature.

After all values have been input, the coordinates of the centroid $(\bar{x}, \bar{y})$ and the area (A) of the section may be output using card 2, key **A**. The moment of inertia about the x axis (I_x), about the y axis (I_y) and the product of inertia (I_{xy}) are output using **B**. Similar moments, $I_{\bar{x}}$, $I_{\bar{y}}$ and $I_{\bar{xy}}$, about an axis translated to the centroid of the section are calculated when **C** is pressed.

Pressing **D** calculates the moments of inertia, $I_{\bar{x}\phi}$ and $I_{\bar{y}\phi}$, about the principal axis. The rotation angle (ϕ) between the principal axis and the axis which was translated to the centroid is also calculated. The moments of inertia I_x' , I_y' , the polar moment of inertia J and the product of inertia I_{xy}' may be calculated about any arbitrary axis by specifying its location and rotation with respect to the original axis and pressing **f D**.

Equations:

$$A = - \sum_{i=0}^n (y_{i+1} - y_i)(x_{i+1} + x_i)/2$$

$$\bar{x} = \frac{-1}{A} \sum_{i=0}^n [(y_{i+1} - y_i)/8] [(x_{i+1} + x_i)^2 + (x_{i+1} - x_i)^2/3]$$

$$\bar{y} = \frac{1}{A} \sum_{i=0}^n [(x_{i+1} - x_i)/8] [(y_{i+1} + y_i)^2 + (y_{i+1} - y_i)^2/3]$$

$$I_x = \sum_{i=0}^n [(x_{i+1} - x_i)(y_{i+1} + y_i)/24] [(y_{i+1} + y_i)^2 + (y_{i+1} - y_i)^2]$$

$$I_y = - \sum_{i=0}^n [(y_{i+1} - y_i)(x_{i+1} + x_i)/24] [(x_{i+1} + x_i)^2 + (x_{i+1} - x_i)^2]$$

$$I_{xy} = \sum_{i=0}^n \frac{1}{(x_{i+1} - x_i)} \left[\frac{1}{8} (y_{i+1} - y_i)^2 (x_{i+1} + x_i) (x_{i+1}^2 + x_i^2) \right. \\ \left. + \frac{1}{3} (y_{i+1} - y_i)(x_{i+1} y_i - x_i y_{i+1})(x_{i+1}^2 + x_{i+1} x_i + x_i^2) \right. \\ \left. + \frac{1}{4} (x_{i+1} y_i - x_i y_{i+1})^2 (x_{i+1} + x_i) \right]$$

$$I_{\bar{x}} = I_x - A\bar{y}^2$$

$$I_{\bar{y}} = I_y - A\bar{x}^2$$

$$I_{\bar{x}\bar{y}} = I_{xy} - A\bar{x}\bar{y}$$

$$\phi = \frac{1}{2} \tan^{-1} \left(\frac{-2I_{\bar{x}\bar{y}}}{I_{\bar{x}} - I_{\bar{y}}} \right)$$

$$I_x' = I_{\bar{x}} \cos^2 \theta + I_{\bar{y}} \sin^2 \theta - I_{\bar{x}\bar{y}} \sin 2\theta$$

$$I_y' = I_{\bar{y}} \cos^2 \theta + I_{\bar{x}} \sin^2 \theta + I_{\bar{x}\bar{y}} \sin 2\theta$$

$$J = I_x' + I_y'$$

$$I_{xy}' = \frac{(I_{\bar{x}} - I_{\bar{y}})}{2} \sin 2\theta + I_{\bar{x}\bar{y}} \cos 2\theta$$

$$A_{\text{circle}} = \frac{\pi d^2}{4}$$

$$I_{\text{circle}} = \frac{\pi d^4}{64}$$

where:

x_{i+1} is the x coordinate of the current vertex point;

y_{i+1} is the y coordinate of the current vertex point;

x_i is the x coordinate of the previous vertex point;

y_i is the y coordinate of the previous vertex point;

A is the area;

$\bar{x}$ is the x coordinate of the centroid;

$\bar{y}$ is the y coordinate of the centroid;

I_x is the moment of inertia about the x-axis;

I_y is the moment of inertia about the y-axis;

I_{xy} is the product of inertia;

$I_{\bar{x}}$ is the moment of inertia about the x-axis translated to the centroid;

$I_{\bar{y}}$ is the moment of inertia about the y-axis translated to the centroid;

$I_{\bar{x}\bar{y}}$ is the product of inertia about the translated axis;

ϕ is the angle between the translated axis and the principal axis;

$I_{\bar{x}\phi}$ is the moment of inertia about the translated, rotated, principal x-axis;

$I_{\bar{y}\phi}$ is the moment of inertia about the translated, rotated, principal y-axis;

θ is the angle between the original axis and an arbitrary axis.

I_x' is the x moment of inertia about the arbitrary axis;

I_y' is the y moment of inertia about the arbitrary axis;

J is the polar moment of inertia about the arbitrary axis;

I_{xy}' is the product of inertia about the arbitrary axis;

d is the diameter of a circular area.

Reference:

Wojciechowski, Felix; *Properties of Plane Cross Sections; Machine Design*; P. 105, Jan. 22, 1976.

Remarks:

Registers $R_{S0} - R_{S9}$ are available for user storage.

The polygon must be entirely contained in the first quadrant.

Rounding errors will accumulate if the centroid of the section is a large distance from the origin of the coordinate system.

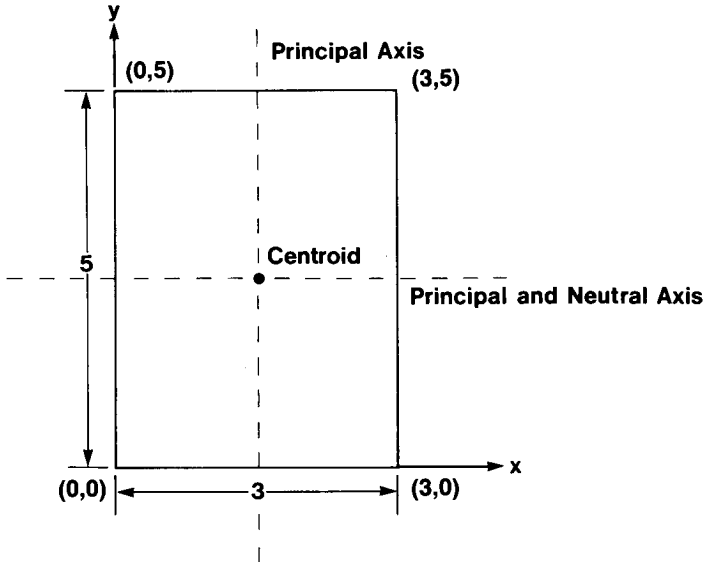
Curved boundaries may be approximated by straight line segments.

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
1	Load side 1 and side 2 of card 1.			
2	Initialize.		I A	
3	Key in (x, y) coordinates of first vertex.	x_i	ENTER	y_i
		y_i	ENTER	y_i
4	Key in (x, y) coordinates of next clockwise vertex.	x_{i+1}	ENTER	x_{i+1}
		y_{i+1}	A	y_{i+1}
5	Wait for execution to end, then repeat step 4 for next point.			
	Go to step 6 after you have reinput the starting point.			
6	To delete subsections within the section just traversed, return to step 3, but traverse in a counter-clockwise direction.			

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
7	Optional: Add circular areas,	x	ENTER	x
		y	ENTER	y
		d	C	0.00
	or delete circular areas.	x	ENTER	x
		y	ENTER	y
		d	CHS C	0.00
8	Load side 1 and side 2 of card 2.			
9	Calculate any or all of the following:			
	Centroid and area;		A	$\bar{x}, \bar{y}, A$
	Properties about original axis;		B	I_x, I_y, I_{xy}
	Properties about axis translated to centroid;		C	$I_{\bar{x}}, I_{\bar{y}}, I_{\bar{x}\bar{y}}$
	Angular orientation of principal axis and properties about principal axis;		D	$\phi, I_{\bar{x}\phi}, I_{\bar{y}\phi}$
	or			
	Specify arbitrary axis and rotation and calculate properties.	x'	ENTER	
		y'	ENTER	
		θ	f D	$I_{x'}, I_{y'}, J, I_{xy'}$
10	To modify the section, go to step 1, but skip step 2. For a new case, go to step 1.			

Example 1:

What is the moment of inertia about the x-axis (I_x) for the rectangular section shown? What is the moment of inertia about the neutral axis through the centroid of the section ($I_{\bar{x}\phi}$)?

**Keystrokes:**

Load side 1 and side 2 of card 1.

f **A** 0 **ENTER** 0 **ENTER**

0 ENTER 5 A	→	5.00
3 ENTER 5 A	→	5.00
3 ENTER 0 A	→	0.00
0 ENTER 0 A	→	0.00

Load side 1 and side 2 of card 2.

B →

125.00 *** (I_x)

45.00 *** (I_y)

56.25 *** (I_{xy})

D →

0.00 *** (ϕ)

31.25 *** ($I_{\bar{x}\phi}$)

11.25 *** ($I_{\bar{y}\phi}$)

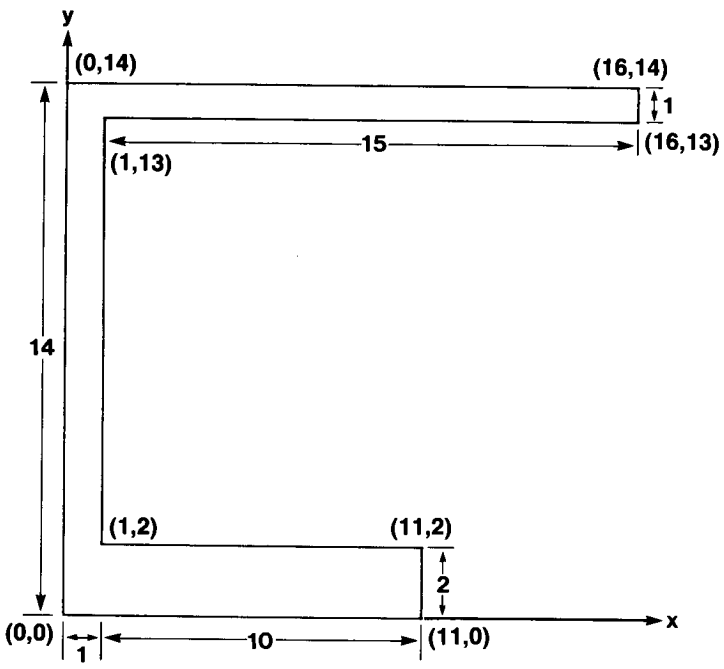
Since $\phi = 0$ we would expect $I_{\bar{x}\phi}$ to equal $I_{\bar{x}}$. Press **C** to calculate $I_{\bar{x}}$, $I_{\bar{y}}$ and $I_{\bar{x}\bar{y}}$ and you will see that this prediction is correct. Also, $I_{\bar{x}\bar{y}}$ is zero about the principal axis.

C →

31.25 *** ($I_{\bar{x}}$)
11.25 *** ($I_{\bar{y}}$)
0.00 *** ($I_{\bar{x}\bar{y}}$)

Example 2:

Calculate the section properties for the beam shown below.



Keystrokes:

Load side 1 and side 2 of card 1.

1 **A** **0** **ENTER** **0** **ENTER**

0 **ENTER** 14 **A** →

16 **ENTER** 14 **A** →

16 **ENTER** 13 **A** →

1 **ENTER** 13 **A** →

1 **ENTER** 2 **A** →

11 **ENTER** 2 **A** →

11 **ENTER** 0 **A** →

Outputs:

14.00

14.00

13.00

13.00

2.00

2.00

0.00

0 **ENTER** 0 **A** $\longrightarrow$

0.00

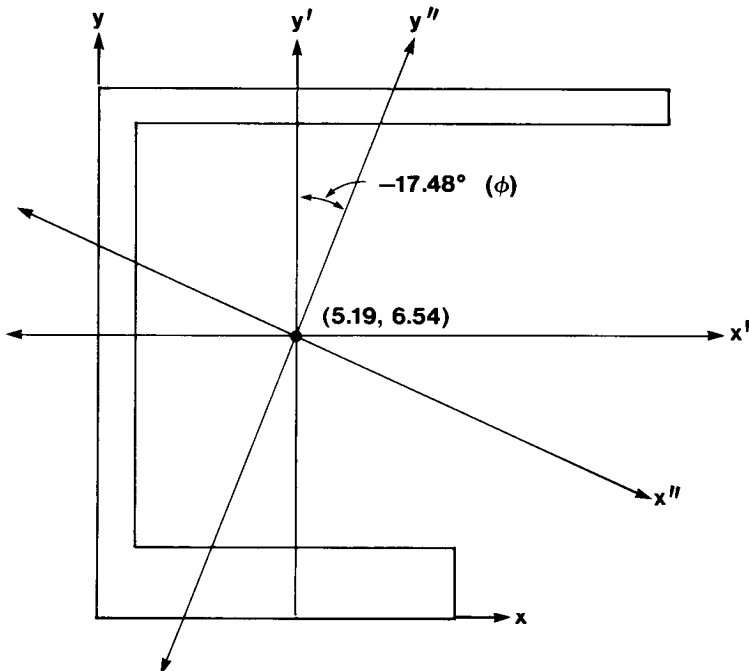
Load side 1 and side 2 of card 2.

A $\longrightarrow$ 5.19 *** ($\bar{x}$)6.54 *** ($\bar{y}$)

49.00 *** (A)

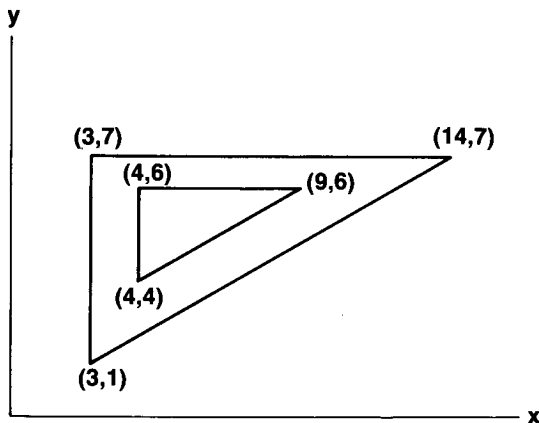
B $\longrightarrow$ 3676.33 *** (I_x)2256.33 *** (I_y)1890.25 *** (I_{xy})**C** $\longrightarrow$ 1580.00 *** ($I_{\bar{x}}$)934.49 *** ($I_{\bar{y}}$)225.61 *** ($I_{\bar{x}\bar{y}}$)**D** $\longrightarrow$ -17.48 *** (ϕ)1651.04 *** ($I_{\bar{x}\phi}$)863.46 *** ($I_{\bar{y}\phi}$)

Below is a figure showing the translated axis and the rotated, principal axis of example 2.



Example 3:

What is the centroid of the section below? The inner triangular boundary denotes an area to be deleted.

**Keystrokes:**

Load side 1 and side 2 of card 1.

f A 3 ENTER 1 ENTER

3 ENTER 7 A →

14 ENTER 7 A →

3 ENTER 1 A →

Delete inner triangle:

4 ENTER 4 ENTER 9 ENTER

6 A →

4 ENTER 6 A →

4 ENTER 4 A →

Load side 1 and side 2 of card 2.

Compute Centroid

A →

Outputs:

7.00

7.00

1.00

6.00

6.00

4.00

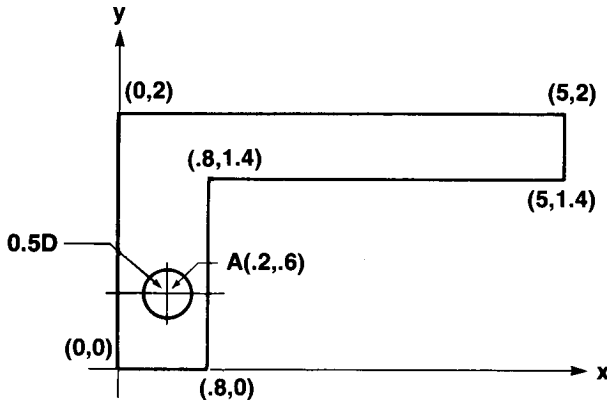
6.85 *** ($\bar{x}$)

4.94 *** ($\bar{y}$)

28.00 *** (A)

Example 4:

For the part below, compute the polar moment of inertia about point A. Point A denotes the center of a hole about which the part rotates. The area of the hole must be deleted from the cross section.

**Keystrokes:**

Load side 1 and side 2 of card 1.

```
f A 0 ENTER 0 ENTER 0 ENTER
2 A 5 ENTER 2 A 5 ENTER
1.4 A .8 ENTER 1.4 A .8 ENTER
0 A 0 ENTER 0 A
```

0.00

Delete the hole.

```
.2 ENTER .6 ENTER
.5 CHS C
```

0.00

Load side 1 and side 2 of card 2.

Compute J about point (.2, .6) with θ of zero.

```
.2 ENTER .6 ENTER
0 f D
```

```
3.91 *** (Ix)
22.22 *** (Iy)
26.13 *** (J)
7.61 *** (Ixy)
```

STRESS ON AN ELEMENT



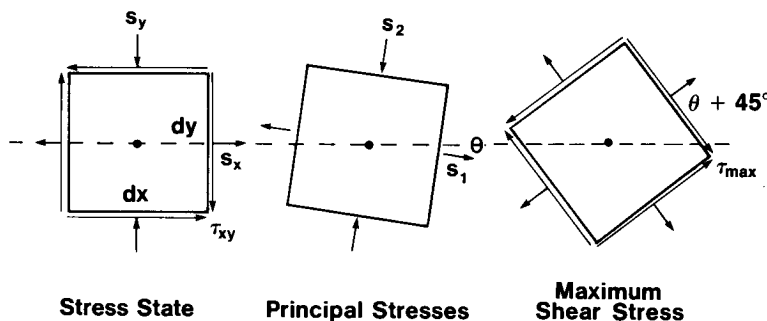
This program reduces data from rosette strain gage measurements and/or performs Mohr circle stress analysis calculations.

Correlations for rectangular and equiangular rosette configurations are included.

Strain Gage Equations:

CONFIGURATION CODE	1	2
TYPE OF ROSETTE	RECTANGULAR	DELTA (EQUIANGULAR)
PRINCIPAL STRAINS: ϵ_1, ϵ_2	$\frac{1}{2} [\epsilon_a + \epsilon_c \pm \sqrt{2(\epsilon_a - \epsilon_b)^2 + 2(\epsilon_b - \epsilon_c)^2}]$	$\frac{1}{3} [\epsilon_a + \epsilon_b + \epsilon_c \pm \sqrt{2(\epsilon_a - \epsilon_b)^2 + 2(\epsilon_b - \epsilon_c)^2 + 2(\epsilon_c - \epsilon_a)^2}]$
CENTER OF MOHR CIRCLE: $\frac{S_1 + S_2}{2}$	$\frac{E(\epsilon_a + \epsilon_c)}{2(1 - \nu)}$	$\frac{E(\epsilon_a + \epsilon_b + \epsilon_c)}{3(1 - \nu)}$
MAXIMUM SHEAR STRESS: τ_{max}	$\frac{E}{2(1 + \nu)} \sqrt{2(\epsilon_a - \epsilon_b)^2 + 2(\epsilon_b - \epsilon_c)^2}$	$\frac{E}{3(1 + \nu)} \sqrt{2(\epsilon_a - \epsilon_b)^2 + 2(\epsilon_b - \epsilon_c)^2 + 2(\epsilon_c - \epsilon_a)^2}$
ORIENTATION OF PRINCIPAL STRESSES	$\tan^{-1} \left[\frac{2\epsilon_b - \epsilon_a - \epsilon_c}{\epsilon_a - \epsilon_c} \right]$	$\tan^{-1} \left[\frac{\sqrt{3} (\epsilon_c - \epsilon_b)}{(2\epsilon_a - \epsilon_b - \epsilon_c)} \right]$

The Mohr circle portion of the program converts an arbitrary stress configuration to principal stresses, maximum shear stress and rotation angle. It is then possible to calculate the state of stress for an arbitrary orientation θ' .



Mohr Circle Equations:

$$\tau_{\max} = \sqrt{\left(\frac{s_x - s_y}{2}\right)^2 + \tau_{xy}^2}$$

$$s_1 = \frac{s_x + s_y}{2} + \tau_{\max}$$

$$s_2 = \frac{s_x + s_y}{2} - \tau_{\max}$$

$$\theta = \frac{1}{2} \tan^{-1} \left(\frac{2\tau_{xy}}{s_x - s_y} \right)$$

$$s = \frac{s_1 + s_2}{2} + \tau_{\max} \cos 2\theta'$$

$$\tau = \tau_{\max} \sin 2\theta'$$

where:

s is the normal stress, and τ is the shear stress.

ϵ_a , ϵ_b , and ϵ_c are the strains measured using rosette gages;

s_x is the stress in the x direction for Mohr circle input;

s_y is the stress in the y direction for Mohr circle input;

τ_{xy} is the shear stress on the element for Mohr circle input;

ϵ_1 and ϵ_2 are the principal strains;

s_1 and s_2 are the principal normal stresses;

$\tau_{\max}$ is the maximum shear stress;

θ is the counterclockwise angle of rotation from the specified axis to the principal axis. Note that this is opposite to the normal Mohr circle convention.

θ' is an arbitrary rotation angle from the original (x, y) axis;

E is modulus of elasticity.

ν is the Poisson's ratio.

Reference:

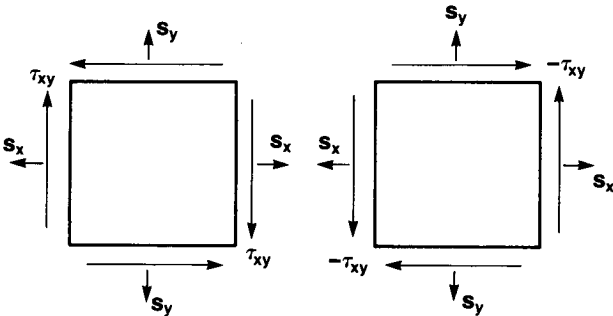
Spotts, M.F., *Design of Machine Elements*, Prentice-Hall, 1971.

Beckwith, T. G., Buck, N. L., *Mechanical Measurements*, Addison-Wesley, 1969

Remarks:

R_0 , R_1 , R_7 , R_8 , R_D and R_{S0} – R_{S9} are available for user storage.

Negative stresses and strains indicate compression. Positive and negative shear are represented below:

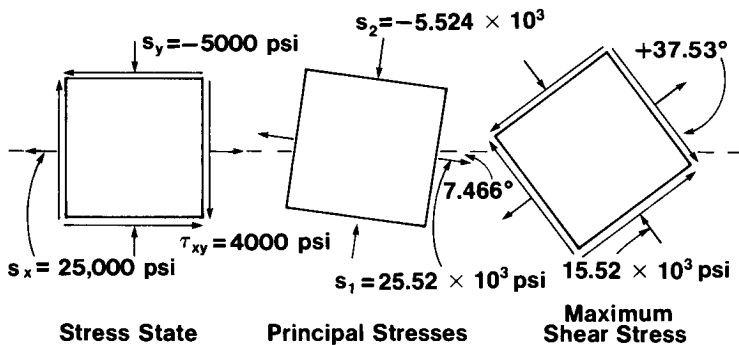


STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
1	Load side 1 and side 2.			
2	If a stress configuration is known, go to step 8 for Mohr circle evaluation. Continue with step 3 for strain gage data reduction.			
3	Select strain gage configuration:			
	Rectangular		F A	1.000 00
	or Delta.		F B	2.000 00

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
4	Input modulus of elasticity,	E	ENTER	E
	then Poisson's ratio.	ν	f D	E
5	Input strains:			
		ϵ_a	ENTER	ϵ_a
		ϵ_b	ENTER	ϵ_b
		ϵ_c	A	ϵ_a
6	Calculate principal strains			
	and rotation angle.		B	$\epsilon_1, \epsilon_2, \theta$
7	Skip to step 9 for Mohr circle			
	applications of calculations			
	just completed.			
8	Input stress on element in x			
	direction	s_x	ENTER	s_x
	then stress in y direction	s_y	ENTER	s_y
	then shear stress.	τ_{xy}	C	0.000 00
9	Calculate principal stresses.		D	$s_1, s_2, \tau_{max},$
				θ
10	Optional: Calculate stress			
	configuration at a specified			
	angle.	θ'	E	s, τ
11	To specify another angle go			
	to step 10. For a new case go			
	to step 2.			

Example 1:

If $s_x = 25000$ psi, $s_y = -5000$ psi, and $\tau_{xy} = 4000$ psi, compute the principal stresses and the maximum shear stress. Compute the normal stresses, where shear stress is maximum ($\theta + 45^\circ$).



Keystrokes:

25000 **ENTER** 5000 **CHS** **ENTER**
 4000 **C** **D** →

45 **+** →
E →

Outputs:

25.52 03 *** (s_1)
 -5.524 03 *** (s_2)
 15.52 03 *** (τ_{max})
 -7.466 00 *** (θ)
 37.53 00
 10.00 03 *** (s)
 15.52 03 *** (τ_1)

Example 2:

A rectangular rosette measures the strains below. What are the principal strains and principal stresses?

$$\epsilon_a = 90 \times 10^{-6} \quad \epsilon_b = 137 \times 10^{-6} \quad \epsilon_c = 305 \times 10^{-6}$$

$$\nu = 0.3 \quad E = 30 \times 10^6 \text{ psi}$$

Keystrokes:

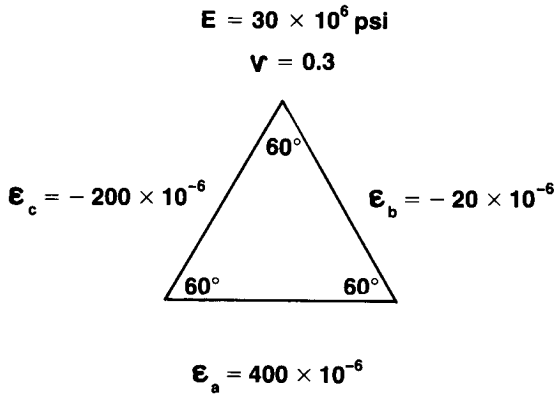
f **A** →
 30 **EEX** 6 **ENTER** .3 **f** **D** →
 90 **EEX** **CHS** 6 **ENTER** 137
EEX **CHS** 6 **ENTER** 305 **EEX** **CHS**
 6 **A** →
B →
D →

Outputs:

1.000 00
 30.00 06
 90.00-06
 320.9-06 *** (ϵ_1)
 74.14-06 *** (ϵ_2)
 14.69 00 *** (θ)
 11.31 03 *** (s_1)
 5.618 03 *** (s_2)
 2.847 03 *** (τ_{max})
 14.69 00 *** (θ)

Example 3:

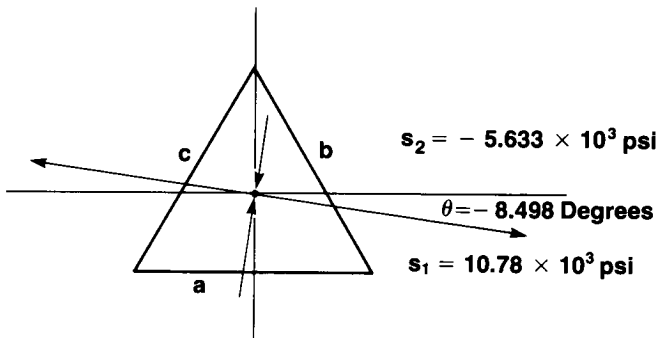
An equiangular rosette measures the strains below. What are the principal strains and stresses?

**Keystrokes:**

f B →
 30 **EEX** 6 **ENTER** .3 **f D**
 400 **EEX** **CHS** 6 **ENTER** 20
CHS **EEX** **CHS** 6 **ENTER** 200
CHS **EEX** **CHS** 6 **A** →
B →
D →

Outputs:

2.000 00
 400.0-06
 415.5-06 *** (ϵ_1)
 -295.5-06 *** (ϵ_2)
 -8.498 00 *** (θ)
 10.78 03 *** (s_1)
 -5.633 03 *** (s_2)
 8.204 03 *** ($\tau_{\max}$)
 -8.498 00 *** (θ)

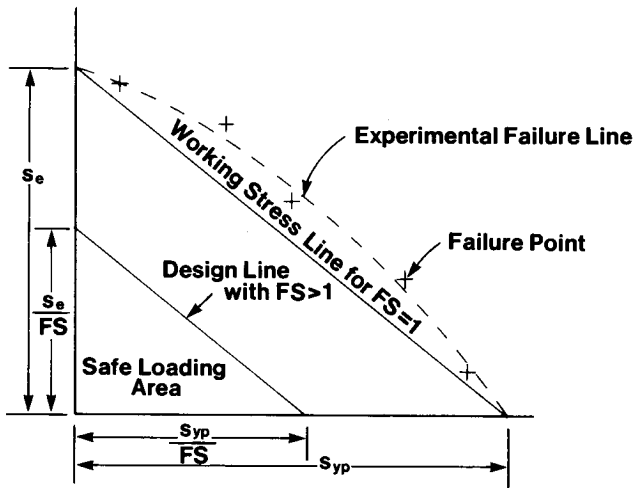


SODERBERG'S EQUATION FOR FATIGUE



This program will calculate the seventh variable from the other six values in Soderberg's equation. It is useful in sizing parts for cyclic loading, calculating factors of safety, choosing materials based on size constraints and estimating the fatigue resistance of available parts. Soderberg's equation is graphically represented in figure 1.

Equations:



Working Stress Diagram
Figure 1

$$\frac{S_{yp}}{FS} = \frac{S_{max} + S_{min}}{2} + K \left(\frac{S_{yp}}{S_e} \right) \left(\frac{(S_{max} - S_{min})}{2} \right)$$

$$\frac{S_{max} + S_{min}}{2} = \frac{P_{max} + P_{min}}{2A}$$

$$\frac{S_{max} - S_{min}}{2} = \frac{P_{max} - P_{min}}{2A}$$

where:

S_{yp} is the yield point stress of the material;

S_e is the material endurance stress from reversed bending tests;

K is the stress concentration factor for the part;

FS is the factor of safety ($FS \geq 1.00$)

$s_{\max}$ is the maximum stress;

$s_{\min}$ is the minimum stress;

$P_{\max}$ is the maximum load;

$P_{\min}$ is the minimum load;

A is the cross sectional area of the part.

Reference:

Spotts, M. F., *Design of Machine Elements*; Prentice-Hall, Inc., 1971.

Baumeister, T. *Marks Standard Handbook for Mechanical Engineers*, McGraw-Hill Book Company, 1967.

Remarks:

If $s_{\max}$ and $s_{\min}$ are to be input or calculated instead of $P_{\max}$ or $P_{\min}$, simply use 1.00 for the value of area.

R_0 – R_7 , R_{S0} – R_{S9} and I are available for storage.

This implementation of Soderberg's equation is for ductile materials only.

Values of stress concentration factors and material endurance limits may be found in the referenced sources.

In the presence of corrosive media, or for rough surfaces, fatigue effects may be much more significant than predicted by this program.

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
1	Load side 1 and side 2.			
2	Input six of the following seven			
	Yield point stress	S_{yp}	F A	S_{yp}
	Endurance stress	S_e	F B	S_e
	Cross sectional area	A	A	A
	Stress concentration factor	K	B	K
	Maximum load	$P_{\max}$	C	$P_{\max}$
	Minimum load	$P_{\min}$	D	$P_{\min}$
	Factor of safety	FS	E	FS

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
3	Calculate the remaining value:			
	Yield point stress		f A	S_{yp}
	Endurance stress		f B	S_e
	Cross sectional area		A	A
	Stress concentration factor		B	K
	Maximum load		C	P_{max}
	Minimum load		D	P_{min}
	Factor of safety		E	FS
4	Optional: Output values in			
	S_{yp} , S_e , A, K, P_{max} , P_{min} ,			
	FS order.		f C	OUTPUT
5	For a new case, go to step 2			
	and change appropriate			
	inputs.			

Example 1:

What is the maximum permissible cyclic load for a part if the minimum load is 2000 pounds and the area is 0.5 square inches?

$s_{yp} = 70000 \text{ psi}$

$s_e = 25000 \text{ psi}$

$K = 1.25$

$FS = 2.0$

Keystrokes:

70000 **f A** 25000 **f B** .5 **A**
1.25 **B** 2000 **D** 2 **E C** →

If P_{max} is changed to 10000 pounds
what will s_e have to be?

10000 **C f B** →

Outputs:

8.889 03 (P_{max})

30.43 03 (s_e)

If s_e is changed back to 25000 psi
what will the factor of safety be?

25000 **f B E** →

1.750 00 (FS)

Output values for review:

f C →

70.00 03 *** (s_{yp})

25.00 03 *** (s_e)

500.0 -03 *** (A)

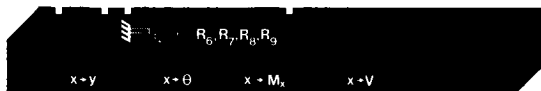
1.250 00 *** (K)

10.00 03 *** (P_{max})

2.000 03 *** (P_{min})

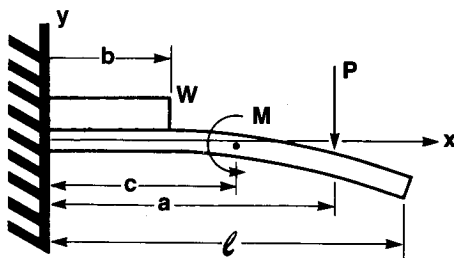
1.750 00 *** (FS)

CANTILEVER BEAMS



This program calculates deflection, slope, moment and shear at any specified point along a rigidly fixed, cantilever beam of uniform cross section. Distributed loads, point loads, applied moments or combinations of all three may be modeled. By using the principle of superposition, complicated beams with multiple point loads, applied moments and combined distributed loads may be analyzed.

Equations:



$$y = y_1 + y_2 + y_3 \quad (\text{total deflection})$$

$$y_1 = \frac{PX_1^2}{6EI} (X_1 - 3a) - \frac{Pa^2}{2EI} (x - a)(x > a)^* \quad (\text{deflection due to point load})$$

$$y_2 = \frac{-WX_2^2}{6EI} \left[X_2 \left(\frac{X_2}{4} - b \right) + 1.5 b^2 \right] - \frac{Wb^3}{6EI} (x - b)(x > b) \quad (\text{distributed load})$$

$$y_3 = \frac{MX_3^2}{2EI} + \frac{Mc}{EI} (x - c)(x > c) \quad (\text{applied moment})$$

$$\theta = \theta_1 + \theta_2 + \theta_3 \quad (\text{total slope})$$

$$\theta_1 = \frac{PX_1}{2EI} (X_1 - 2a) \quad (\text{slope due to point load})$$

$$\theta_2 = \frac{WX_2}{EI} \left[X_2 \left(\frac{X_2}{6} - \frac{b}{2} \right) + \frac{b^2}{2} \right] \quad (\text{distributed load})$$

$$\theta_3 = \frac{MX_3}{EI} \quad (\text{applied moment})$$

$$M_x = M_{x1} + M_{x2} + M_{x3} \quad (\text{total moment})$$

$$M_{x1} = P(X_1 - a) \quad (\text{moment due to point load})$$

$$M_{x2} = -W (X_2 (X_2/2 - b) + b^2/2) \quad (\text{distributed load})$$

$$M_{x3} = M \quad (x \leq c) \quad (\text{applied moment})$$

$$V = V_1 + V_2 + V_3 \quad (\text{total shear})$$

$$V_1 = P \quad (x \leq a) \quad (\text{shear due to point load})$$

$$V_2 = W (b - X_2) \quad (\text{distributed load})$$

$$V_3 = 0 \quad (\text{applied moment})$$

where:

y is the deflection at a distance x from the wall;

θ is the slope (change in y per change in x) at x ;

M_x is the moment at x ;

V is the shear at x ;

I is the moment of inertia of the beam;

E is the modulus of elasticity of the beam;

ℓ is the length of the beam;

P is a concentrated load;

W is a uniformly distributed load with dimensions of force per unit length.

M is an applied moment;

a is the distance from the foundation to the point load;

b is the distance to the end of the distributed load;

c is the distance to the applied moment;

$X_1 = x$ if $x \leq a$ or a if $x > a$;

$X_2 = x$ if $x \leq b$ or b if $x > b$

$X_3 = x$ if $x \leq c$ or c if $x > c$.

*The notation $(x > a)$ is interpreted as 1.00 if x is greater than a and as 0.00 if x is less than or equal to a .

Remarks:

Deflections must not significantly alter the geometry of the problem. Beams must be of constant cross section for deflection and slope equations to be valid. Stresses must be in the elastic region.

Registers R_{S0} – R_{S9} are available for user storage.

SIGN CONVENTIONS FOR BEAMS

NAME	VARIABLE	SENSE	SIGN
DEFLECTION	y		+
SLOPE	θ		+
INTERNAL MOMENT	M_x		+
SHEAR	V		+
EXTERNAL FORCE OR LOAD	P or W		+
EXTERNAL MOMENT	M		+

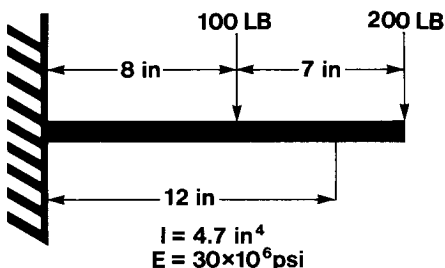
Sums of y , θ , M_x and V may be stored in R_6 , R_7 , R_8 , and R_9 , respectively. Note that these registers are indicated on the magnetic card.

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
1	Load side 1 and side 2.			
2	Initialize.			0.000 00
3	Input moment of inertia	I		I
	then modulus of elasticity	E		E
	then beam length.	l		EI
4	Input load(s):			
	Location of point load	a		a
	Point load	P		a
	Length of distributed load	b		b
	Distributed load (force/length)	W		b
	Location of applied moment	c		c
	Applied moment	M		c
5	Key in x to specify the point			
	of interest and calculate			
	deflection	x		y
	or slope	x		θ

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
	or moment	x	C	M_x
	or shear.	x	D	V
6	For a new calculation with the			
	same loading, go to step 5.			
	For new loads, go to step 4.			
	Be sure to set obsolete			
	loadings to zero. For new			
	beam properties, go to step 3.			
	To restart, go to step 2.			

Example 1:

What is the deflection at $x = 12$? Neglect the weight of the beam.

**Keystrokes:****Outputs:**

f A 4.7 ENTER+ 30 EEX

6 ENTER+ 15 f B → 141.0 06

Compute deflection at 12 inches due to 100 lb weight:

8 ENTER+ 100 f C 12 A → -211.8 -06

Store deflection due to 100 lb load for addition to deflection due to 200 lb load:

STO 9 → -211.8-06

Compute deflection at 12 inches due to 200 lb load:

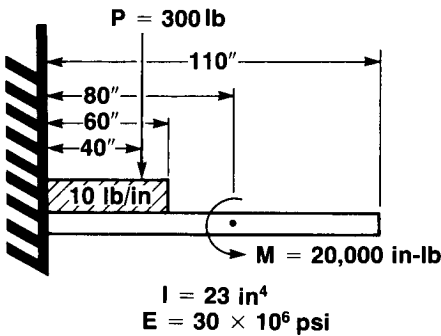
15 ENTER+ 200 f C 12 A → -1.123-03

Compute total deflection:

RCL 9 + → -1.335-03

Example 2:

For the beam below, compute deflection, slope, moment and shear at 0, 50, and 90 inches. Neglect the weight of the beam.



Keystrokes:

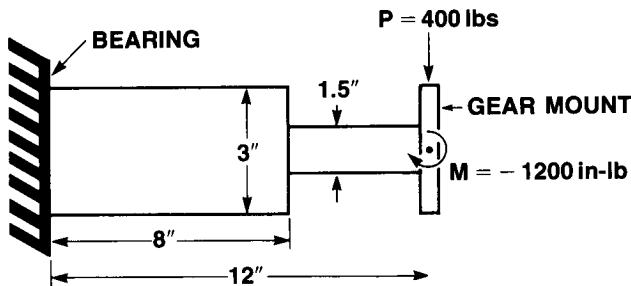
f A 23 ENTER 30 EEX
6 ENTER 110 f B 40 ENTER
300 f C 60 ENTER 10 f D
80 ENTER 20000 f E

Outputs:

0	A	→	0.000	00 (y)
0	B	→	0.000	00 (θ)
0	C	→	-10.00	03 (M_x)
0	D	→	900.00	00 (V)
50	A	→	5.211	-03
50	B	→	582.1	-06
50	C	→	19.50	03
50	D	→	100.0	00
90	A	→	50.14	-03
90	B	→	1.449	-03
90	C	→	0.000	00
90	D	→	0.000	00

Example 3:

The axle for a gear has the cross sectional shape and properties below. Assuming that the shaft may be modeled as a cantilever, calculate the deflection and slope at the gear mount and the moment and shear at the bearing. Neglect the weight of the axle.



$$E = 30 \times 10^6 \text{ psi}$$

$$I_{0-8} = 3.98 \text{ in}^4$$

$$I_{8-12} = 0.25 \text{ in}^4$$

Keystrokes:

Outputs:

First compute the deflection and slope from 0 to 8 inches based on larger cross section.

f A 3.98 ENTER 30 EEX

6 ENTER 12 f B 12 ENTER

400 f C 12 ENTER 1200

CHS f E 8 A STO 6 → -1.322 -03 (y_8)

8 B STO 7 → -294.8 -06 (θ_8)

Compute the deflection at 12 inches assuming no bending occurs from 8 to 12 inches.

4 x RCL 6 + STO 6 → -2.501 -03 (y_{12})

Compute the moment and shear at the bearing.

0 C → -6.000 03 (M_0)

0 D → 400.0 00 (V_0)

Change to smaller cross section and move origin to shoulder between large and small members.

.25 ENTER 30 EEX 6 ENTER

4 f B → 7.500 06

Add deflection and slope at 12 inches based on smaller cross section to values previously stored for large cross section.

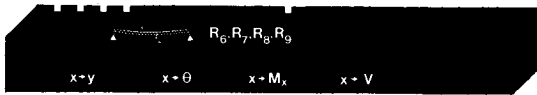
4 A → -5.831 -03

STO + 6 RCL 6 → -8.333 -03 (y_{12})

4 B → -2.773 -03

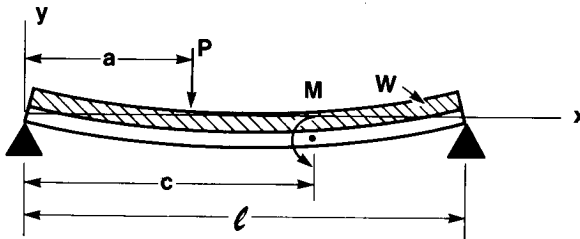
STO + 7 RCL 7 → -3.068 -03 (θ_{12})

SIMPLY SUPPORTED BEAMS



This program calculates deflection, slope, moment and shear at any specified point along a simply supported beam of uniform cross section. Distributed loads, point loads, applied moments or combinations of all three may be modeled. By using the principle of superposition, complicated beams with multiple point loads, and multiple applied moments can be analyzed.

Equations:



$$y = y_1 + y_2 + y_3 \quad (\text{total deflection})$$

$$y_1 = \frac{P(\ell - a)x}{6EI\ell} [x^2 + (\ell - a)^2 - \ell^2]^* \quad (\text{deflection due to point load})$$

$$y_2 = \frac{-Wx}{24EI} [\ell^3 + x^2(x - 2\ell)] \quad (\text{distributed load})$$

$$y_3 = \frac{-Mx}{EI} \left[c - \frac{x^2}{6\ell} - \frac{\ell}{3} - \frac{c^2}{2\ell} \right]^{**} \quad (\text{applied moment})$$

$$\theta = \theta_1 + \theta_2 + \theta_3 \quad (\text{total slope})$$

$$\theta_1 = \frac{P(\ell - a)}{6EI} [3x^2 + (\ell - a)^2 - \ell^2]^* \quad (\text{slope due to point load})$$

$$\theta_2 = -\frac{W}{24EI} [\ell^3 + x^2(4x - 6\ell)] \quad (\text{distributed load})$$

$$\theta_3 = \frac{-M}{EI} \left[c - \frac{x^2}{2\ell} - \frac{\ell}{3} - \frac{c^2}{2\ell} \right]^{**} \quad (\text{applied moment})$$

$$M_x = M_{x1} + M_{x2} + M_{x3} \quad (\text{total moment})$$

$$M_{x1} = \frac{P(\ell - a)x}{\ell}^* \quad (\text{moment due to point load})$$

$$M_{x2} = -\frac{Wx}{2} [x - \ell] \quad (\text{distributed load})$$

$$M_{x3} = \frac{Mx}{\ell}^{**} \quad (\text{applied moment})$$

$$V = V_1 + V_2 + V_3 \quad (\text{total shear})$$

$$V_1 = \frac{P(\ell - a)}{\ell}^* \quad (\text{shear due to point load})$$

$$V_2 = W \left(\frac{\ell}{2} - x \right) \quad (\text{distributed load})$$

$$V_3 = \frac{M}{\ell} \quad (\text{applied moment})$$

where:

y is the deflection at a distance x from the left support;

θ is the slope (change in y per change in x) at x ;

M_x is the moment at x ;

V is the shear at x ;

I is the moment of inertia of the beam;

E is the modulus of elasticity of the beam;

ℓ is the length of the beam;

P is a concentrated load;

W is a uniformly distributed load with dimensions of force per unit length;

M is an applied moment;

a is the distance from the left support to the point load;

c is the distance to the applied moment.

*If x is greater than a , $(\ell - a)$ is replaced by $-a$ and x is replaced by $(x - \ell)$.

**If x is greater than c , x is replaced by $(x - \ell)$ and c is replaced by $(\ell - c)$.

Remarks:

Deflections must not significantly alter the geometry of the problem. Beams must be of constant cross section for deflection and slope equations to be valid. Stresses must be in the elastic region.

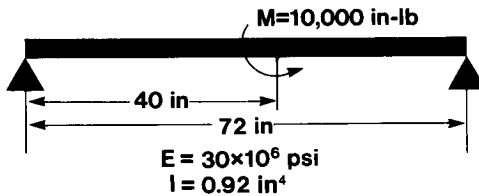
Registers R_{S0} – R_{S9} are available for user storage.

Sums of y , θ , M_x and V may be stored in R_6 , R_7 , R_8 , and R_9 , respectively. Note that these registers are indicated on the magnetic card.

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
1	Load side 1 and side 2.			
2	Initialize.		f A	0.000 00
3	Input moment of inertia	I	ENTER	I
	then modulus of elasticity	E	ENTER	E
	then beam length.	l	f B	EI
4	Input load(s):			
	Location of point load	a	ENTER	a
	Point load	P	f C	a
	Distributed load (force/length)	W	f D	W
	Location of applied moment	c	ENTER	c
	Applied moment	M	f E	c
5	Key in x to specify the point of interest and calculate			
	deflection	x	A	y
	or slope	x	B	θ
	or moment	x	C	M_x
	or shear.	x	D	V
6	For a new calculation with the same loading, go to step 5.			
	For new loads, go to step 4. Be sure to set obsolete loadings to zero. For new beam properties,			
	go to step 3. To restart, go to step 2.			

Example 1:

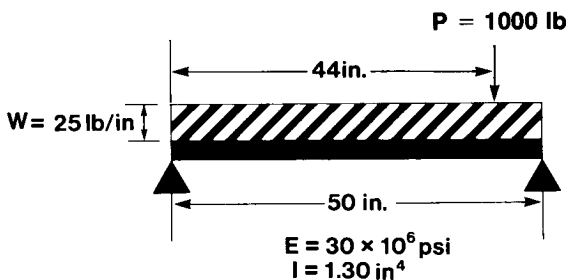
Find the deflection, slope, internal moment and shear at distances of 0, 24 and 60 inches for the beam below. Neglect the weight of the beam.

**Keystrokes:****Outputs:**

f A .92 ENTER 30 EEX			
6 ENTER 72 f B	27.60	06	
40 ENTER 10000 f E	40.00	00	
0 A	0.000	00	(y_0)
0 B	-1.771	-03	(θ_0)
0 C	0.000	00	(M_0)
0 D	138.9	00	(V_0)
24 A	-30.92	-03	(y_{24})
24 B	-322.1	-06	(θ_{24})
24 C	3.333	03	(M_{24})
24 D	138.9	00	(V_{24})
60 A	2.415	-03	(y_{60})
60 B	40.26	-06	(θ_{60})
60 C	-1.667	03	(M_{60})
60 D	138.9	00	(V_{60})

Example 2:

What is the slope of the beam below at $x = 38$ inches?



Keystrokes:

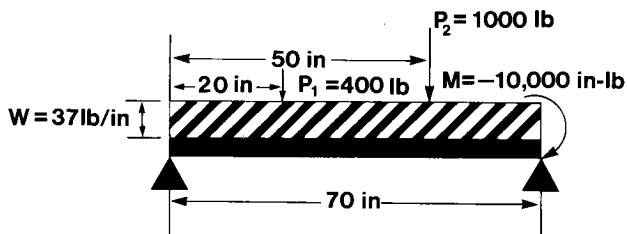
Outputs:

f A 1.30 ENTER 30 EEX	
6 ENTER 50 f B →	39.00 06
44 ENTER 1000 f C →	44.00 00
25 f D →	25.00 00
38 B →	3.327 -03 (in/in)

Example 3:

What is the total moment at the center of the beam below? (It is not necessary to know the values of E or I to solve the problem. Simply key in 70 and press

f **B**.)



First solve for the effect of the distributed load, P_1 , and M .

Keystrokes:

Outputs:

f A 70 f B 20 ENTER	
400 f C →	20.00 00
37 f D 70 ENTER	
10000 CHS f E →	70.00 00
70 ENTER 2 ÷ C →	21.66 03

Store values in R_6 .

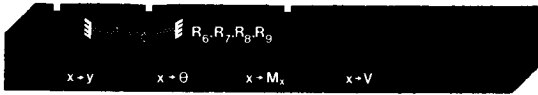
STO [6] →	21.66 03 (in-lb)
-------------------------	------------------

Now solve for the effect of P_2 and add it to the content of R_6 . This is the final answer assuming superposition is valid.

f A 50 ENTER 1000 f C →	50.00 00
35 C →	10.00 03 (in-lb)
RCL [6] + →	31.66 03 (in-lb)

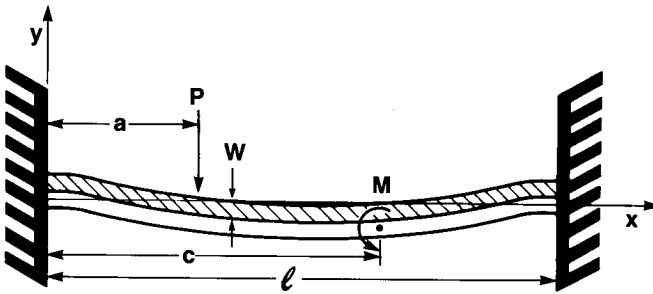
Notes

BEAMS FIXED AT BOTH ENDS



This program calculates deflection, slope, moment and shear at any specified point along a beam of uniform cross section, fixed at both ends. Distributed loads, point loads, applied moments or combinations of all three may be modeled. By using the principle of superposition, complicated beams with multiple point loads, and multiple applied moments can be analyzed.

Equations:



$$y = y_1 + y_2 + y_3 \quad (\text{total deflection})$$

$$y_1 = \frac{P(\ell - a)^2 x^2}{6EI\ell^3} [x(\ell + 2a) - 3a\ell]^* \quad (\text{deflection due to point load})$$

$$y_2 = \frac{Wx^2}{24EI} [x(2\ell - x) - \ell^2] \quad (\text{distributed load})$$

$$y_3 = \frac{M(\ell - c)x^2}{\ell^2 EI} \left[\frac{cx}{\ell} + \frac{\ell - 3c}{2} \right]^{**} \quad (\text{applied moment})$$

$$\theta = \theta_1 + \theta_2 + \theta_3 \quad (\text{total slope})$$

$$\theta_1 = \frac{P(\ell - a)^2 x}{2EI\ell^3} [x(\ell + 2a) - 2a\ell]^* \quad (\text{slope due to point load})$$

$$\theta_2 = \frac{Wx}{12EI} [x(3\ell - 2x) - \ell^2] \quad (\text{distributed load})$$

$$\theta_3 = \frac{M(\ell - c)x}{\ell^2 EI} \left[\frac{3cx}{\ell} + \ell - 3c \right]^{**} \quad (\text{applied moment})$$

$$M_x = M_{x1} + M_{x2} + M_{x3} \quad (\text{total moment})$$

$$M_{x1} = \frac{P(\ell - a)^2}{\ell^3} [x(\ell + 2a) - a\ell]^* \quad (\text{moment due to point load})$$

$$M_{x2} = \frac{W}{12} [6x(\ell - x) - \ell^2] \quad (\text{distributed load})$$

$$M_{x3} = \frac{M(\ell - c)}{\ell^2} \left[\frac{6cx}{\ell} + \ell - 3c \right]** \quad (\text{applied moment})$$

$$V = V_1 + V_2 + V_3 \quad (\text{total shear})$$

$$V_1 = \frac{P(\ell - a)^2}{\ell^3} (\ell + 2a) \quad (\text{shear due to point load})$$

$$V_2 = \frac{-W}{2} (2x - \ell) \quad (\text{distributed load})$$

$$V_3 = \frac{-6M(\ell - c)c}{\ell^3} \quad (\text{applied moment})$$

where:

y is the deflection at a distance x from the left support;

θ is the slope (change in y per change in x) at x ;

M_x is the moment at x ;

V is the shear at x ;

I is the moment of inertia of the beam;

E is the modulus of elasticity of the beam;

ℓ is the length of the beam;

P is a concentrated load;

W is a uniformly distributed load with dimensions of force per unit length;

M is an applied moment;

a is the distance from the left support to the point load;

c is the distance to the applied moment.

*If x is greater than a , a is replaced by $(\ell - a)$ and x is replaced by $(\ell - x)$. The signs of θ_1 and V_1 are also changed.

**If x is greater than c , x is replaced by $(\ell - x)$ and c is replaced by $(\ell - c)$. The signs of y_3 and M_{x3} are also changed.

Remarks:

This card differs from other beam cards. The “start” function is not included on **LBL** **f** **A**. You must manually perform the “start” function by storing zero when P, W or M are not included in the problem.

Deflections must not significantly alter the geometry of the problem. Beams must be of constant cross section for deflection and slope equations to be valid. Stresses must be in the elastic region.

Registers R_{S0} – R_{S9} are available for user storage.

Sums of y , θ , M_x and V may be stored in R_6 , R_7 , R_8 , R_9 , respectively. Note that these registers are indicated on the magnetic card.

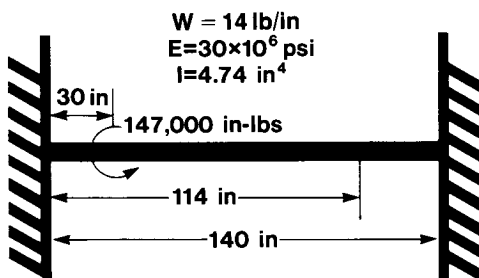
STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
1	Load side 1 and side 2.			
2	Input moment of inertia	I	ENTER +	I
	then modulus of elasticity	E	ENTER +	E
	then beam length.	l	f B	EI
3	Input load(s):*			
	Location of point load	a	ENTER +	a
	Point load	P	f C	a
	Distributed load (force/length)	W	f D	W
	Location of applied moment	c	ENTER +	c
	Applied moment	M	f E	c
4	Key in x to specify the point			
	of interest and calculate			
	deflection	x	A	y
	or slope	x	B	θ
	or moment	x	C	M_x
	or shear.	x	D	V



STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
5	For a new calculation with the			
	same loading, go to step 4. For			
	new loads, go to step 3. Be			
	sure to set obsolete loadings to			
	zero. For new beam properties,			
	go to step 2.			
	*Loads must be input, even if			
	zero.			

Example 1:

For the beam below, what are the values of deflection, slope, moment, and shear at an x of 114 inches?

**Keystrokes:**

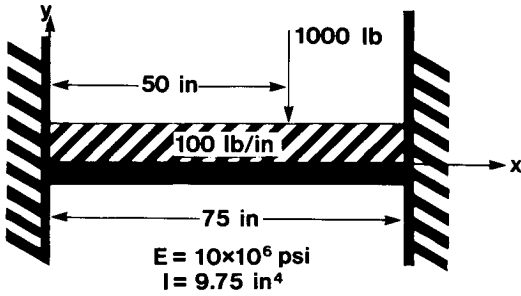
4.74 **ENTER** 30 **EEX** 6 **ENTER**
 140 **f B** $\longrightarrow$
 0 **f C** 30 **ENTER** 147000 **f E**
 14 **f D** $\longrightarrow$
 114 **A** $\longrightarrow$
RCL **O B** $\longrightarrow$
RCL **O C** $\longrightarrow$
RCL **O D** $\longrightarrow$

Outputs:

142.2 06
 14.00 00
 43.72 -03 (y)
 -3.155-03 (θ)
 13.05 03 (M_x)
 444.7 00 (V)

Example 2:

Find the internal moment at $x = 0$ for the configuration below.



Keystrokes:

9.75 **ENTER** 10 **EEX** 6 **ENTER**
75 **f B** →
0 **f E** 100 **f D** 50 **ENTER**
1000 **f C** →
0 **C** →

Also, find the deflection at $x = 40$.

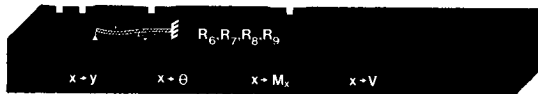
40 **A** →

Outputs:

97.50 06
50.00 00
-52.43 03 (M_0)
-101.0 -03 (Y_{40})

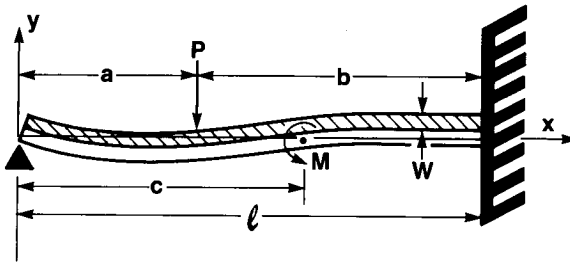
Notes

PROPPED CANTILEVER BEAMS



This program calculates deflection, slope, moment and shear at any specified point along a propped cantilever beam of uniform cross section. Distributed loads, point loads, applied moments or combinations of all three may be modeled. By using the principle of superposition, complicated beams with multiple point loads, and multiple applied moments can be analyzed.

Equations:



$$y = y_1 + y_2 + y_3 \quad (\text{total deflection})$$

$$y_1 = \frac{P}{6EI} [F(x^3 - 3\ell^2 x) + 3b^2 x]; \quad x \leq a \quad (\text{deflection due to point load})$$

$$y_2 = \frac{W}{48EI} (3\ell x^3 - 2x^4 - \ell^3 x) \quad (\text{distributed load})$$

$$y_3 = \frac{M}{EI} G(x^3 - 3\ell^2 x) + \ell x - cx; \quad x \leq c \quad (\text{applied moment})$$

$$y_3 = \frac{M}{EI} G(x^3 - 3\ell^2 x) + \ell x - \frac{1}{2} (x^2 + c^2); \quad x > c$$

$$\theta = \theta_1 + \theta_2 + \theta_3 \quad (\text{total slope})$$

$$\theta_1 = \frac{P}{6EI} [F(3x^2 - 3\ell^2) + 3b^2]; \quad x \leq a \quad (\text{slope due to point load})$$

$$\theta_1 = \frac{P}{6EI} [F(3x^2 - 3\ell^2) - 3(x - a)^2]; \quad x > a$$

$$\theta_2 = \frac{W}{48EI} (9x^2 - 8x^3 - \ell^3) \quad (\text{distributed load})$$

$$\theta_3 = \frac{M}{EI} [G(3x^2 - 3\ell^2) + \ell - c]; \quad x \leq c \quad (\text{applied moment})$$

$$\theta_3 = \frac{M}{EI} [G(3x^2 - 3\ell^2) + \ell - x]; \quad x > c$$

$$M_x = M_{x1} + M_{x2} + M_{x3} \quad (\text{total moment})$$

$$M_{x1} = PFx; \quad x \leq a \quad (\text{moment due to point load})$$

$$M_{x1} = PFx - P(x - b); \quad x > a$$

$$M_{x2} = W (3/8x \ell - x^2/2) \quad (\text{distributed load})$$

$$M_{x3} = 6MGx; \quad x \leq c \quad (\text{applied moment})$$

$$M_{x3} = 6MGx - M; \quad x > c$$

$$V = V_1 + V_2 + V_3 \quad (\text{total shear})$$

$$V_1 = PF; \quad x \leq a \quad (\text{shear due to point load})$$

$$V_1 = PF - P; \quad x > a$$

$$V_2 = W \left(\frac{3}{8} \ell - x \right) \quad (\text{distributed load})$$

$$V_3 = 6MG \quad (\text{applied moment})$$

$$F = \left[\frac{3b^2 \ell - b^3}{2\ell^3} \right]$$

$$b = (\ell - a)$$

$$G = \frac{\ell^2 - c^2}{4\ell^3}$$

where:

y is the deflection at a distance x from the left support;

θ is the slope (change in y per change in x) at x ;

M_x is the moment at x ;

V is the shear at x ;

I is the moment of inertia of the beam;

E is the modulus of elasticity of the beam;

l is the length of the beam;

P is a concentrated load;

W is a uniformly distributed load with dimensions of force per unit length;

M is an applied moment;

a is the distance from the left support to the point load;

c is the distance to the applied moment.

Remarks;

Deflections must not significantly alter the geometry of the problem. Beams must be of constant cross section for deflection and slope equations to be valid. Stresses must be in the elastic region.

Registers R_{S0} – R_{S9} and R_B are available for user storage.

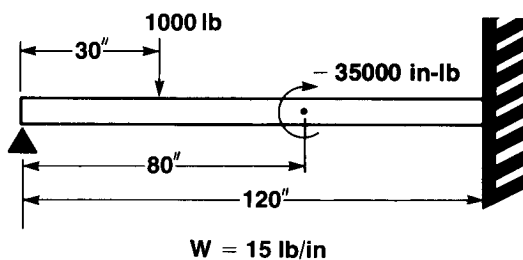
Sums of y , θ , M_x and V may be stored in R_6 , R_7 , R_8 and R_9 , respectively. Note that those registers are indicated on the magnetic card.

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
1	Load side 1 and side 2.			
2	Initialize.		f A	0.000 00
3	Input moment of inertia	I	ENTER	I
	then modulus of elasticity	E	ENTER	E
	then beam length.	l	f B	EI
4	Input load(s):			
	Location of point load	a	ENTER	a
	Point load	P	f C	a
	Distributed load (force/length)	W	f D	W
	Location of applied moment	c	ENTER	c
	Applied moment.	M	f E	c

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
5	Key in x to specify the point of interest and calculate			
	deflection	x	A	y
	or slope	x	B	θ
	or moment	x	C	M_x
	or shear	x	D	V
6	For a new calculation with the same loading, go to step 5.			
	For new loads, go to step 4.			
	Be sure to set obsolete loadings to zero. For new beam properties, go to step 3.			
	To restart, go to step 2.			

Example 1:

What are the values of moment and shear at both ends of the beam below? (It is not necessary to know the values of E or I since deflection and slope are not required.)



Keystrokes:

f A 120 **f B** 30 **ENTER+**

1000 **f C** →

80 **ENTER+** 35000 **CHS f E**

15 **f D** →

0 **C** →

0 **D** →

120 **C** →

120 **D** →

Outputs:

30.00 00

15.00 00

0.000 00 (in-lb)

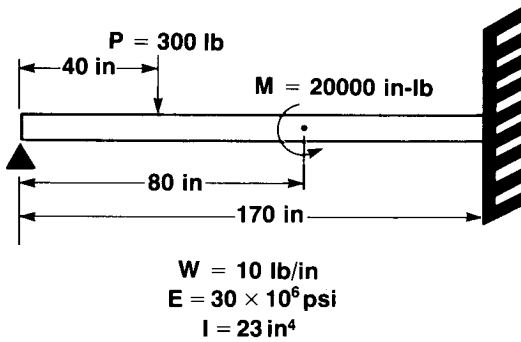
1.065 03 (lb)

-35.23 03 (in-lb)

-1.735 03 (lb)

Example 2:

Calculate the deflection, slope, moment and shear at $x = 90$ for the beam below.

**Keystrokes:**

f **A** 23 **ENTER** 30 **EEX** 6 **ENTER**

170 **f** **B** →

40 **ENTER** 300 **f** **C** 10 **f** **D**

80 **ENTER** 20000 **f** **E** →

90 **A** →

90 **B** →

90 **C** →

90 **D** →

Outputs:

690.0 06

80.00 00

-75.73 -03 (in)

920.8 -06 (in/in)

11.89 03 (in-lb)

-229.0 00 (lb)

Notes

HELICAL SPRING DESIGN



This program performs one or two point design for helical compression springs, of round wire, with ends square and ground.

After a tentative spring design has been found, a check can be run to determine whether stresses are acceptable, and whether sufficient clearance between coils is available at the point of highest operating load.

Equations:

$$k = \frac{P_2 - P_1}{L_1 - L_2}$$

$$s_2 = \frac{8 P_2 D_H}{\pi d^3}$$

$$D = D_{Hf_0} - d$$

$$N = \frac{Gd^4}{8 D^3 k}$$

$$L_s = (N + 2) d$$

$$L_f = \frac{P_1}{k} + L_1$$

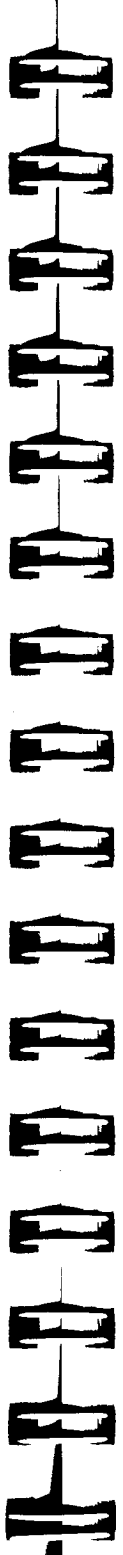
$$s_s = \frac{8 D k (L_f - L_s) W}{\pi d^3}$$

$$W = \frac{4 (D/d) - 1}{4 (D/d) - 4} + \frac{0.615}{(D/d)}$$

$$s_{\max} = \begin{cases} .45 \text{ TS for ferrous materials.} \\ .35 \text{ TS for non-ferrous materials.} \end{cases}$$

$$Y_S = \begin{cases} .65 \text{ TS for ferrous materials.} \\ .55 \text{ TS for non-ferrous materials.} \end{cases}$$

$$TS = \beta \ln d + \alpha$$



Design checking logic:

If $(L_2 - L_s) < 0.1 (L_f - L_2)$ and $s_s > s_{\max}$, the spring lacks sufficient clearance between coils and stresses are too high; code = 1.

If $(L_2 - L_s) < 0.1 (L_f - L_2)$ and $s_s \leq s_{\max}$, clearance between coils is insufficient; code = 2.

If $(L_2 - L_s) \geq 0.1 (L_f - L_2)$ and $s_s > YS$, stress is too high; code = 3.

If $(L_2 - L_s) \geq 0.1 (L_f - L_2)$ and $s_s \leq YS$, design is satisfactory. If $s_s \leq 0.3 TS$, stresses are quite conservative and code = 4. If $s_s > 0.3 TS$, design is acceptable and code = 5.

where:

G is the torsional modulus of rigidity;

α and β are tensile strength regression coefficients from table 1 (metric) or table 2 (English);

P_1 is the spring load at most extended operating point (see figure 1);

L_1 is spring length, at the most extended operating point;

P_2 is spring load at most compressed operating point;

L_2 is the spring length, at the most compressed operating point;

k is the spring constant;

d is the wire diameter;

f_0 is the clearance factor for the spring and the hole (possibly imaginary) in which the spring is designed to work:

$$f_0 = \begin{cases} 0.95 & \text{if } D_H \geq 12.70 \text{ mm (0.5 in)} \\ 0.90 & \text{if } D_H < 12.70 \text{ mm (0.5 in)} \end{cases}$$

D_H is the diameter of the hole (possibly imaginary) into which the spring must fit;

s_2 is the uncorrected stress at operating point 2;

N is the number of active coils;

s_s is the Wahl corrected stress when the spring is fully compressed to solid (coils touching);

L_f is the free length of the spring;

L_s is the fully compressed or solid spring length;

D is the mean spring diameter;
 OD is the outside spring diameter;
 Code is a digit from 1-5, explained in program User Instructions;
 W is the Wahl factor which corrects stresses for curvature;
 s_{max} is the maximum allowable working stress for the material;
 YS is the yield strength of the material;
 TS is the tensile strength of the material.

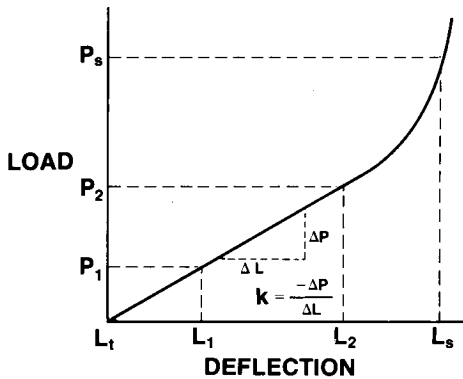


Figure 1-Spring Deflection

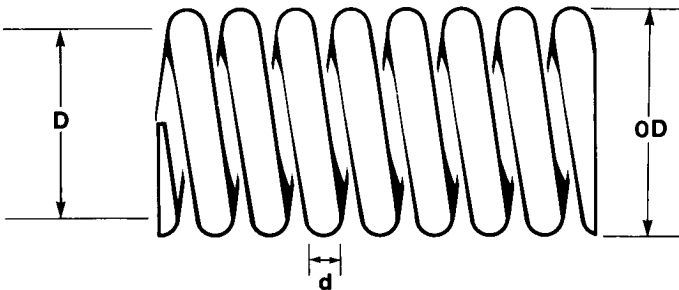


Figure 2-Helical Compression Spring

Table 1
MINIMUM TENSILE STRENGTH REGRESSION COEFFICIENTS
(Metric Units)

MATERIAL	MODULUS OF RIGIDITY G,N/(mm) ²	WIRE DIAMETER RANGE— MILLIMETERS	TENSILE STRENGTH COEF.	
			α ,N/(mm) ²	β ,N/(mm) ²
Music Wire ASTM-A228	7.93×10^4	0.41–6.35	2205	–346.1
Alloy Steel ASTM-A232	7.93×10^4	0.64–7.62	1921	–249.7
Stainless Steel ASTM-A313	6.90×10^4	0.41–1.91	1851	–209.6
		1.91–5.08	1950	–393.6
		5.08–9.40	2221	–560.4
Oil Tempered ASTM-A229	7.93×10^4	0.51–6.86	1827	–304.7
Hard Drawn ASTM-A227	7.93×10^4	0.51–3.56	1773	–283.4
		3.56–12.7	1757	–270.8
Tempered Valve Spring ASTM-A230	7.93×10^4	2.36–5.08	1586	–153.1
Phosphor Bronze ASTM-B159	4.07×10^4	0.64–9.40	957	– 63.97

Table 2
MINIMUM TENSILE STRENGTH REGRESSION COEFFICIENTS
(English Units)

MATERIAL	MODULUS OF RIGIDITY G,psi	WIRE DIAMETER RANGE— INCHES	TENSILE STRENGTH COEF.	
			α ,psi	β ,psi
Music Wire ASTM-A228	11.5×10^6	0.016–0.25	157400	–50200
Alloy Steel ASTM-A232	11.5×10^6	0.025–0.30	161400	–36220
Stainless Steel ASTM-A313	10.0×10^6	0.016–0.075	170200	–30400
		0.075–0.20	98110	–57090
		0.20–0.37	59190	–81280
Oil Tempered ASTM-A229	11.5×10^6	0.020–0.27	122100	–44190
Hard Drawn ASTM-A227	11.5×10^6	0.020–0.14	124200	–41110
		0.14–0.50	127800	–39280
Tempered Valve Spring ASTM-A230	11.5×10^6	0.093–0.20	158300	–22200
Phosphor Bronze ASTM-B159	5.9×10^6	0.025–0.37	108800	–9278

Reference:

Design Handbook—Springs, Custom Metal Parts, Associated Spring Corporation, Bristol, Connecticut, 1970.

Remarks:

Registers R_{s0} – R_{s9} are available for user storage.

The assumptions implicit to this program are based on engineering practice and experience. Generally, designs found by this program will be conservative, however, caution must be exercised when high or low temperatures, corrosive media or other adverse environmental circumstances exist.

For one point design, specify the free length (L_1) and a corresponding zero load (P_1), then specify the length (L_2) and corresponding load (P_2).

Some designs achieved by this program may require coiling the spring wire in such a small radius that the spring material would fail in the manufacturing process. No program check is made for this condition.

If code = 2, then s_2 has no intelligent meaning.

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
1	Load side 1 and side 2.			
2	Toggle ferrous (1) or non-ferrous (0) material mode (consider stainless steel non-ferrous).		[F] [A]	1.00/0.00
3	Specify material properties from table 1 (Metric) or table 2 (English):			
	Modulus of rigidity	G	[ENTER]	G
	Tensile strength Alpha	α	[ENTER]	α
	Tensile strength Beta	β	[F] [B]	G
4	Input load point 1:			
	Force 1	P_1	[ENTER]	P_1
	Corresponding spring length 1	L_1	[F] [C]	P_1
5	Input load Point 2 and calculate spring constant:			
	Force 2	P_2	[ENTER]	P_2
	Corresponding spring length 2	L_2	[F] [D]	k
6	Input wire diameter, and clearance factor ($f_0 = 0.90$ if spring diameter < 12.70mm (0.5 in); otherwise, $f = 0.95$), and maximum outside spring diameter.	d f_0 D_H	[ENTER] [ENTER] [F] [E]	d f_0 s_2

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
7	If s_2 is a reasonable value (not extremely high or low for your application), proceed to step 8. Otherwise, you may wish to modify the design specifica- tions in steps 4, 5 or 6.			
8	Compute number of coils.		A	N
9	Compute stress at solid (maximum).		B	S_s
10	Check design.		C	Code
11	If code = 1, the design is over constrained. The specified conditions cannot be met. Try another material, larger D_H , new load points or another type of spring.			
	If code = 2, clearance between coils is not sufficient. Press R+ to see current wire diameter.		R+	d
	Key in a smaller wire diameter and calculate a new N. Go back to instruction step 9.	d	R/S	N

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
	If code = 3, stress at solid			
	is too high. Press R+ to			
	see the current wire diameter.		R+	d
	Key in a larger wire dia-			
	meter and calculate a new N.	d	R/S	N
	Go back to instruction			
	step 9.			
	If code = 4, design is			
	acceptable but smaller wire			
	might also work. Press R+			
	to see current wire diameter.		R+	d
	Key in a new smaller wire			
	diameter and calculate N.	d	R/S	N
	Go back to instruction			
	step 9.			
	If code 5, design is			
	acceptable but not necessarily			
	optimal. Try manipulating			
	design parameters to obtain a			
	more economical design.			
12	Display free length, solid			
	length, mean diameter, and			
	outside diameter.		E	L, L _s , D, OD
13	Go to steps 2 through 6 for			
	a new case.			

Example 1:

Using Oil Tempered Wire (ASTM-A229), design a spring which supports a load of 270 newtons at a length of 62 millimeters and a load of 470 newtons at 50 millimeters. Wire is available in 0.5 mm increments. Try 4.0 mm wire first. Space available limits the spring diameter to 40.00 mm.

Variables:

$$P_1 = 270 \text{ N}$$
$$L_1 = 62 \text{ mm}$$
$$P_2 = 470 \text{ N}$$
$$L_2 = 50 \text{ mm}$$
$$d = 4.0 \text{ mm}$$
$$D_H = 40.0 \text{ mm}$$
$$f_0 = 0.95 \text{ (since } D_H > 12.70 \text{ mm)}$$
$$G = 7.93 \times 10^4 \text{ N/mm}^2$$
$$\alpha = 1827 \text{ N/mm}^2$$
$$\beta = -304.7$$

}

From table 1

Keystrokes:

Select iron wire (press **f A** until 1.00 is displayed.)

f A $\longrightarrow$

7.93 **EEX** 4 **ENTER** 1827 **ENTER**

304.7 **CHS** **f B** $\longrightarrow$

270 **ENTER** 62 **f C** 470 **ENTER**

50 **f D** $\longrightarrow$

4 **ENTER** .95 **ENTER** 40 **f E** $\longrightarrow$

A $\longrightarrow$

B $\longrightarrow$

C $\longrightarrow$

Outputs:

1.00 00

79.30 03

16.67 00 *** (k)

748.0 00 *** (N/mm², s₂)

3.874 00 *** (Coils)

1.446 03 *** (N/mm², s_s)

3.000 00 (Code)

Since Code = 3, select a larger wire. 4.5 mm wire is the next largest, so give it a try.

4.5 **R/S** $\longrightarrow$

B $\longrightarrow$

C $\longrightarrow$

6.487 00 *** (Coils)

748.4 00 *** (s_s)

5.000 00 (Code)

Since code = 5, design is acceptable. Output free length, solid length, mean diameter and outside diameter.

E →	78.20	00 ***	(L_f)
	38.19	00 ***	(L_s)
	33.50	00 ***	(D)
	38.00	00 ***	(OD)

Example 2:

Using music wire (ASTM-A228), design a spring which will work in a 0.25 inch hole, for the loading below:

$P_1 = 1 \text{ lb}$	$L_1 = 1.5 \text{ in}$	
$P_2 = 10 \text{ lb}$	$L_2 = 1.0 \text{ in}$	
$G = 11.5 \times 10^6 \text{ psi}$	} From table 2	
$\alpha = 157.4 \times 10^3 \text{ psi}$		
$\beta = -50.20 \times 10^3 \text{ psi}$		
$d = 0.035 \text{ or } 0.040$		
$f_0 = 0.90 \text{ (from User Instructions)}$		

Keystrokes:

Outputs:

Since music wire is a ferrous material, press **f A** until 1.00 is displayed.

f A →	1.000	00	
11.5 EE 6 ENTER 157.4 EE			
3 ENTER 50.20 CHS EE			
3 f B →	11.50	06	
1 ENTER 1.5 f C 10 ENTER			
1.0 f D →	18.00	00 ***	(k)
.035 ENTER .9 ENTER			
.25 f E →	148.5	03 ***	(s_2 , psi)
A →	17.47	00 ***	(Coils)
B →	227.7	03 ***	(s_s , psi)
C →	3.000	00	(Code)

Try the larger wire.

.04 R/S →	32.29	00 ***	(Coils)
B →	32.66	03 ***	(s_s , psi)
C →	2.000	00	(Code)

Since neither available wire will meet these specifications the specifications must be modified. After due consideration, it is decided that P_2 could be lowered to 9 pounds.

9	ENTER	1	f	D	→	16.00	00	***	(k)
.04	ENTER	.9	ENTER						
.25	f	E	→			89.52	03	***	(s ₂ , psi)
A	→					36.33	00	***	(Coils)
B	→					4.651	03	***	(s _s , psi)

Interestingly, and unfortunately, $s_s < s_2$ indicates that this spring cannot be compressed to s_2 .

C	→					2.000	00		
---	---	--	--	--	--	-------	----	--	--

Sure enough, insufficient clearance. Try the smaller wire.

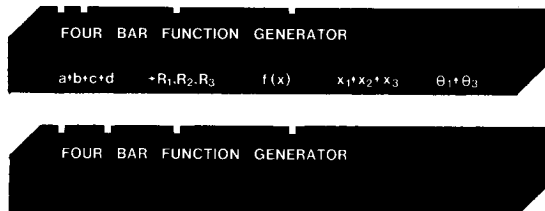
.035	R/S	→				21.29	00	***	(Coils)
B	→					169.6	03	***	(s _s , psi)
C	→					5.000	00		(Code)

Since the design checks out, calculate the dimensions:

E	→					1.563	00	***	(L _f)
						815.3	-03	***	(L _s)
						185.0	-03	***	(D)
						220.0	-03	***	(OD)

Notes

FOUR BAR FUNCTION GENERATOR



These cards may be used to design a four bar linkage which will approximate an arbitrary function of one variable. Freudenstein's approach is used in the solution. Cramer's rule is used to solve the 3×3 system of linear equations.

Equations:

Three precision points are used in the solution.

Freudenstein's equations

$$R_1 \cos \theta_1 - R_2 \cos \phi_1 + R_3 = \cos (\theta_1 - \phi_1)$$

$$R_1 \cos \theta_2 - R_2 \cos \phi_2 + R_3 = \cos (\theta_2 - \phi_2)$$

$$R_1 \cos \theta_3 - R_2 \cos \phi_3 + R_3 = \cos (\theta_3 - \phi_3)$$

are solved simultaneously for R_1 , R_2 and R_3 which are defined as follows:

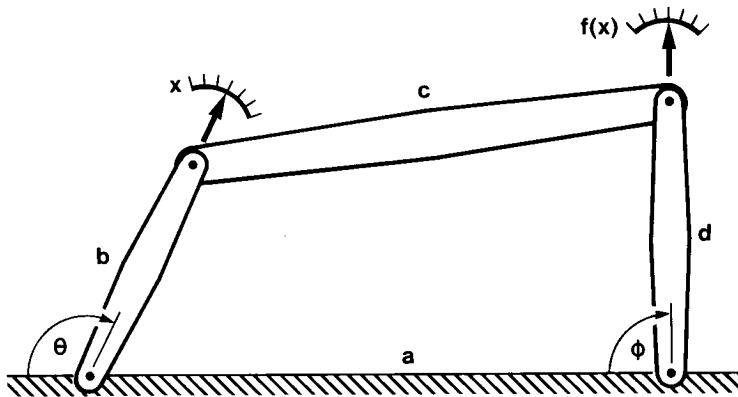
$$R_1 = a/d, \quad R_2 = a/b, \quad R_3 = \frac{a^2 + b^2 + d^2 - c^2}{2bd}$$

where a is the distance between fixed pivots, b is the length of the input link, c is the length of the coupler and d is the length of the output link. θ_1 refers to the angle of the input link at the first precision point, θ_2 the angle at the second point, and θ_3 the angle at the third. ϕ_1 is the angle of the output link at the first precision point, ϕ_2 is the angle at the second point, and ϕ_3 is the angle at the third precision point.

$$\theta_2 = \theta_1 + \frac{x_2 - x_1}{x_3 - x_1} (\theta_3 - \theta_1)$$

$$\phi_2 = \phi_1 + \frac{f(x_2) - f(x_1)}{f(x_3) - f(x_1)} (\phi_3 - \phi_1)$$

x_1 , x_2 and x_3 are the precision points or the three points at which the mechanism will yield kinematically exact solutions to the function ($f(x)$) which is to be generated.

**Reference:**

Martin, G. H., *Kinematics and Dynamics of Machines* McGraw-Hill, 1969.

Remarks:

$f(x)$ must be stated in 119 or less steps.

$$\left(\cos \phi_2 - \frac{\cos \phi_1 \cos \theta_2}{\cos \theta_1} \right) \left(\frac{\cos \theta_3}{\cos \theta_1} - 1 \right) \\ \neq \left(\frac{\cos \theta_2}{\cos \theta_1} - 1 \right) \left(\cos \phi_3 - \frac{\cos \phi_1 \cos \theta_3}{\cos \theta_1} \right)$$

θ_1 may not be equal to 90° or 270° .

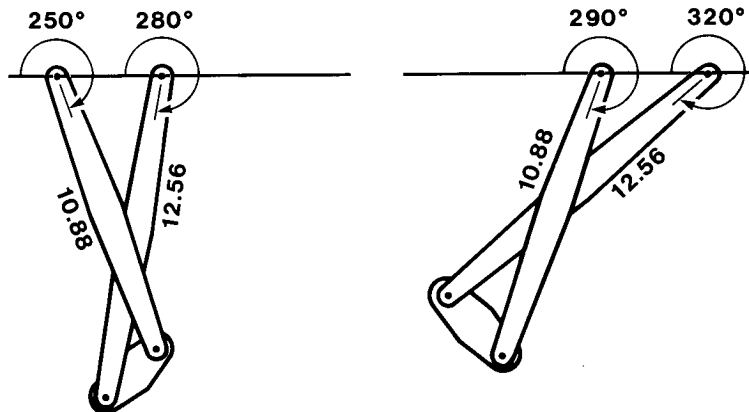
All registers are used.

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
1	Load side 1 and side 2 of card 1.			
2	To calculate link ratios, go to step 4.			
3	For function generator, go to step 7.			
4	Input the link lengths.	a	ENTER	a
		b	ENTER	b
		c	ENTER	c
		d	A	a
5	Calculate the link ratios.		B	R_1, R_2, R_3
6	For a new case, go to step 2.			
7	Key the function into memory:			
	i. Go to label C.		GTO C	
	ii. Switch to PRGM mode.			
	iii. Key in the function.*	f(x)		
	iv. Switch to RUN mode.			
	(The argument of the function is in X when the routine is called.)			
8	Input 3 precision points	x_1	ENTER	x_1
		x_2	ENTER	x_2
		x_3	D	x_1
9	Input starting input angle and final input angle ($\theta_1 \neq 90 \neq 270$)	θ_1	ENTER	θ_1
		θ_3	E	θ_2
10	Input starting output angle and final output angle.	ϕ_1	ENTER	ϕ_1
		ϕ_3	f A	ϕ_2
11	Load side 1 and side 2 of card 2.			

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
12	Calculate R_1 , R_2 and R_3 .		f B	R_1 , R_2 , R_3
13	Input a to calculate b, c, and d.	a	f C	b, c, d
14	For a new case, go to step 1.			
	*119 steps are allowed.			

Example 1:

Suppose the output of a linkage is to be the square root of the input. The input link is to move from 70° to 110° while the output moves from 100° to 140° . Precision points are $x_1 = 3(70^\circ)$, $x_2 = 5$, and $x_3 = 9(110^\circ)$. The distance between foundation pivots is 3.75. What are the remaining link lengths?



Data for input:

$$f(x) = \sqrt{x}$$

$$x_1 = 3, x_2 = 5, x_3 = 9$$

$$\theta_1 = 70^\circ, \theta_3 = 110^\circ, \phi_1 = 100^\circ, \phi_3 = 140^\circ$$

$$a = 3.75$$

Keystrokes:

Load side 1 and side 2 of Card 1.

GTO **C**

Switch to PRGM mode.

√x

Switch to RUN mode.

3 **ENTER** 5 **ENTER** 9 **D** 70 **ENTER**

110 **E** →

100 **ENTER** 140 **f** **A** →

Load side 1 and side 2 of card 2.

f **B** →

3.75 **f** **C** →

Outputs:

83.33 (θ_2)

115.90 (ϕ_2)

-0.30 *** (R_1)

-0.34 *** (R_2)

1.03 *** (R_3)

-10.88 *** (b)

3.04 *** (c)

-12.56 *** (d)

Note that should you decide to run the program "PROGRESSION OF FOUR BAR SYSTEM" for the same linkage, then input of a, b, c and d is not necessary since a, b, c and d are already stored in the corresponding registers from this program.

b = -10.88, c = 3.04, d = -12.56 (The negative signs indicate that the links are opposite to the assumed direction i.e., $\theta = 250^\circ$ and $\phi = 280^\circ$).

Example 2:

Compute the link ratios for the following link lengths:

a = 1.0

b = 1.371

c = 2.12

d = 1.502

Keystrokes:

Load side 1 and side 2 of Card 1

DSP **4**

1 **ENTER** 1.371 **ENTER**

2.12 **ENTER** 1.502 **A** **B** →

Outputs:

0.6658 *** (R_1)

0.7294 *** (R_2)

0.1557 *** (R_3)

Notes

PROGRESSION OF FOUR BAR SYSTEM



This program calculates angular displacement, velocity and acceleration for the output link of a four bar system (figure 1). (Either the “connecting link” (c) or the “output link” (d) may be selected as the program’s output link.)

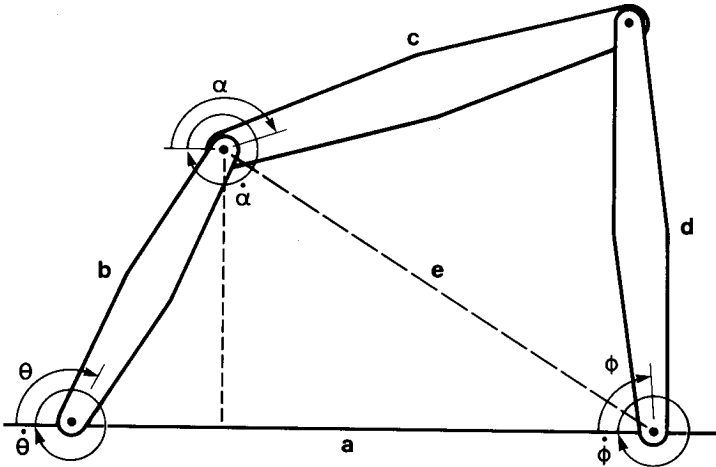


FIGURE 1-FOUR BAR SYSTEM SHOWING
POSITIVE ANGULAR CONVENTIONS

Automatic and manual modes of operation are available. In manual mode, the output angle is calculated by keying in the input angle and pressing **A**. The angular output velocity may then be found by keying in the angular input velocity and pressing **C**. After angular velocity is calculated, the output link acceleration is found by keying in the input link acceleration and pressing **E**. In automatic mode, a starting input link angle θ_0 , the number of increments n , the angular increment $\Delta\theta$, and the constant input link RPM are input using **fE**. The program automatically progresses from θ_0 through n increments of $\Delta\theta$. RPM is output once, followed by groups of four values. The first value, of these four-value groups, is input angle, the second value is output angle, the third value is angular output velocity and the fourth value is angular output acceleration. Example problem 1 demonstrates manual operation while example 2 demonstrates automatic operation.

Equations:

Output Link

$$\phi = \sin^{-1} \left(\frac{b}{e} \sin \theta \right) + \cos^{-1} \left(\frac{d^2 + e^2 - c^2}{2de} \right)$$

Connecting Link

$$\alpha = \sin^{-1} \left(\frac{b}{e} \sin \theta \right) + \cos^{-1} \left(\frac{c^2 + e^2 - d^2}{-2ce} \right)$$

where:

$$e = \sqrt{a^2 + b^2 + 2ab \cos \theta}$$

$$\frac{d\phi}{d\theta} = \frac{R_1 \sin \theta - \sin(\theta - \phi)}{R_2 \sin \phi - \sin(\theta - \phi)}$$

$$R_1 = \frac{a}{d} \quad R_2 = \frac{a}{b}$$

$$\frac{d\alpha}{d\theta} = \frac{S_1 \sin \theta - \sin(\theta - \alpha)}{S_2 \sin \alpha - \sin(\theta - \alpha)}$$

$$S_1 = -\frac{a}{c} \quad S_2 = \frac{a}{b}$$

$$\frac{d^2\phi}{d\theta^2} = \frac{R_1 \cos \theta - R_2 \cos \phi \left(\frac{d\phi}{d\theta} \right)^2 - \left(1 - \frac{d\phi}{d\theta} \right)^2 \cos(\theta - \phi)}{R_2 \sin \phi - \sin(\theta - \phi)}$$

$$\frac{d^2\alpha}{d\theta^2} = \frac{S_1 \cos \theta - S_2 \cos \alpha \left(\frac{d\alpha}{d\theta} \right)^2 - \left(1 - \frac{d\alpha}{d\theta} \right)^2 \cos(\theta - \alpha)}{S_2 \sin \alpha - \sin(\theta - \alpha)}$$

$$\dot{\phi} = \frac{d\phi}{d\theta} \dot{\theta} \quad \dot{\alpha} = \frac{d\alpha}{d\theta} \dot{\theta}$$

$$\ddot{\phi} = \frac{d^2\phi}{dt^2} = \frac{d^2\phi}{d\theta^2} \left(\frac{d\theta}{dt} \right)^2 + \frac{d^2\theta}{dt^2} \frac{d\phi}{d\theta}$$

$$= \dot{\theta}^2 \frac{d^2\phi}{d\theta^2} + \ddot{\theta} \frac{d\phi}{d\theta} \quad \alpha = \dot{\theta}^2 \frac{d^2\alpha}{d\theta^2} + \alpha \frac{d\ddot{\theta}}{d\theta}$$

Remarks:

$\dot{\phi}$ has the units of θ , since $\frac{d\phi}{d\theta}$ is dimensionless.

$\frac{d^2\phi}{d\theta^2}$ has units of rad^{-1} . So that the dimensions making up $\ddot{\phi}$ agree, the program assumes $\frac{d^2\theta}{dt^2}$ is given in RPM^2 , and $\frac{d^2\phi}{d\theta^2}$ is multiplied by $2\pi \frac{\text{rad}}{\text{rev}}$:

$$\ddot{\phi} \frac{\text{rev}}{\text{min}^2} = \ddot{\theta}^2 \frac{\text{rev}^2}{\text{min}^2} \frac{d^2\phi}{d\theta^2} \text{rad}^{-1} \left[\frac{2\pi \text{ rad}}{\text{rev}} \right] + \ddot{\theta} \frac{\text{rev}}{\text{min}^2} \frac{d\phi}{d\theta}$$

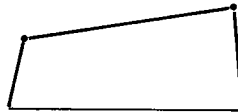
The program could be altered by the appropriate constant change if $\dot{\theta}$ and $\ddot{\theta}$ are in units other than revolutions/time (e.g. for degrees/ time change 2π to $\pi/180$ (radians/degree), or for radians/time, no constant necessary).

These same remarks apply to $\dot{\alpha}$ and $\ddot{\alpha}$.

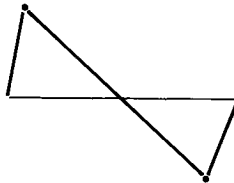
An error during calculation of ϕ or α may indicate the linkage may not physically assume the specified position.

The sign of RPM determines the direction of rotation in automatic mode.

Two possible configurations exist for a given set of links:



Configuration A



Configuration B

Configuration A is assumed by the program. To obtain configuration B change step 87 from + to -.

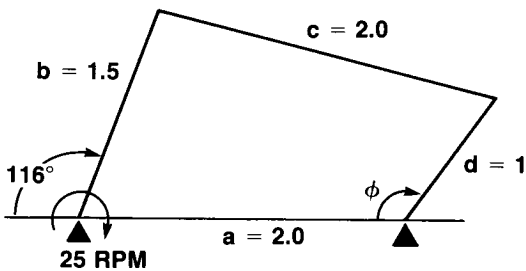
Registers R_{S0} – R_{S9} are available for user storage.

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
1	Load side 1 and side 2.			
2	Input link lengths:			
	fixed link	a	ENTER	a
	input link	b	ENTER	b
	connecting link	c	ENTER	c
	output link	d	f A	a
3	If connecting link output values (α , $\dot{\alpha}$, $\ddot{\alpha}$) are desired, rather than output link values (ϕ , $\dot{\phi}$, $\ddot{\phi}$), set connecting link mode by pressing f C. A 1.00 appears in the display indicating connecting link mode is on. Pressing f C repeatedly toggles connecting link mode off and on.		f C	1.00/0.00
4	For automatic progression of input link, go to step 9.			
5	Key in input link angle and calculate output angle.	θ	A	ϕ (α)
6	Key in input RPM and calculate output RPM.	$\dot{\theta}$ (RPM)	C	$\dot{\phi}$ ($\dot{\alpha}$)
7	Key in input link acceleration and calculate output acceleration.	$\ddot{\theta}$ (RPM ²)	E	$\ddot{\phi}$ ($\ddot{\alpha}$)
8	For a new input link angle, go to step 5. For the alternate output member (connector, or output link), go to step 3. For a new case, go to step 2.			

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
9	Key in starting input link angle	θ_0	ENTER	θ_0
	then number of increments	n	ENTER	n
	then angular increment	$\Delta\theta$	ENTER	$\Delta\theta$
	then RPM (+ or -) and			
	calculate the output $\theta(\alpha)$, $\dot{\phi}(\dot{\alpha})$,			
	and $\ddot{\phi}(\ddot{\alpha})$ for constant input			
	RPM between θ_0 and θ_f .	RPM	f E	output
10	For another set of inputs, go			
	to step 9. For the alternate			
	output member (connector or			
	output link) go to step 3. For a			
	new case go to step 2.			

Example 1:

The input link of the four bar linkage below is instantaneously rotating at 25 RPM with an angular acceleration of 2.3 RPM². The input link is at 116°. What are the values of position, velocity, and acceleration of link d? Link c?



Keystrokes:

2 **ENTER** 1.5 **ENTER** 2 **ENTER**
1 **f A**
116 **A**
25 **C**
2.3 **E**

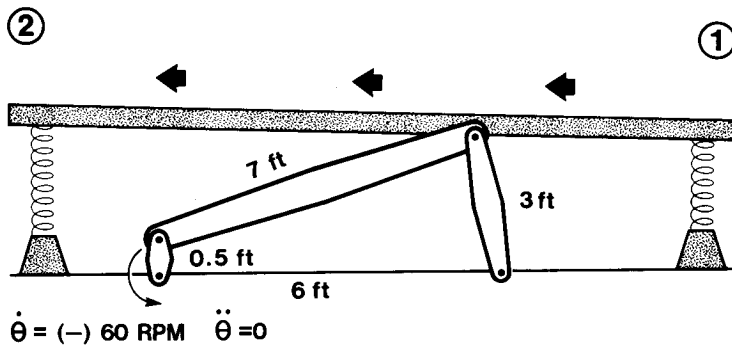
Outputs:

2.00
125.75 (ϕ)
39.29 ($\dot{\phi}$)
2279.89 ($\ddot{\phi}$)

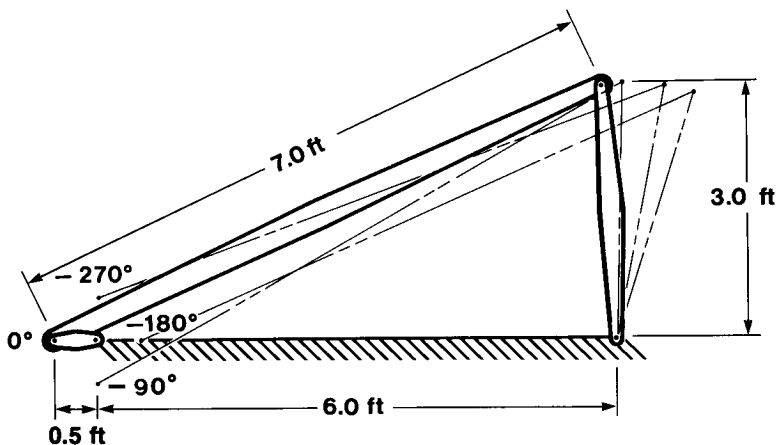
r C	→	1.00	(connecting link selected)
116 A	→	195.56	(α)
25 C	→	3.38	($\dot{\alpha}$)
2.3 E	→	2049.01	($\ddot{\alpha}$)

Example 2:

A four bar linkage is to be used to convert rotary motion from an electric motor to the reciprocating motion necessary to activate a shaking conveyor system which moves fruit between two process stations.



For the geometry shown above, what is the motion of the output link? Start at $\theta = 0^\circ$ and go to -330° by 12, 30° increments. Find the corresponding connecting link motion.

Four Bar Shaker Mechanism

Solution:

θ°	ϕ°	$\dot{\phi}(\text{RPM})$	$\ddot{\phi}(\text{RPM}^2)$	α°	$\alpha(\text{RPM})$	$\alpha(\text{RPM}^2)$
0	86.69	-4.62	3392.91	154.67	-4.62	-92.82
-30	85.63	0.46	3816.90	152.42	-4.20	713.38
-60	87.18	5.70	3615.33	150.67	-2.60	1594.02
-90	91.19	10.12	2592.67	150.01	0.10	2210.83
-120	96.94	12.38	449.28	150.84	3.19	2062.19
-150	102.95	10.93	-2597.20	153.04	5.34	887.00
-180	107.18	5.45	-4998.56	155.83	5.45	-693.75
-210	108.09	-1.86	-5112.85	158.18	3.73	-1628.64
-240	105.56	-7.86	-3351.37	159.45	1.32	-1738.45
-270	100.72	-10.95	-1099.60	159.53	-0.93	-1481.44
-300	95.11	-11.05	887.85	158.59	-2.75	-1133.46
-330	90.08	-8.70	2404.65	156.87	-4.04	-698.86

Keystrokes:

6 **ENTER** .5 **ENTER** 7 **ENTER**
3 **f** **A** →

Select output link.
f **C** →

0 **ENTER** 12 **ENTER** 30 **ENTER**
60 **CHS** **f** **E** →

Outputs:

6.00
0.00 (Press **f** **C** again if 1.00 is displayed)
-60.00 *** (RPM)
0.00 *** (θ_0)
86.69 *** (ϕ)
-4.62 *** ($\dot{\phi}$)
3392.91 *** ($\ddot{\phi}$)
-30.00 *** (θ_1)
85.63 *** (ϕ_1)
0.46 *** ($\dot{\phi}_1$)
3816.90 *** ($\ddot{\phi}_1$)
etc.
⋮
-330.00 *** (θ_f)
90.08 *** (ϕ_f)
-8.70 *** ($\dot{\phi}_f$)
2404.65 *** ($\ddot{\phi}_f$)

f C →
 0 ENTER 12 ENTER 30 ENTER
 60 CHS f E →

1.00
 -60.00 *** (RPM)
 0.00 *** (θ_0)
 154.67 *** (α_0)
 -4.62 *** ($\dot{\alpha}_0$)
 -92.82 *** ($\ddot{\alpha}_0$)
 -30.00 *** (θ_1)
 152.42 *** (α_1)
 -4.20 *** ($\dot{\alpha}_1$)
 713.38 *** ($\ddot{\alpha}_1$)
 etc.
 ⋮
 ⋮

PROGRESSION OF SLIDER CRANK

PROGRESSION OF SLIDER CRANK

$N \times E \times L \times R \times \omega$ $\theta \times x, \phi$ $v, \dot{\phi}$ $a, \ddot{\phi}$ $\theta_1, \theta_2, n, \dots$

In a slider crank mechanism (e.g., the piston, wrist pin and connecting rod in an internal combustion engine), for given crank radius, connecting rod length, slider offset, crankshaft speed (RPM) and crank position, this program calculates the following: the displacement, velocity, and acceleration of the slider; the connecting rod angle, velocity and acceleration; the maximum and minimum displacements, and the maximum and minimum angular values for ϕ .

Equations:

$$\omega = \frac{\pi N}{30}$$

$$x = R \cos \theta + L \cos \phi$$

$$x_{\max} = (R + L) \cos \left[\sin^{-1} \left(\frac{E}{R + L} \right) \right]$$

$$x_{\min} = (L - R) \cos \left[\sin^{-1} \left(\frac{E}{L - R} \right) \right]$$

$$\Delta x = x_{\max} - x_{\min}$$

$$\phi = \sin^{-1} \left(\frac{E + R \sin \theta}{L} \right)$$

$$v = \frac{dx}{dt} = R\omega \left(\frac{-\sin(\theta + \phi)}{\cos \phi} \right)$$

$$a = \frac{d^2x}{dt^2} = R\omega^2 \left(\frac{-\cos(\theta + \phi)}{\cos \phi} - \frac{R \cos^2 \theta}{L \cos^3 \phi} \right)$$

$$\phi_{\max} = \sin^{-1} \left(\frac{E + R}{L} \right)$$

$$\phi_{\min} = \sin^{-1} \left(\frac{E - R}{L} \right)$$

$$\Delta\phi = \phi_{\max} - \phi_{\min}$$

$$\dot{\phi} = \frac{d\phi}{dt} = \omega \frac{R \cos \theta}{L \cos \phi}$$

$$\ddot{\phi} = \frac{d^2\phi}{dt^2} = \omega^2 \left[\left(\frac{d\phi}{d\theta} \right)^2 \tan \phi - \frac{R \sin \theta}{L \cos \phi} \right]$$

where:

N is crankshaft speed in RPM;

E is slider offset;

L is connecting rod length;

R is crank radius;

ω is crank angular velocity in radians/sec;

θ is crank angle;

x is slider displacement;

$x_{\max}$ is maximum slider displacement;

$x_{\min}$ is minimum slider displacement;

Δx is stroke;

v is slider velocity;

a is slider acceleration;

ϕ is connecting rod angular displacement;

$\phi_{\max}$ is maximum connecting rod angular displacement;

$\phi_{\min}$ is minimum connecting rod angular displacement;

$\Delta\phi$ is total angular throw of connecting rod;

$\dot{\phi}$ is angular velocity of connecting rod;

$\ddot{\phi}$ is angular acceleration of connecting rod.

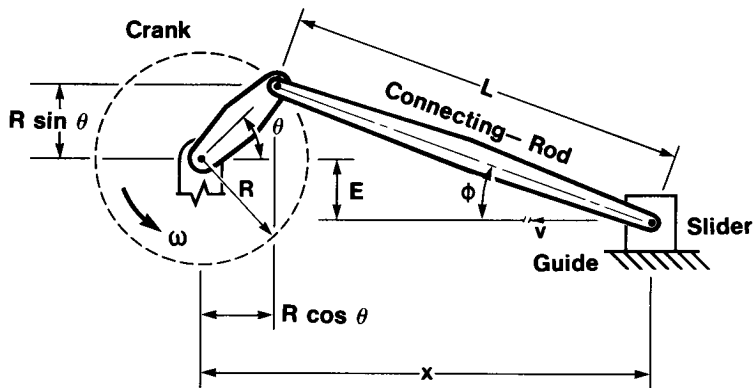
References:

H. A. Rothbart, *Mechanical Design and Systems Handbook*, McGraw-Hill, 1964.

V. M. Faires, *Kinematics*, McGraw-Hill, 1959.

Remarks:

Registers R_{S0} – R_{S9} are available for user storage.



STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
1	Load side 1 and side 2.			
2	Input the data for the mechanism.	N	ENTER	
		E	ENTER	
		L	ENTER	
		R	A	ω
3	Calculate maximum displacement and minimum displacement of slider.		f A	$x_{\max}$
				$x_{\min}$
4	Calculate maximum and minimum angular displacements for connecting rod.		f B	$\phi_{\max}$
				$\phi_{\min}$
5	Input crank angle to calculate slider displacement and connecting rod angle.	θ	B	x, ϕ
6	Calculate slider velocity and connecting rod angular velocity.		C	$v, \dot{\phi}$

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
7	Calculate slider acceleration and connecting rod angular acceleration.		D	$a, \ddot{\phi}$
8	Repeat steps 5-7 for a different θ .			
9	To calculate $x, \phi, v, \dot{\phi}, a, \text{ and } \ddot{\phi}$ for crank angles between θ_1 and θ_2 with n intervals.	θ_1	ENTER*	
		θ_2	ENTER*	
		n	E	$\theta, x, \phi, v, \dot{\phi}, a, \ddot{\phi}$
10	For a new mechanism, go to step 2.			

Example 1:

For an in-line slider crank mechanism ($E = 0$), turning at 4800 RPM having a crank radius of 2.0 inches and connecting rod length of 7.0 inches, Find:

- (1) $x_{\max}, x_{\min}$ and $\phi_{\max}, \phi_{\min}$
 - (2) $x, v,$ and a of the wrist pin in the slider
 - (3) $\phi, \dot{\phi},$ and $\ddot{\phi}$ of the connecting rod
- for $\theta = 0^\circ, 15^\circ, 45^\circ, 90^\circ, 135^\circ, 180^\circ, 225^\circ$.

θ°	$x(\text{in})$	ϕ°	$v(\text{in/sec})$	$\dot{\phi}(\text{rad/sec})$	$a(\text{in/sec}^2)$	$\ddot{\phi}(\text{rad/sec}^2)$
0	9.00	0.00	0.00	143.62	-649701.96	0.00
15	8.91	4.24	-332.20	139.10	-614226.44	-17300.41
45	8.27	11.66	-857.50	103.69	-360454.40	-49902.29
90	6.71	16.60	-1005.31	0.00	150658.43	-75329.22
135	5.44	11.66	-564.22	-103.69	354181.29	-49902.29
180	5.00	0.00	0.00	-143.62	360945.53	0.00
225	5.44	-11.66	564.22	-103.69	354181.29	49902.29

Keystrokes:

4800 **ENTER** 0 **ENTER**7 **ENTER** 2 **A** →**f** **A** →**f** **B** →0 **B** →**C** →**D** →15 **B** →**C** →**D** →45 **B** →**C** →**D** →

⋮

225 **B** →**C** →**D** →

Outputs:

502.65 *** (ω)9.00 *** ($x_{\max}$)5.00 *** ($x_{\min}$)16.60 *** ($\phi_{\max}$)-16.60 *** ($\phi_{\min}$)9.00 *** (x)0.00 *** (ϕ)0.00 *** (v)143.62 *** ($\dot{\phi}$)-649701.96 *** (a)0.00 *** ($\ddot{\phi}$)8.91 *** (x)4.24 *** (ϕ)-332.20 *** (v)139.10 *** ($\dot{\phi}$)-614226.44 *** (a)-17300.41 *** ($\ddot{\phi}$)8.27 *** (x)11.66 *** (ϕ)-857.50 *** (v)103.69 *** ($\dot{\phi}$)-360454.40 *** (a)-49902.29 *** ($\ddot{\phi}$)

5.44 ***

-11.66 ***

564.22 ***

-103.69 ***

354181.29 ***

49902.29 ***

Alternatively, the values may be generated automatically.

0 **ENTER** 225 **ENTER** 5 **E** $\longrightarrow$

0.00 ***	(θ)
9.00 ***	(x)
0.00 ***	(ϕ)
0.00 ***	(v)
143.62 ***	($\dot{\phi}$)
-649701.96 ***	(a)
0.00 ***	($\ddot{\phi}$)
45.00 ***	
8.27 ***	
11.66 ***	
-857.58 ***	
103.69 ***	
-360454.40 ***	
-49902.29 ***	
90.00 ***	
6.71 ***	
16.60 ***	
-1005.31 ***	
0.00 ***	
150658.43 ***	
-75329.22 ***	
:	
225.00 ***	
5.44 ***	
-11.66 ***	
564.22 ***	
-103.69 ***	
354181.29 ***	
49902.29 ***	

Example 2:

Determine the same values as in example 1 for a slider crank with offset of 1.5 inches (E = 1.5 inches).

Keystrokes:

4800 **ENTER** 1.5 **ENTER**
7 **ENTER** 2 **A** →
f **A** →
f **B** →
0 **B** →
C →
D →
15 **B** →
C →
D →
⋮
225 **B** →
C →
D →

Outputs:

502.65 *** (ω)
8.87 *** ($x_{\max}$)
4.77 *** ($x_{\min}$)
30.00 *** ($\phi_{\max}$)
-4.10 *** ($\phi_{\min}$)
8.84 *** (x)
12.37 *** (ϕ)
-220.55 *** (v)
147.03 *** ($\dot{\phi}$)
-660249.41 *** (a)
4742.62 *** ($\ddot{\phi}$)
8.63 *** (x)
16.75 *** (ϕ)
-552.49 *** (v)
144.87 *** ($\dot{\phi}$)
-602160.36 *** (a)
-13194.60 *** ($\ddot{\phi}$)
5.59 ***
0.70 ***
719.57 ***
-101.56 ***
280733.14 ***
51175.65 ***



θ°	x(in)	ϕ°	v(in/sec)	$\dot{\phi}$ (rad/sec)	a(in/sec ²)	$\ddot{\phi}$ (rad/sec ²)
0	8.84	12.37	-220.55	147.03	-660249.41	4742.62
15	8.63	16.75	-552.49	144.87	-602160.36	-13194.60
45	7.78	24.60	-1036.35	111.69	-289750.94	-50429.96
90	6.06	30.00	-1005.31	0.00	291748.80	-83356.80
135	4.95	24.60	-385.37	-111.69	424884.76	-50429.96
180	4.84	12.37	220.55	-147.03	350398.08	4742.62
225	5.59	0.70	719.57	-101.56	280733.14	51175.65

0 ENTER 360 ENTER 8 E →

0.00 *** (θ)

8.84 *** (x)

12.37 *** (ϕ)

-220.55 *** (v)

147.03 *** ($\dot{\phi}$)

-660249.41 *** (a)

4742.62 *** ($\ddot{\phi}$)

45.00 ***

7.78 ***

24.60 ***

-1036.35 ***

111.69 ***

-289750.94 ***

-50429.96 ***

⋮

360.00 ***

8.84 ***

12.37 ***

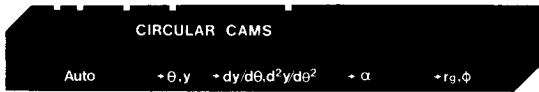
-220.55 ***

147.03 ***

-660249.41 ***

4742.62 ***

CIRCULAR CAMS



This program computes the parameters necessary for the design of a harmonic or cycloidal circular cam with a roller, point or flat follower.

Equations:

Harmonic cams:

$$y = \frac{h}{2} \left(1 - \cos \frac{180\theta}{\beta} \right)$$

$$\frac{dy}{d\theta} = \frac{\pi h}{2\beta} \sin \frac{180\theta}{\beta} \quad \left[\frac{dy}{dt} = \omega \frac{dy}{d\theta} \right]$$

$$\frac{d^2y}{d\theta^2} = \frac{\pi^2 h}{2\beta^2} \cos \frac{180\theta}{\beta} \quad \left[\frac{d^2y}{dt^2} = \omega^2 \frac{d^2y}{d\theta^2} \right]$$

Cycloidal cams:

$$y = h \left[\frac{\theta}{\beta} - \frac{1}{2\pi} \sin \frac{2\pi\theta}{\beta} \right]$$

$$\frac{dy}{d\theta} = \frac{h}{\beta} \left[1 - \cos \frac{2\pi\theta}{\beta} \right] \quad \left[\frac{dy}{dt} = \omega \frac{dy}{d\theta} \right]$$

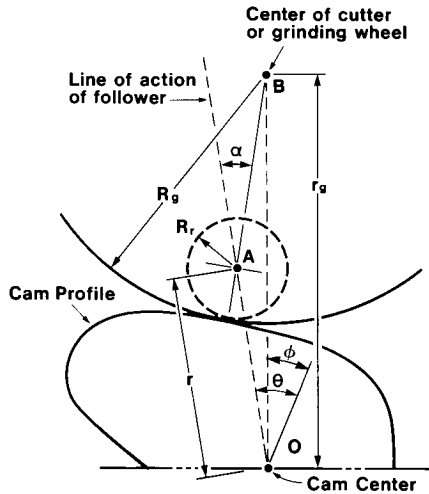
$$\frac{d^2y}{d\theta^2} = \frac{2\pi h}{\beta^2} \sin \frac{2\pi\theta}{\beta} \quad \left[\frac{d^2y}{dt^2} = \omega^2 \frac{d^2y}{d\theta^2} \right]$$

Both cycloidal and harmonic cams:

$$\alpha = \tan^{-1} \left(\frac{180}{\pi r} \frac{dy}{d\theta} \right)$$

$$\mathbf{r} = \mathbf{R}_b + \mathbf{y}$$

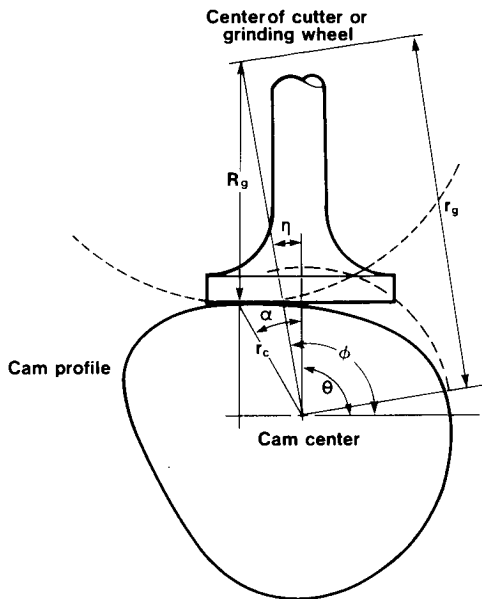
Roller followers:



$$r_g = (r^2 + (R_g - R_r)^2 - 2r(R_g - R_r) \cos \alpha)^{1/2}$$

$$\phi = \sin^{-1} \frac{R_g - R_r}{r_g} + \theta$$

Flat followers:



$$r_c = \left(r^2 + \left(\frac{180}{\pi} \frac{dy}{d\theta} \right)^2 \right)^{1/2}$$

$$r_g = (R_g^2 + r_c^2 + 2R_g r_c \cos \alpha)^{1/2}$$

$$\phi = \cos^{-1} \left(\frac{r_c + R_g \cos \alpha}{r_g} \right) - \alpha + \theta$$

where:

β is duration of lift h ;

$\Delta\theta$ is angular increment of calculation;

h is total cam lift over angle β ;

R_b is base circle radius;

R_g is grinder radius (set to zero for cam profile);

R_r is roller radius (set to zero for point follower);

θ is cam angle;

y is follower lift;

$\frac{dy}{d\theta}$ is follower velocity;

$\frac{d^2y}{d\theta^2}$ is follower acceleration;

α is pressure angle;

ϕ is angle from zero to grinder center;

r_g is center to center distance of grinder and cam.

Reference:

M.F. Spotts, *Design of Machine Elements*, Prentice-Hall 1971.

Remarks:

A flat follower will not properly follow a cam profile with any concave sections, e.g., see figure 1.



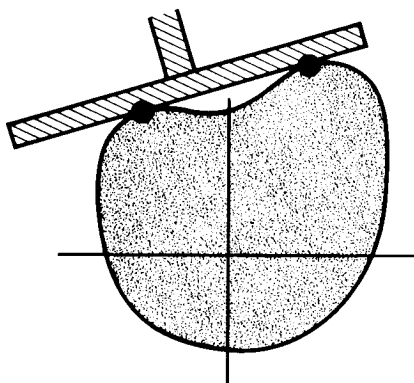


Figure 1
Note two points of contact

A roller follower will not properly follow a cam profile with concave section whose radius is less than the roller radius, e.g., see figure 2.

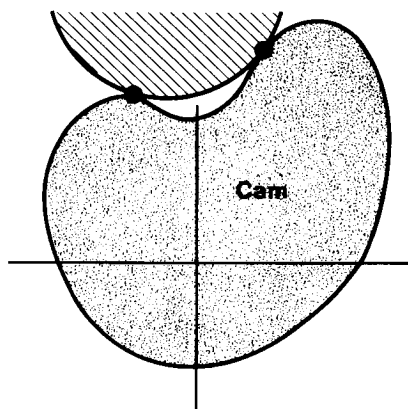


Figure 2
Note two points of contact

When the program is loaded, roller follower and harmonic profile modes are automatically selected.

Profiles other than harmonic and cycloidal may be generated by substituting them instead of label 1 or label 2. Example 3 demonstrates this.

Registers R_8 and $R_{S0}-R_{S9}$ are available for user storage.

For a parabolic profile, substitute the LBL 3 subroutine of ME1-14A for LBL 1 or LBL 2 of ME1-13A.

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
1	Load side 1 and side 2.			
2	Select flat or roller follower (1 = flat, 0 = roller. Roller follower is set when card is loaded).		f A	1/0
3	Select cam function type: Harmonic (set when card was loaded) or cycloidal.	1 2	f B f B	1.000 00 2.000 00
4	Input starting angle.	θ_0	ENTER +	θ_0
5	Input duration of lift.	β	ENTER +	β
6	Input increment of θ .	$\Delta\theta$	f C	0.000 00
7	Input lift.	h	f D	h
8	Input radius of roller (skip for flat followers).	R_r	ENTER +	R_r
9	Input radius of grinder (use zero if cam profile is desired).	R_g	ENTER +	R_g
10	Input base radius.	R_b	f E	$(R_r - R_g)$
11	For automatic output, go to step 15.			
12	Output angle and lift.		B	θ, y
13	Optional: Output other quantities of velocity and acceleration		C	$dy/d\theta, d^2y/d\theta^2$
	and/or pressure angle		D	α
	and/or grinder radius and angle.		E	r_g, ϕ



STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
14	For next increment, go to			
	step 12. For a new lift, go to			
	step 4. For a new case, go to			
	step 2.			
15	Automatic output of θ , y , $dy/d\theta$,			
	$d^2y/d\theta^2$, α , r_g , and ϕ with			
	increments of $\Delta\theta$ from θ_0			
	through $\theta_0 + \beta$.		A	θ , y , $dy/d\theta$
16	For next lift, go to step 4. For			
	a new case, go to step 2.			

Example 1:

Design a harmonic cam with a 1.0 inch roller follower, which develops harmonic motion, dropping from a base radius of 12.0 inches to 7.5 inches in 130° of rotation. From 130° to 170° , increase the lift to the original base radius. Using 10° increments, generate the cam profile by letting $R_g = 0$.

θ°	y (in)	$dy/d\theta$ (in/deg)	$d^2y/d\theta^2$ (in/deg ²)	α°	r_g (in)	ϕ
0.00 00	0.000 00	0.000 00	-1.314-03	0.000 00	11.00 00	0.000 00
10.00 00	-65.38-03	-13.01-03	-1.276-03	-3.575 00	10.94 00	9.673 00
20.00 00	-257.7-03	-25.27-03	-1.163-03	-7.029 00	10.75 00	19.35 00
30.00 00	-565.9-03	-36.06-03	-983.5-06	-10.24 00	10.45 00	29.03 00
40.00 00	-971.9-03	-44.75-03	-746.4-06	-13.09 00	10.06 00	38.71 00
50.00 00	-1.452 00	-50.84-03	-466.0-06	-15.44 00	9.588 00	48.41 00
60.00 00	-1.979 00	-53.98-03	-158.4-06	-17.15 00	9.070 00	58.14 00
70.00 00	-2.521 00	-53.98-03	158.4-06	-18.07 00	8.534 00	67.92 00
80.00 00	-3.048 00	-50.84-03	466.0-06	-18.02 00	8.007 00	77.79 00
90.00 00	-3.528 00	-44.75-03	746.4-06	-16.84 00	7.520 00	87.79 00
100.0 00	-3.934 00	-36.06-03	983.5-06	-14.37 00	7.101 00	98.00 00
110.0 00	-4.242 00	-25.27-03	1.163 03	-10.57 00	6.777 00	108.4 00
120.0 00	-4.435 00	-13.01-03	1.276-03	-5.628 00	6.571 00	119.1 00
130.0 00	-4.500 00	0.000 00	1.314-03	0.000 00	6.500 00	130.0 00
130.0 00	0.000 00	0.000 00	13.88-03	0.000 00	6.500 00	130.0 00
140.0 00	659.0-03	125.0-03	9.814-03	41.27 00	7.437 00	145.1 00
150.0 00	2.250 00	176.7-03	0.000 00	46.08 00	9.085 00	154.5 00
160.0 00	3.841 00	125.0-03	-9.814-03	32.26 00	10.51 00	162.9 00
170.0 00	4.500 00	0.000 00	-13.88-03	0.000 00	11.00 00	170.0 00

Keystrokes:

Select roller follower by pressing **f A** until zero is displayed.

f A →

0.000 00

Select harmonic cam:

1 **f B** →

1.000 00

0 **ENTER** 130 **ENTER**

10 **f C** →

0.000 00

7.5 **ENTER** 12 **- f D** →

-4.500 00

1 **ENTER** 0 **ENTER** 12 **f E** →

1.000 00

A →

0.000 00 *** (θ)

0.000 00 *** (y)

0.000 00 *** ($dy/d\theta$)

-1.314-03 *** ($d^2y/d\theta^2$)

0.000 00 *** (α)

11.00 00 *** (r_g)

0.000 00 *** (ϕ)

10.00 00 ***

-65.38-03 ***

-13.01-03 ***

-1.276-03 ***

-3.575 00 ***

10.94 00 ***

9.673 00 ***

⋮

etc.

For the lift back to the original base radius, input β ($170^\circ - 130^\circ = 40^\circ$) and $\Delta\theta$. The start of this lift ($\theta_0 = 130^\circ$) is already displayed and does not need to be keyed in again (unless you hit **R/S** and stopped the calculation prematurely).

Keystrokes:

40 **ENTER** 10 **f C** →

0.000 00

Key in new lift:

4.5 **f D** →

4.500 00

Key in previous roller and grinder radii and new base radius of 7.5:

1 **ENTER** 0 **ENTER** 7.5 **f E** →

1.000 00

A →

130.0 00 ***



```

0.000 00 ***
0.000 00 ***
13.88-03 ***
0.000 00 ***
6.500 00 ***
130.0 00 ***
140.0 00 ***
659.0-03 ***
125.0-03 ***
9.814-03 ***
41.27 00 ***
7.437 00 ***
145.1 00
:
etc.

```

Example 2:

Design a cycloidal, flat-faced cam with a lift of 50 millimeters in 40 degrees. The base radius is 500 millimeters and a 200 millimeter cutter is to be used for manufacture. Calculate θ , y , r_g and ϕ at 10 degree increments and calculate dy/dt ($dy/dt = \omega dy/d\theta$) at 20 degrees for a speed of 600 RPM.

Keystrokes:

Press **f A** until 1.000 00 is displayed:

f A →

1.000 00

Select cycloidal subroutine:

2 **f B** →

2.000 00

Input θ_0 , β , $\Delta\theta$.

0 **ENTER** 40 **ENTER**

10 **f C** →

0.000 00

Input h :

50 **f D** →

50.00 00

Input R_g and R_b :

200 **ENTER** 500 **f E** →

200.0 00

B →

0.000 00 *** (θ)

0.000 00 *** (y)

E →	700.0 00 *** (r_g)
	0.000 00 *** (ϕ)
B →	10.00 00 ***
	4.542 00 ***
E →	708.2 00 ***
	15.80 00 ***
B →	20.00 00 ***
	25.00 00 ***
E →	739.0 00 ***
	31.18 00 ***
Compute dy/dt at 20 degrees:	
C →	2.500 00 *** ($dy/d\theta$)
	0.000 00 *** ($d^2y/d\theta^2$)
x$\geq$y →	2.500 00 ($dy/d\theta$)
600 ENTER 10 ÷ 360 x x →	54.00 03 (dy/dt ; mm/sec)
B →	30.00 00 ***
	45.46 00 ***
E →	748.9 00 ***
	35.49 00 ***
B →	40.00 00 ***
	50.00 00 ***
E →	750.0 00 ***
	40.00 00 ***

Example 3:

A cam with a flat-faced follower is to convert an angular input to a linear output according to the following equation and its derivatives:

$$y = (\theta/\beta)^2$$

$$y' = 2 (\theta/\beta)$$

$$y'' = 2$$

Let $\beta = 90^\circ$ and $h = 1$ inch. Generate the cam profile from 0° to 90° in increments of 15° by setting $R_g = 0$.

$$R_b = 3.0 \text{ inches}$$

$$h = 1.0 \text{ inches}$$

The first step is to write a cam function subroutine incorporating the function and the derivatives. The subroutine can access (θ/β) in R_E and must store y' in R_4 , and y'' in R_3 , before returning to the main program with y in the X-register. One such subroutine is shown below:

```

LBL 3
  2
STO 3  (y''calculated and stored)
RCL E
  x
STO 4  (y'calculated and stored)
RCL E
  x2
RTN    (y calculated)

```

Now, load this sequence into program memory in place of LBL 1 (steps 168-188) or LBL 2 (steps 189-214). After this, the following keystrokes will generate the cam data:

Keystrokes:**Outputs:**

Select flat-faced follower by pressing **f A** until 1.000 00 appears:

f A →	1.000 00
Select subroutine 3 (since the new subroutine is LBL 3):	
3 f B →	3.000 00
0 ENTER 90 ENTER	
15 f C →	0.000 00
1 f D →	1.000 00
0 ENTER 3.0 f E →	0.00 00
A →	0.000+00 ***
	0.000+00 ***
	0.000+00 ***
	246.9-06 ***
	0.000+00 ***
	3.000+00 ***
	0.000+00 ***
	15.00+00 ***
	27.78-03 ***
	3.704-03 ***
	246.9-06 ***
	4.009+00 ***
	3.035+00 ***
	19.01+00 ***
	30.00+00 ***

111.1-03 ***
7.407-03 ***
246.9-06 ***
7.768+00 ***
3.140+00 ***
37.77+00 ***
45.00+00 ***
250.0-03 ***
11.11-03 ***
246.9-06 ***
11.08+00 ***
3.312+00 ***
56.08+00 ***
60.00+00 ***
444.4-03 ***
14.81-03 ***
246.9-06 ***
13.84+00 ***
3.547+00 ***
73.84+00 ***
75.00+00 ***
694.4-03 ***
18.52-03 ***
246.9-06 ***
16.02+00 ***
3.844+00 ***
91.02+00 ***
90.00+00 ***
1.000+00 ***
22.22-03 ***
246.9-06 ***
17.66+00 ***
4.198+00 ***
107.7-00 ***

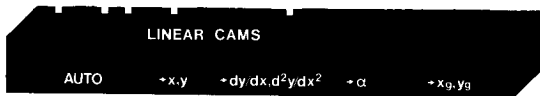


CAM DATA SUMMARY

θ	θ/β	y	r_o	ϕ
0°	0	0	3.000	0
15°	0.167	27.78-03	3.035	19.01
30°	0.333	111.1-03	3.140	37.77
45°	0.500	250.0-03	3.312	56.08
60°	0.667	444.4-03	3.547	73.84
75°	0.833	694.4-03	3.844	91.02
90°	1.000	1.000-00	4.198	107.7

Note that $y = (\theta/\beta)^2$ as specified by the original equation.

LINEAR CAMS



This program computes parameters necessary for the design of harmonic, cycloidal or parabolic profiles for linear cams with roller followers.

Equations:

$$y = hf (x/L) + R_b$$

$$x_g = x - (R_g - R_f) \sin \alpha \quad y_g = y + (R_g - R_f) \cos \alpha$$

$$\alpha = \tan^{-1} \left(\frac{dy}{dx} \right)$$

$$= \tan^{-1} \left(\frac{h}{L} f' (x/L) \right)$$

$$\frac{dy}{dx} = \frac{h}{L} f' (x/L)$$

$$\frac{d^2y}{dx^2} = \frac{h}{L^2} f'' (x/L)$$

For harmonic profiles:

$$f (x/L) = \left(1 - \cos \left(\frac{180x}{L} \right) \right)$$

For cycloidal profiles:

$$f (x/L) = \left(\frac{x}{L} - \frac{1}{2\pi} \sin \frac{180x}{L} \right)$$

For parabolic profiles:

$$f (x/L) = \begin{cases} 2h \left(\frac{x}{L} \right)^2 & \frac{x}{L} < .5 \\ \left[1 - 2 \left(1 - \frac{x}{L} \right)^2 \right] & \frac{x}{L} \geq .5 \end{cases}$$



where:

L is the duration of lift h ;

Δx is the linear increment of calculation;

h is the total follower lift over length L ;

y_b is the base height from reference datum to roller center;

R_r is the roller radius (zero for point follower);

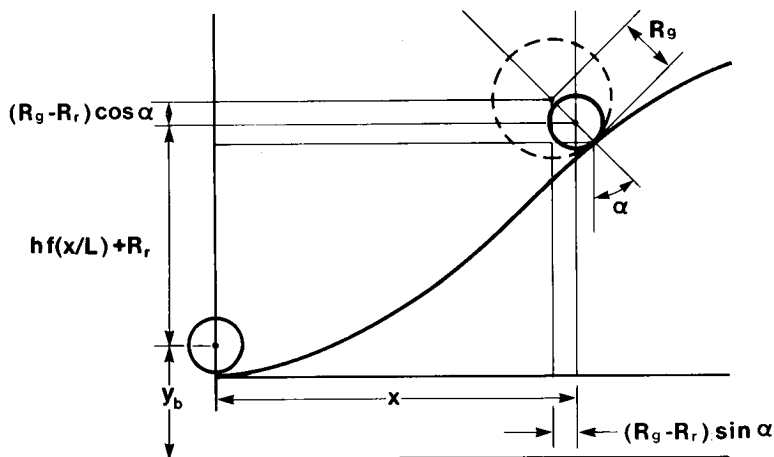
R_g is the grinder radius;

x is the linear displacement of cam;

y is the roller center height above datum;

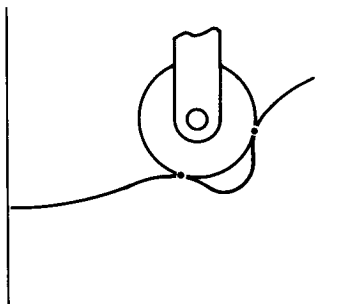
(x_g, y_g) is the grinder center for displacement x ;

α is the pressure angle.



Remarks:

The roller follower will not properly follow a cam profile with concave sections whose radius is less than the roller radius.



Note two points of contact

When the program is loaded, the harmonic profile mode is assumed. You may change to cycloidal by keying 2 and pressing **f A**. Parabolic is selected by keying 3 and pressing **f A**. Keying 1 and pressing **f A** returns the program to original status.

Arbitrary functions of (x/L) may be substituted in a manner analogous to that of example 3, ME1-13A.

Registers R_{S0} – R_{S9} are available for user storage.

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
1	Load side 1 and side 2.			
2	Select cam function type:			
	Harmonic (set when card			
	was loaded)	1	f A	1
	or cycloidal	2	f A	2
	or parabolic	3	f A	3
3	Input starting x.	x_0	ENTER	x_0
4	Input duration of lift.	L	ENTER	L
5	Input increment of x.	Δx	f B	0.000 00
6	Input lift.	h	f C	h
7	Input height of follower center			
	above reference datum at x_0 .	y_b	f D	y_b
8	Input grinder radius.	R_g	ENTER	R_g
9	Input roller radius.	R_r	f E	$R_g - R_r$
10	For automatic output, go to			
	step 14.			
11	Output x, y coordinates of			
	roller.		B	x, y
12	Optional: output other			
	quantities:			
	Follower velocity and			
	acceleration,		C	$dy/dx, d^2y/dx^2$
	and/or pressure angle,		D	α
	and/or grinder coordinates.		E	x_g, y_g

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
13	For next increment, go to			
	step 11. For a new case, go to			
	step 2.			
14	Automatic output of x , y , dy/dx ,			
	d^2y/dx^2 , α , x_g , and y_g with			
	increments of Δx from x_0			
	through $x + L$.		A	$x, y, dy/dx \dots$
15	For a new case, go to step 2.			

Example:

Design a harmonic, linear profile which has a base follower displacement of 4 cm, and a 3 cm lift over a distance of 7 cm. After the harmonic profile, a cycloidal lift of 2 cm occurs over a distance of 8 cm. Then a parabolic profile returns the follower to its original height (a drop of 5 cm) over a distance of 10 cm.

The follower and the grinder both have a radius of 1 cm. Therefore, the grinder and follower paths are equivalent. Instead of generating redundant grinder data, generate the surface profile by setting $R_g = 0$.

Use 1 cm step size.

Keystrokes:

Harmonic segment from 0 cm to 7 cm.

1 **f A** —————→
 0 **ENTER** 7 **ENTER** 1 **f B** —————→
 3 **f C** —————→
 4 **f D** —————→
 0 **ENTER** 1 **f E** —————→
A —————→

Outputs:

1.000 00 (harmonic profile)
 0.000 00
 3.000 00
 4.000 00
 -1.000 00
 0.000 00 *** (x)
 4.000 00 *** (y)
 0.000 00 *** (dy/dx)
 302.1-03 *** (d^2y/dx^2)
 0.000 00 *** (α)
 0.000 00 *** (x_g)

3.000 00 *** (y_g)
1.000 00 ***
4.149 00 ***
292.1-03 ***
272.2-03 ***
16.28 00 ***
1.280 00 ***
3.189 00 ***
...
7.000 00 ***
7.000 00 ***
0.000 00 ***
-302.1-03 ***
0.000 00 ***
7.000 00 ***
6.000 00 ***

Cycloidal segment from 7 cm to 15 cm.

2 **f** **A** →
7 **ENTER** 8 **ENTER** 1 **f** **B** →
2 **f** **C** →
7 **f** **D** →
A →

2.000 00
0.000 00
2.000 00
7.000 00
7.000 00 *** (x)
7.000 00 *** (y)
0.000 00 *** (dy/dx)
0.000 00 *** (d^2y/dx^2)
0.000 00 *** (α)
7.000 00 *** (x_g)
6.000 00 *** (y_g)
8.000 00 ***
7.025 00 ***
73.22-03 ***
138.8-03 ***
4.188 00 ***
8.073 00 ***
6.028 00 ***

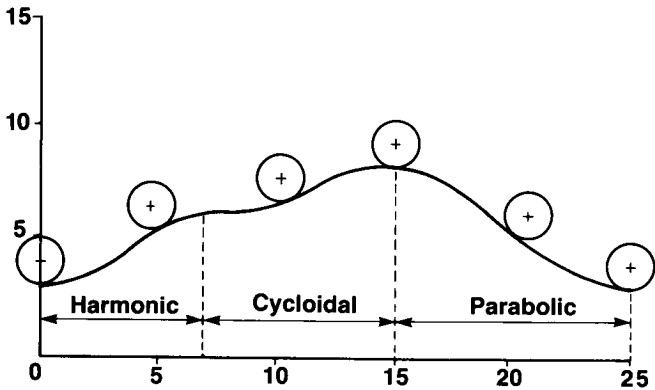
.
 .
 .
 14.00 00 ***
 8.975 00 ***
 73.22-03 ***
 -138.8-03 ***
 4.188 00 ***
 14.07 00 ***
 7.978 00 ***
 15.00 00 ***
 9.000 00 ***
 0.000 00 ***
 0.000 00 ***
 0.000 00 ***
 15.00 00 ***
 8.000 00 ***

Parabolic segment from 15 cm to 25 cm.

3 **f** **A** $\longrightarrow$ 3.000 00
 15 **ENTER** 10 **ENTER** 1 **f** **B**
 5 **CHS** **f** **C** 9 **f** **D** $\longrightarrow$ 9.000 00
A $\longrightarrow$ 15.00 00 *** (x)
 9.000 00 *** (y)
 0.000 00 *** (dy/dx)
 -200.0-03 *** (d²y/dx²)
 0.000 00 *** (α)
 15.00 00 *** (x_g)
 8.000 00 *** (y_g)
 16.00 00 ***
 8.900 00 ***
 -200.00-03 ***
 -200.00-03 ***
 -11.31 00 ***
 15.80 00 ***
 7.919 00 ***

.
 .
 .

24.00 00 ***
4.100 00 ***
-200.0-03 ***
200.0-03 ***
-11.31 00 ***
23.80 00 ***
3.119 00 ***
25.00 00 ***
4.000 00 ***
0.000 00 ***
200.0-03 ***
0.000 00 ***
25.00 00 ***
3.000 00 ***



Notes

GEAR FORCES



This program computes three mutually perpendicular forces, resulting from input torque, on helical, bevel or worm gears.

Helical gear equations:

$$F_t = \frac{T}{r}$$

$$F_{gs} = F_t \tan \phi$$

$$F_{gax} = F_t \tan \alpha$$

$$\tan \phi = \frac{\tan \phi_n}{\cos \alpha}$$

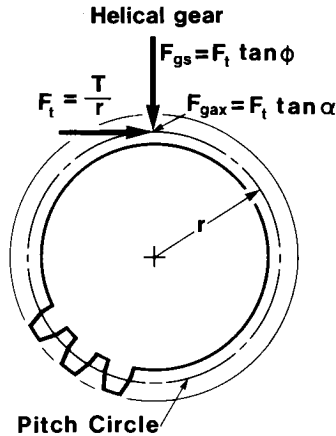


Figure 1-Helical Gear

where:

T is the input torque;

r is the pitch radius of the input gear;

F_t is the tangential force;

α is the helix angle measured from the axis of the gear (for spur gears $\alpha = 0$);

ϕ_n is the pressure angle measured perpendicular to the gear tooth;

ϕ is the pressure angle measured perpendicular to the gear axis;

F_{gs} is the radial force trying to separate the gears;

F_{gax} is the force parallel to the gear axis.

Bevel gear equations:

$$F_t = \frac{T}{r}$$

$$F_{bpax} = F_t \left(\frac{\tan \phi_n \sin (\text{cone} \angle)}{\cos \alpha} + \tan \alpha \cos (\text{cone} \angle) \right)$$

$$F_{bgax} = F_t \left(\frac{\tan \phi_n \cos (\text{cone} \angle)}{\cos \alpha} - \tan \alpha \sin (\text{cone} \angle) \right)$$

$$\tan \phi = \frac{\tan \phi_n}{\cos \alpha}$$

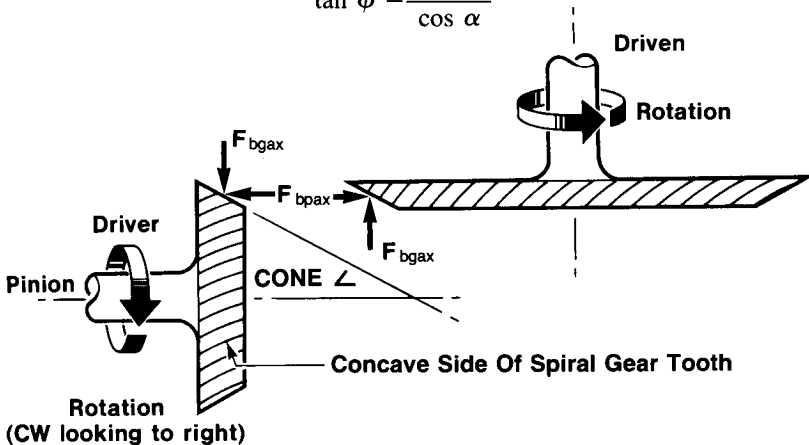


Figure 2—Spiral Bevel Gears

where:

T is the input (pinion) torque;

r is the pitch radius of the pinion gear;

F_t is the tangential force;

α is the pinion spiral angle (zero for straight tooth bevel gears);

ϕ_n is the pressure angle measured perpendicular to the gear tooth;

ϕ is the pressure angle measured perpendicular to the gear axis;

Cone $\angle$ is the pitch cone angle of the pinion;

F_{bpax} is the force along the axis of the bevel pinion;

F_{bgax} is the force along the axis of the bevel gear.

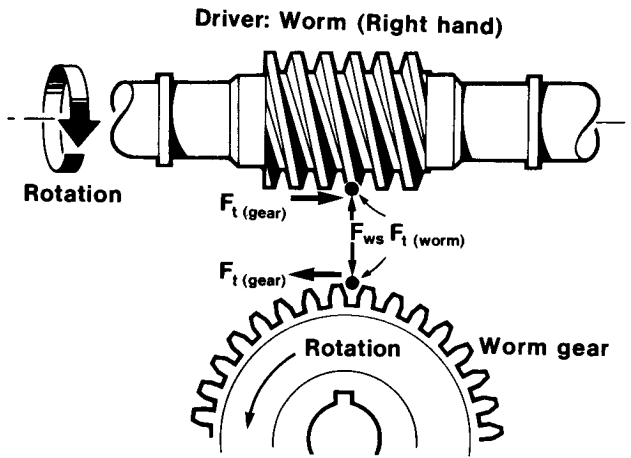
Worm gear equations:

$$F_t = \frac{T}{r}$$

$$F_{ws} = F_t \left(\frac{\sin \phi_n}{\cos \phi_n \sin \alpha + f \cos \alpha} \right)$$

$$F_{gax} = F_t \frac{1 - \frac{f \tan \alpha}{\cos \phi_n}}{\tan \alpha + \frac{f}{\cos \phi_n}}$$

$$\tan \phi = \frac{\tan \phi_n}{\cos \alpha}$$



where:

T is the input (worm) torque;

n is the pitch radius of the worm;

F_t is the tangential force on the worm;

α is the lead angle of the worm ($\alpha = \tan^{-1} (L/2\pi r)$, where L is the lead of the worm);

ϕ_n is the pressure angle measured perpendicular to the worm teeth;

ϕ is the pressure angle measured parallel to the worm axis;

f is the coefficient of friction;

F_{ws} is the separating force between the worm and gear;

F_{gax} is the force parallel to the gear axis.

Remarks:

For bevel gears, the spiral angle (α) is positive if the concave face of the pinion teeth are facing the direction of rotation (see figure 2). α is negative if the convex surface of the pinion teeth face the direction of rotation.

Registers R_0 – R_3 , R_7 – R_{S9} and R_c – R_l are available for user storage.

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
1	Load side 1.			
2	Input torque.	T	ENTER	T
3	Input pitch radius and calculate tangential force.	r	A	F_t
4	Input helix angle for helical gears, or spiral angle for spiral bevel gears, or lead angle for worm gears.	α	B	α
5	Input normal pressure angle	ϕ_n	C	ϕ_n
	or			
	input pressure angle.	ϕ	D	ϕ_n
6	For helical gears, go to step 7, for bevel gears, go to step 9, for worm gears, go to step 12.			
7	Calculate separating force and axial force.		E	F_{gs}, F_{gax}
8	For a new case, return to step 2 and modify inputs as necessary.			
9	Input bevel cone angle.	cone $\angle$	F A	cone $\angle$
10	Calculate pinion axial force and gear axial force.		F B	F_{bpax}, F_{bgax}

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
11	For a new case, return to step 2 and modify inputs as necessary.			
12	Input coefficient of friction.	f	f D	f
13	Calculate separating force and gear axial force.		f E	F_{ws}, F_{gax}
14	For a new case, go to step 2 and modify inputs as necessary.			

Example 1:

A helical gear with pitch radius 12 cm has a torque applied to it of 450,000 dyne-cm. The helix angle is 30°, and the normal pressure angle, measured perpendicular to a tooth, is 17.5°. Find the tangential, separating, and thrust forces.

Keystrokes:

450000 **ENTER** 12 **A** →
30 **B** 17.5 **C E** →

Outputs:

37500.00 (F_t)
13652.84 *** (F_{gs})
21650.64 *** (F_{gax})

Example 2:

A spiral pinion with mean radius 1.73 inches is subjected to a torque of 745 in-lb. The pinion is cut with a normal pressure angle of 20°, a spiral angle of 35°, with a pitch cone of 18°. Find the forces acting on the pinion. Rotation is in the direction of the concave side of the pinion teeth, so α is positive 35°.

Keystrokes:

745 **ENTER** 1.73 **A** →
35 **B** 20 **C** 18 **f A f B** →

Outputs:

430.64 (F_t)
345.90 *** (F_{bpax})
88.80 *** (F_{bgax})

If the rotation were reversed, leaving all other input values unchanged, what would the forces be?

35 **CHS** **B** **f** **B** $\longrightarrow$ -227.65 *** (F_{bpax})
 275.16 *** (F_{bgax})

Example 3:

A torque of 512 in-lb is applied to a worm gear having a pitch diameter of 2.92 inches and a lead of 2.20 inches. The normal pressure angle is 20° , and the coefficient of friction is 0.10. Find the lead angle and the forces on the worm and worm gear.

Keystrokes:

512 **ENTER** 2.92 **ENTER**

2 **$\div$** **A** $\longrightarrow$

Calculate lead angle ($\alpha = \tan^{-1}(\text{lead}/2\pi r)$).

2.2 **ENTER** 2 **$\div$** **π** **$\div$**

2.92 **ENTER** 2 **$\div$** **$\div$** **TAN⁻¹** $\longrightarrow$

B 20 **C** .1 **f** **D** **f** **E** $\longrightarrow$

Outputs:

350.68 (F_t)

13.49 (α)

379.10 *** (F_{ws})

986.99 *** (F_{gax})

STANDARD EXTERNAL INVOLUTE SPUR GEARS

EXTERNAL INVOLUTE SPUR GEARS

P+N-D.t

$\phi \cdot d_w$

+inv ϕ_w

+ ϕ_w

+M

This program calculates various parameters for standard external involute spur gears. Given the diametral pitch P , number of teeth N , pressure angle ϕ , and pin diameter d_w , the program will calculate the pitch diameter D , tooth thickness t , and the involute and corresponding flank angle $\text{inv } \phi_w$ and ϕ_w . The flank angle ϕ_w is calculated from the involute by a Newton's method iterative solution for the equation $f(\phi_w) = 0$,

where:

$$f(\phi_w) = \tan \phi_w - \phi_w - \text{inv } \phi_w$$

In this solution, an initial guess is made for ϕ_w :

$$\phi_w^{(0)} = (3 \text{ inv } \phi_w)^3$$

Newton's method then provides refinements of the initial guess by

$$\begin{aligned} \phi_w^{(n+1)} &= \phi_w^{(n)} - \frac{f(\phi_w^{(n)})}{f'(\phi_w^{(n)})} \\ &= \phi_w^{(n)} - \frac{\tan \phi_w^{(n)} - \phi_w^{(n)} - \text{inv } \phi_w}{\tan^2 \phi_w^{(n)}} \end{aligned}$$

The program also calculates various measurements over pins, namely, the theoretical values of the measurement over pins, M ; the radius to the center of the pin, 1 ; and the measurement over one pin, R_w . In addition, given the value of the tooth thinning Δt , the program will return the measurement over pins with tooth thinning, M_t .

Equations:

$$D = \frac{N}{P}$$

$$t = \frac{\pi}{2P}$$

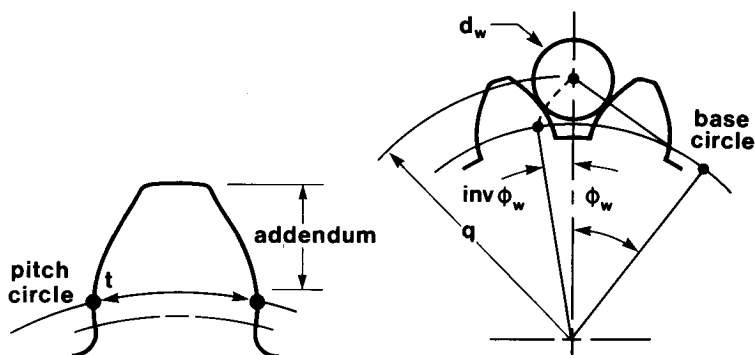
$$\text{inv } \phi_w \text{ (radians)} = \frac{t}{D} + \tan \phi - \frac{\pi \phi}{180} + \frac{d_w}{D \cos \phi} - \frac{\pi}{N}$$

$$M = \begin{cases} d_w + 2q & (N \text{ even}) \\ d_w + 2q \cos \left(\frac{90}{N} \right) & (N \text{ odd}) \end{cases}$$

$$q = \frac{D \cos \phi}{2 \cos \phi_w}$$

$$R_w = q + \frac{d_w}{2}$$

$$M_t = M - \Delta t \frac{\cos \phi}{\sin \phi_w}$$



Reference:

Adapted from a program submitted to the HP-65 Users's Library by Mr. John Nemcovich, Los Angeles, CA.

Dudley, D.W., *Gear Handbook*, McGraw-Hill, 1962.

Remarks:

Registers R_0 , $R_{S0}-R_c$ and I are available for user storage.

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
1	Load side 1 and side 2.			
2	Input diametral pitch P	P	ENTER $\blacktriangleright$	P
	and number of teeth N to			
	calculate the pitch diameter			
	and tooth thickness t.	N	A	D, t
3	Input pressure angle ϕ	ϕ	ENTER $\blacktriangleright$	ϕ
	and pin diameter d_w .	d_w	B	ϕ
4	Calculate the involute $\text{inv } \phi_w$.		C	$\text{inv } \phi_w$ (deg.)
5	Calculate the corresponding			
	flank angle.		D	ϕ_w (deg.)
6	Calculate the measurement			
	over pins (theoretical).		E	M
7	Input tooth thinning and			
	calculate measurement over			
	pins with tooth thinning.	Δt	f A	M_t
8	Calculate radius to the center			
	of pin.		f B	q
9	Calculate measurement over			
	one pin.		f C	R_w
10	To change tooth thinning, go			
	to step 7. To change any other			
	input, go to step 2.			
	Note: If d_w is not known, it may			
	be calculated from the pin			
	constant k and pitch P:	k	ENTER $\blacktriangleright$	
	$d_w = k/P$	P	=	d_w
11	To calculate ϕ_w directly from			
	$\text{inv } \phi_w$: store $\text{inv } \phi_w$ in register 6	$\text{inv } \phi_w$	STO 6	
	and calculate ϕ_w .		D	ϕ_w (deg.)

Example:

A 27-tooth gear with pitch 8 is cut with a 20° pressure angle. The pin diameter is 0.24 inches, and tooth thinning is reckoned at 0.002 inches. Calculate the unknown parameters.

Keystrokes:

8 **ENTER** 27 **A** →

20 **ENTER** 0.24 **B** **C** →

D →

E →

0.002 **f** **A** →

f **B** →

f **C** →

Outputs:

3.3750 *** (D)

0.1963 *** (t)

1.8565 *** (inv ϕ_w)

25.6215 *** (ϕ_w)

3.7514 *** (M)

3.7470 *** (M_t)

1.7587 *** (q)

1.8787 *** (R_w)

BELT LENGTH



This program computes the belt length around an arbitrary set of pulleys. It may also be used to compute the total length between any connected set of coordinates. The program assumes the coordinates of the first pulley to be (0,0). Optionally the x, y coordinates of the intersections of the belt and pulleys may be output.

$(x_i, y_i, R_i) = x, y$ coordinates and radius of pulley i

R_1 = Radius of first pulley

C.D. = Center to center distance of consecutive pulleys

L = Total length of belt

Equations:

$$L_{12} = \sqrt{C.D.^2 - (R_2 - R_1)^2}$$

$$\text{Arc Length}_2 = R_2 (\pi - \alpha - \beta - \gamma_2)$$

$$\alpha = \tan^{-1} \left(\frac{R_1 - R_2}{L_{12}} \right)$$

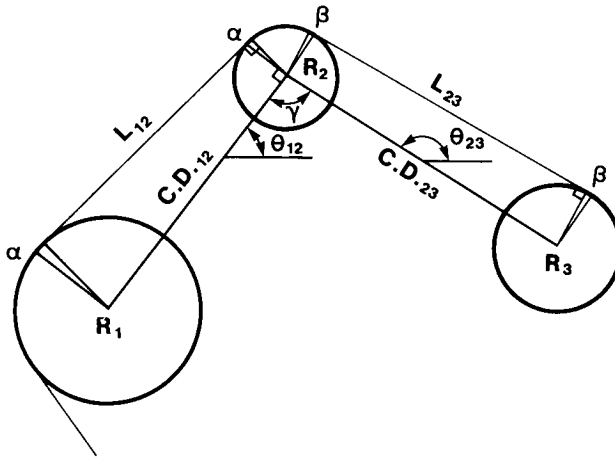
$$\beta = \tan^{-1} \left(\frac{R_3 - R_2}{L_{23}} \right)$$

$$\gamma = \theta_{12} - \theta_{23}$$

$$\theta_{12} = \tan^{-1} \frac{y_2 - y_1}{x_2 - x_1}$$

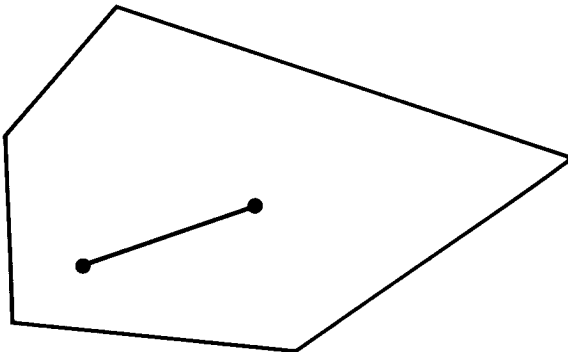
$$\theta_{23} = \tan^{-1} \frac{y_3 - y_2}{x_3 - x_2}$$



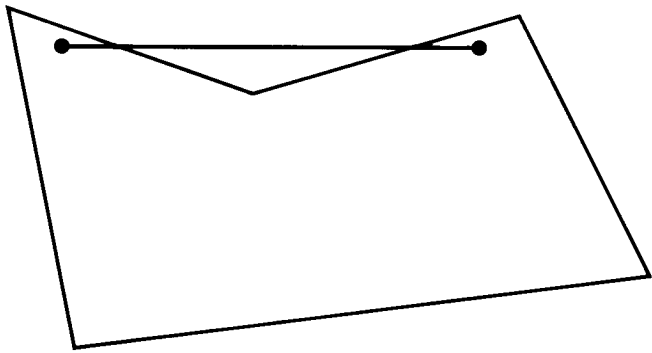


This program generates accurate results for any convex polygon, i.e., a line between any two points within the region bounded by the center-to-center line segments is entirely contained within the region.

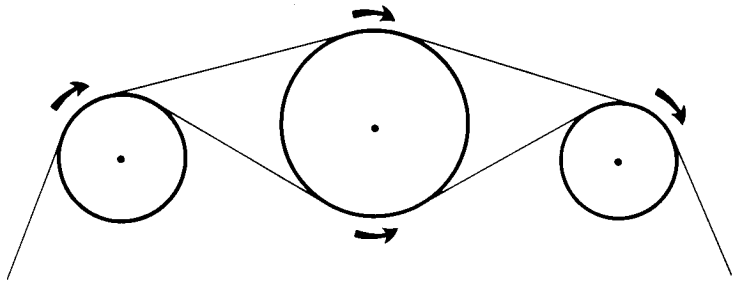
Convex



Concave

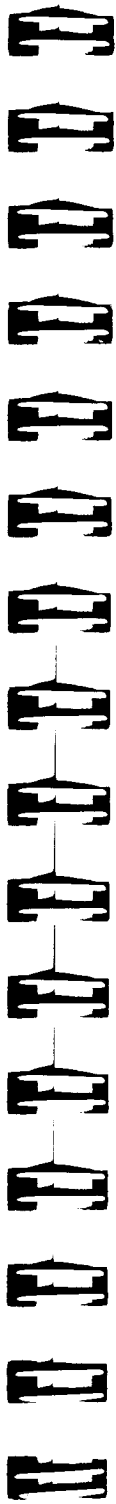
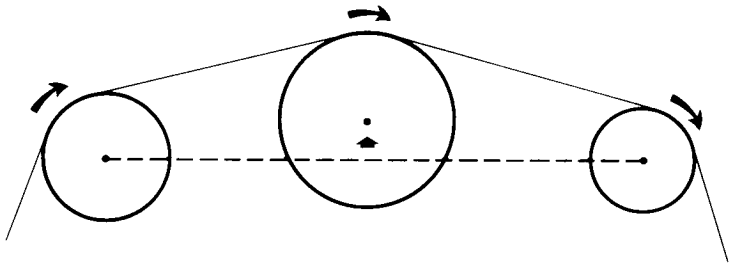


In some cases, there are two physically possible directions for the belt to take:



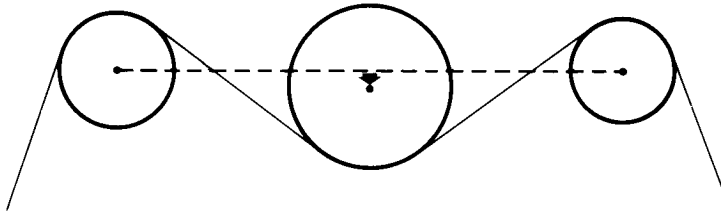
The program chooses the upper side if the middle pulley center lies above the line connecting the previous and following pulleys.

Case 1



The program chooses the lower side if the middle pulley center lies below the line connecting the previous and following pulleys.

Case 2



The program generates inaccurate answers in the second case. Note the figure bounded by the center-to-center line segments for the second case is not convex.

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
1	Load side 1 and side 2.			
2	Optional: Toggle for printing belt tangent points for each pulley.*		T A	1.00
3	Input the coordinates (x_1, y_1) and radius of the first pulley.	x_1	ENTER	x_1
		y_1	ENTER	y_1
		R_1	A	R_1
4	Input the next pulley coordinates (x_i, y_i) and radius (R_i).	x_i	ENTER	x_i
		y_i	ENTER	y_i
		R_i	B	R_i
5	Repeat step 4 for all remaining pulleys.			
6	Calculate the belt length.		C	L
7	For a new case, go to step 2.			
	*Note: Pulley coordinates have to be entered in the clockwise sense.			

Example 1:

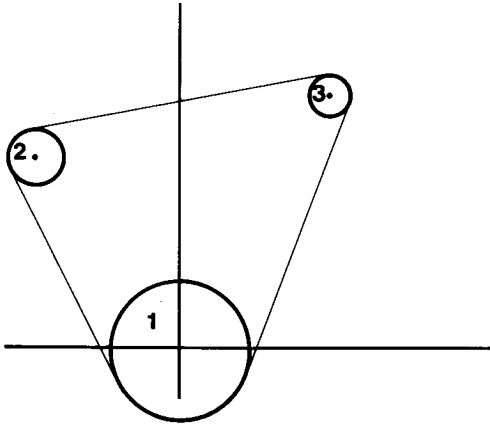
Assume three pulleys are positioned as shown below with the following coordinates and radii:

Pulley 1 (0, 0, 4 inches)

Pulley 2 (-8, 15, 1.5 inches)

Pulley 3 (9, 16, 1 inches).

Find the belt length around the three pulleys.



Keystrokes:

0 ENTER 0 ENTER 4 A →
8 CHS ENTER 15 ENTER
1.5 B →
9 ENTER 16 ENTER 1 B →
C →

Outputs:

4.00 (R₁)
1.50 (R₂)
1.00 (R₃)
66.53 (L)

Example 2:

Find the length of line connecting the points (0, 0), (1.5, 7), (3.2, -6), (0, 0.5), (0, 0). (28.01). Let the radius of each “pulley” be 0.

Keystrokes:

0 ENTER 0 ENTER 0 A →
1.5 ENTER 7 ENTER 0 B →
3.2 ENTER 6 CHS ENTER
0 B →

Outputs:

0.00
0.00
0.00
0.00



0 **ENTER** 0.5 **ENTER** 0 **B** →

0.00

C →

28.01 (L)

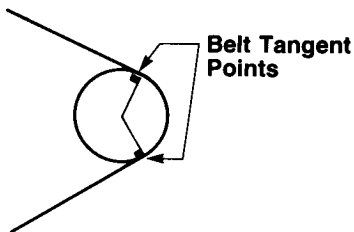
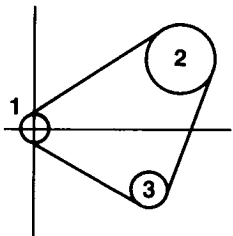
Example 3:

Find the belt length around the following pulley system, also find the belt tangent points on each pulley.

Pulley 1 (0, 0, 2.5)

Pulley 2 (30, 3, 7.5)

Pulley 3 (18, -18, 3.66)



Keystrokes:

f **A** →

0 **ENTER** 0 **ENTER** 2.5 **A** →

30 **ENTER** 3 **ENTER** 7.5 **B** →

18 **ENTER** 18 **CHS** **ENTER** 3.66

B →

C →

Outputs:

1.00

2.5 (R₁)

-0.66 *** (x)

2.41 *** (y) 1st pulley

28.03 *** (x)

10.24 *** (y) 2nd pulley

7.5 (R₂)

35.84 *** (x)

-1.71 *** (y) 2nd pulley

20.85 *** (x)

-20.30 *** (y) 3rd pulley

3.66 (R₃)

15.30 *** (x)

-20.47 *** (y) 3rd pulley

-1.85 *** (x)

-1.69 *** (y) 1st pulley

109.33 (L)

FREE VIBRATIONS

FREE VIBRATIONS

$$m\ddot{x} + c\dot{x} + kx = 0$$

$$c < c_{crit}$$

$$x_0, \dot{x}_0$$

$$t = x, \dot{x}, \ddot{x}$$

$$t_1, t_2, t_3, \dots (LIST)$$

This program provides an exact solution to the differential equation for a damped oscillator vibrating freely: $m\ddot{x} + c\dot{x} + kx = 0$.

The user inputs the mass m , spring constant k , and damping constant c at **A**. The output will be:

1. ω for an underdamped system, i.e. $c < c_{crit}$. c_{crit} is calculated by pressing **B**.
2. 0 for a critically damped system, i.e. $c = c_{crit}$.
3. -1 for an overdamped system, i.e. $c > c_{crit}$.

The initial conditions are the displacement and velocity at time zero (x_0 and $\dot{x}_0$).

Equations:

$$c_{crit} = 2\sqrt{km}$$

$$\omega = \sqrt{\frac{k}{m} - \left(\frac{c}{2m}\right)^2}$$

$$\ddot{x} = -(c\dot{x} + kx)/m$$

Underdamping

$$(c^2 - 4km < 0)$$

$$x(t) = Re^{-\frac{c}{2m}t} \cos(\omega t - \delta)$$

$$\dot{x}(t) = -R\omega e^{-\frac{c}{2m}t} \sin(\omega t - \delta) - \frac{c}{2m} Re^{-\frac{c}{2m}t} \cos(\omega t - \delta)$$

where:

$$R \cos \delta = x_0$$

$$R \sin \delta = \frac{1}{\omega} \left[\dot{x}_0 + \frac{c}{2m} x_0 \right]$$

Critical damping

$$(c = c_{crit}, \text{ or } c^2 = 4km)$$

$$x(t) = (A_{cr} + B_{cr}t)e^{-\frac{c}{2m}t}$$

$$\dot{x}(t) = \left[B_{cr} - \frac{c}{2m} (A_{cr} + B_{cr}t) \right] e^{-\frac{c}{2m}t}$$

where:

$$A_{cr} = x_0$$

$$B_{cr} = \dot{x}_0 + \frac{c}{2m} x_0$$

Overdamping

$$(c^2 - 4km > 0)$$

$$\dot{x}(t) = A_{ov}e^{r_1t} + B_{ov}e^{r_2t}$$

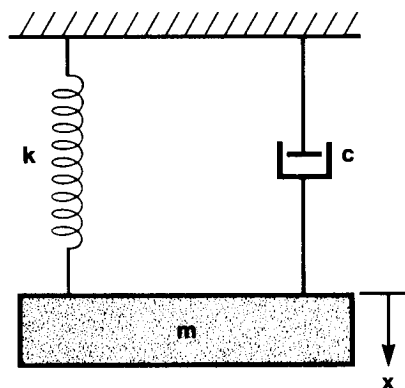
$$x(t) = A_{ov}r_1e^{r_1t} + B_{ov}r_2e^{r_2t}$$

where:

$$r_1, r_2 = -\frac{c}{2m} \pm \sqrt{\left(\frac{c}{2m}\right)^2 - \frac{k}{m}}$$

$$A_{ov} = x_0 - B_{ov}$$

$$B_{ov} = \frac{\dot{x}_0 - r_1 x_0}{r_2 - r_1}$$



Reference:

Boyce, W.E. and DiPrima, R.C., *Elementary Differential Equations*, John Wiley and Sons, 1969.

Remarks:

For overdamping, ω has no meaning and is, in fact, an imaginary number.
For $c = c_{crit}$, $\omega = 0$.

This program sets the angular mode of the calculator to radians. Erroneous answers will occur if degree mode is inadvertently set.

Registers R_{S0} – R_{S9} are available for user storage.

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
1	Load side 1 and side 2.			
2	Input the system parameters	m	ENTER	
	of mass, damping constant,	c	ENTER	
	and spring constant.	k	A	ω or 0 or -1
3	Optional: Calculate c_{crit}		B	C_{crit}
4	Input initial conditions of			
	position	x_0	ENTER	x_0
	and velocity.	$\dot{x}_0$	C	$\dot{x}_0$
5	Input t to calculate $x(t)$, $\dot{x}(t)$,			
	and $\ddot{x}(t)$.	t	D	$x(t), \dot{x}(t), \ddot{x}(t)$
6	Repeat step 5 for a different t.			
7	Input t_1 and t_2 and number of			
	intervals (n) to calculate			
	$x(t)$, $\dot{x}(t)$, and $\ddot{x}(t)$ automatically.	t_1	ENTER	t_1
		t_2	ENTER	t_2
		n	E	$x(t), \dot{x}(t), \ddot{x}(t)$
8	For different initial conditions			
	for the same system, go to			
	step 4.			
9	For a different system, go to			
	step 2.			

Example:

A mass of 20 g stretches a spiral spring 10 cm. The mass is pulled down an additional 4 cm, held, and then released. Find the mass displacement and velocity at 0.1 second intervals up to 1 second for the cases in which (a) $c = 50$ dyne-sec/cm (b) $c = c_{\text{crit}}$ and (c) $c = 400$ dyne-sec/cm.

$$k = \frac{F}{x} = \frac{mg}{x} = \frac{20\text{g} (980 \text{ cm/s}^2)}{10 \text{ cm}} = \frac{20 \times 980}{10} \text{ dyne/cm}$$

(a) $c = 50$

Keystrokes:

20 **ENTER** 50 **ENTER** 20 **ENTER**

980 **x** 10 **=** **A** $\longrightarrow$

B $\longrightarrow$

4 **ENTER** 0 **C** $\longrightarrow$

0 **D** $\longrightarrow$

0.1 **D** $\longrightarrow$

0.2 **D** $\longrightarrow$

Outputs:

9.820 (ω)

395.980 (c_{crit})

4.000 (x_0)

4.000 *** (x)

1.00000000-09 *** ($\dot{x}$)

-392.00 *** ($\ddot{x}$)

2.334 *** (x)

-29.296 *** ($\dot{x}$)

-155.494 *** ($\ddot{x}$)

-0.827 *** (x)

-28.715 *** ($\dot{x}$)

152.880 *** ($\ddot{x}$)

Or, the same results can be achieved automatically.

0 **ENTER** 1 **ENTER** 10 **E** $\longrightarrow$

0.000 *** (t)

4.000 *** (x)

1.00000000-09 *** ($\dot{x}$)

-392.000 *** ($\ddot{x}$)

0.100 ***

2.334 ***

-29.296 ***

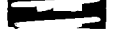
-155.494 ***

0.200 ***

-0.827 ***

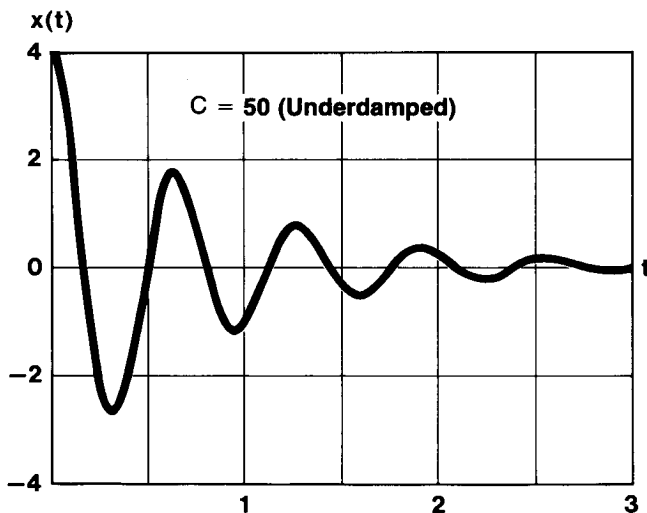
-28.715 ***

152.880 ***
0.300 ***
-2.629 ***
-5.330 ***
270.947 ***
0.400 ***
-1.932 ***
17.139 ***
146.511 ***
0.500 ***
0.153 ***
20.950 ***
-67.408 ***
0.600 ***
1.655 ***
7.187 ***
-180.174 ***
0.700 ***
1.503 ***
-9.272 ***
-124.104 ***
0.800 ***
0.184 ***
-14.685 ***
18.677 ***
0.900 ***
-0.990 ***
-7.173 ***
114.959 ***
1.000 ***
-1.114 ***
4.406 ***
98.133 ***



Solution (a) $c = 50$

t s	x cm	$\dot{x}$ cm/s	$\ddot{x}$ cm/s ²
0	4.000	0.00	-392.000
.1	2.334	-29.296	-155.494
.2	-0.827	-28.715	152.880
.3	-2.629	-5.330	270.947
.4	-1.932	17.139	146.511
.5	0.153	20.950	-67.408
.6	1.655	7.187	-180.174
.7	1.503	-9.272	-124.104
.8	0.184	-14.685	18.677
.9	-0.990	-7.173	114.959
1.0	-1.114	4.406	98.133

(b) $c = c_{\text{crit}}$

Keystrokes:

20 **ENTER** 395.98 **ENTER**20 **ENTER** 980 **X**10 **÷** **A** $\longrightarrow$ 4 **ENTER** 0 **C** $\longrightarrow$ 0 **D** $\longrightarrow$

Outputs:

0.000

4.000 (x_0)4.000 *** ($\dot{x}$)0.000 *** ($\ddot{x}$)-392.000 *** ($\ddot{x}$)

18-07

0.1 **D** →

2.958 ***
-14.567 ***
-1.464 ***

0.2 **D** →

1.646 ***
-10.826 ***
53.041 ***

⋮

Or, automatically:

0 **ENTER** 1 **ENTER** 10 **E** →

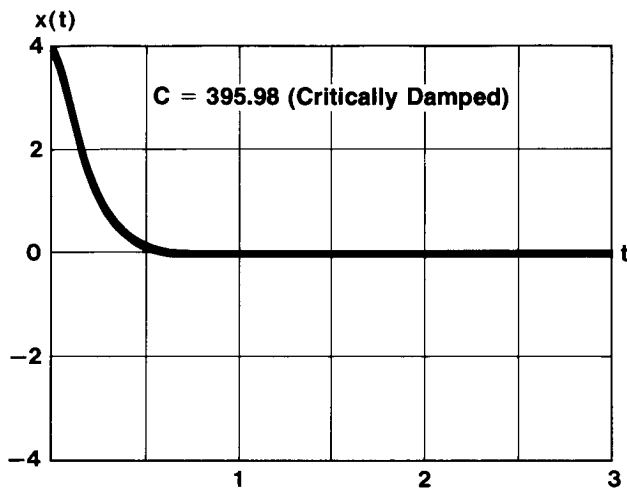
0.000 ***
4.000 ***
0.000 ***
-392.000 ***
0.100 ***
2.958 ***
-14.567 ***
-1.464 ***
0.200 ***
1.646 ***
-10.826 ***
53.041 ***
0.300 ***
0.815 ***
-6.034 ***
39.622 ***
0.400 ***
0.378 ***
-2.990 ***
22.122 ***
0.500 ***
0.169 ***
-1.389 ***
10.970 ***
0.600 ***
0.073 ***
-0.619 ***
5.098 ***
0.700 ***
0.031 ***



-0.268 ***
 2.274 ***
 0.800 ***
 0.013 ***
 -0.114 ***
 0.986 ***
 0.900 ***
 0.005 ***
 -0.048 ***
 0.419 ***
 1.000 ***
 0.002 ***
 -0.020 ***
 0.175 ***

Solution (b) $c = c_{\text{crit}}$

t s	x cm	$\dot{x}$ cm/s	$\ddot{x}$ cm/s ²
0	4.000	0.000	-392.000
.1	2.958	-14.567	-1.464
.2	1.646	-10.826	53.041
.3	0.815	-6.034	39.622
.4	0.378	-2.990	22.122
.5	0.169	-1.389	10.970
.6	0.073	-0.619	5.098
.7	0.031	-0.268	2.274
.8	0.013	-0.114	0.986
.9	0.005	-0.048	0.419
1.0	0.002	-0.020	0.175



(c) $c = 400$ **Keystrokes:**20 **ENTER** 400 **ENTER** 20 **ENTER**980 **x** 10 **=** **A** →4 **ENTER** 0 **C** →0 **D** →0.1 **D** →0.2 **D** →

Or, automatically:

0 **ENTER** 1 **ENTER** 10 **E** →**Outputs:**

-1.000 ***

4.000 (x_0)4.000 *** (x)0.000 *** ($\dot{x}$)-392.000 *** ($\ddot{x}$)2.963 *** (x)-14.469 *** ($\dot{x}$)-0.963 *** ($\ddot{x}$)1.660 *** (x)-10.752 *** ($\dot{x}$)52.336 *** ($\ddot{x}$)

0.000 ***

4.000 ***

0.000 ***

-392.000 ***

0.100 ***

2.963 ***

-14.469 ***

-0.963 ***

0.200 ***

1.660 ***

-10.752 ***

52.336 ***

0.300 ***

0.833 ***

-6.032 ***

39.022 ***

0.400 ***

0.394 ***

-3.028 ***

21.916 ***

0.500 ***

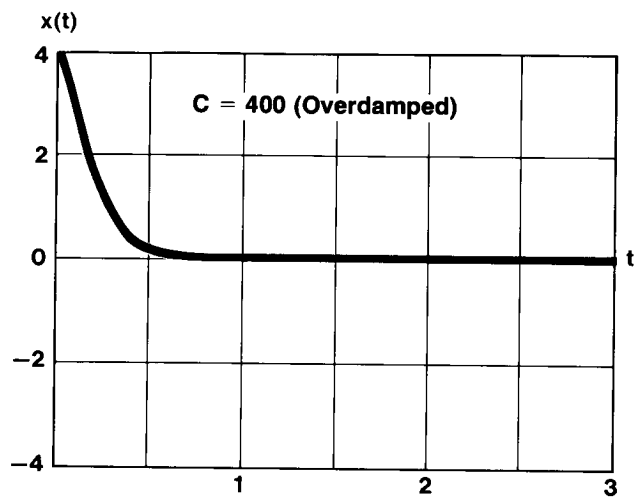
0.180 ***

-1.433 ***

11.005 ***
 0.600 ***
 0.081 ***
 -0.656 ***
 5.212 ***
 0.700 ***
 0.035 ***
 -0.293 ***
 2.384 ***
 0.800 ***
 0.015 ***
 -0.129 ***
 1.066 ***
 0.900 ***
 0.007 ***
 -0.056 ***
 0.470 ***
 1.000 ***
 0.003 ***
 -0.024 ***
 0.205 ***

Solution (c) $c = 400$

t s	x cm	$\dot{x}$ cm/s	$\ddot{x}$ cm/s ²
0	4.000	0.000	-392.000
.1	2.963	-14.469	-0.963
.2	1.660	-10.752	52.336
.3	0.833	-6.032	39.022
.4	0.394	-3.028	21.916
.5	0.180	-1.433	11.005
.6	0.081	-0.656	5.212
.7	0.035	-0.293	2.384
.8	0.015	-0.129	1.066
.9	0.007	-0.056	0.470
1.0	0.003	-0.024	0.205



Notes

VIBRATION FORCED BY $F_0 \cos \omega t$

VIBRATION FORCED BY $F_0 \cos \omega t$

$m \cdot c \cdot k = \omega_0, \omega_n, \zeta, \omega_{res}, \omega = F_0 \cdot \text{AMP}, \delta, t = x, \dot{x}, \ddot{x} \quad t_1, t_2, n = \text{LIST}$

This program finds the steady-state solution for an object undergoing damped forced oscillations from a periodic external force of the form $F_0 \cos \omega t$. The differential equation to be solved is

$$m\ddot{x} + c\dot{x} + kx = F_0 \cos \omega t$$

The program calculates the following variables: ω_0 , ω_n , ζ , ω_{res} , AMP, δ , $x(t)$, $\dot{x}(t)$, and $\ddot{x}(t)$, which are defined as follows:

Equations:

The steady-state solution ($t \rightarrow \infty$) to this equation is

$$x(t) = \frac{F_0}{\Delta} \cos(\omega t - \delta)$$

$$\dot{x}(t) = -\omega \frac{F_0}{\Delta} \sin(\omega t - \delta)$$

where:

$$\Delta = \sqrt{m^2 (\omega_0^2 - \omega^2)^2 + c^2 \omega^2}$$

$$\omega_0 = \sqrt{\frac{k}{m}} = \text{natural frequency or undamped system}$$

$$\omega_n = \sqrt{\frac{k}{m} - \left(\frac{c}{2m}\right)^2} = \text{damped natural frequency}$$

$$\zeta = \frac{c}{C_{crit}} = \frac{c}{2m \omega_0} = \text{damping ratio}$$

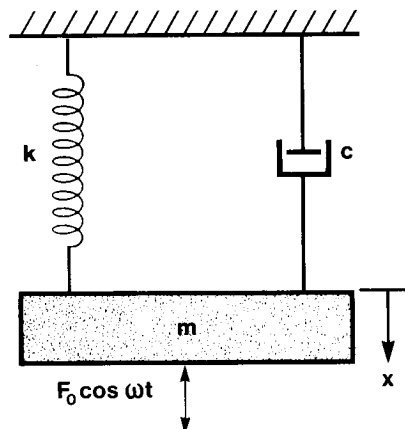
$$\delta = \tan^{-1} \frac{c \omega}{m(\omega_0^2 - \omega^2)}$$

$$\text{AMP} = \frac{F_0}{\Delta}$$

ω_{res} is computed from

$$\omega_{res}^2 = \omega_0^2 - \frac{1}{2} \left(\frac{c}{m}\right)^2$$

$$\text{AMP}_{max} = \frac{F_0}{\Delta} \quad (\text{where } \omega = \omega_{res})$$

**Reference:**

Boyce, W.E. and DiPrima, R.C., *Elementary Differential Equations*, John Wiley and Sons, 1969.

Remarks:

The above solution does not take into account the initial conditions ($x(0)$, $\dot{x}(0)$) of the system, consequently values of $x(t)$, $\dot{x}(t)$ and $\ddot{x}(t)$ calculated by this program are for large values of t . However, should you need values of $x(t)$, $\dot{x}(t)$ and $\ddot{x}(t)$ for the system with initial conditions $x(0)$ and $\dot{x}(0)$, use ME1-18A. Calculate the homogeneous solution $x(t)$, $\dot{x}(t)$ and $\ddot{x}(t)$ and add it to the values (the particular solution) calculated by this program.

This program sets the angular mode of the calculator to radians.

Registers R_{S0} — R_{S9} are available for user storage.

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
1	Load side 1 and side 2.			
2	Input the system parameters			
	of mass,	m	ENTER	
	damping coefficient	c	ENTER	
	and spring constant.	k	A	$\omega_0, \omega_n, \zeta$
3	Optional: Calculate the			
	resonant frequency ω_{res} .		B	ω_{res}
4	Input the frequency of external			
	excitation	ω	ENTER	
	and the external excitation			
	force.	F_0	C	AMP, $\delta(\text{deg.})$
5	Input t to calculate $x(t)$, $\dot{x}(t)$,			
	$\ddot{x}(t)$.	t	D	$x, \dot{x}(t) \ddot{x}(t)$
6	Input t_1 and t_2 and number of			
	intervals to calculate $x(t)$, $\dot{x}(t)$,			
	and $\ddot{x}(t)$ automatically.	t_1	ENTER	t_1
		t_2	ENTER	t_2
		n	E	n + 1 values of
				$x(t), \dot{x}(t),$
				$\ddot{x}(t)$ between
				t_1 and t_2
7	For a different external			
	excitation, applied to the same			
	system, go to step 4.			
8	For a different system, go to			
	step 2.			

Example:

A 400-lb. weight is suspended from a spring and stretches it a distance of 2 inches. The damping constant of the system is 0.5 lb-sec/ft. If the weight is driven by a periodic external force whose greatest value is 5 pounds, find (a) the resonant frequency of the system and (b) the amplitude and phase shift of the oscillation that will result if the mass is driven at the resonant frequency. Calculate the position, velocity, and acceleration for $t = 6.0$ sec. Also calculate the position, velocity, and acceleration for $t_1 = 6$ sec. and $t_2 = 10$ sec. with four intervals ($n = 4$).

$$m = \frac{F}{g} = \frac{400 \text{ lb}}{32.2 \text{ ft/sec}^2} \quad k = \frac{F}{x} = \frac{400 \text{ lb}}{2 \text{ in}} \frac{12 \text{ in}}{1 \text{ ft}}$$

Keystrokes:

400 **ENTER** 32.2 **÷** .5 **ENTER**
 400 **ENTER** 2 **÷** 12 **×** **A** **→**

B **→**

(To drive the system at the resonant frequency, leave ω_{res} in the display and key in the driving force of 5 pounds).

5 **C** **→**

6 **D** **→**

or automatically:

6 **ENTER** 10 **ENTER** 4 **E** **→**

Outputs:

13.900 *** (ω_0)

13.900 *** (ω_n)

0.001 *** (ζ)

13.900 (ω_{res})

0.719 *** (AMP)

89.917 *** (δ in deg.)

0.712 *** (x)

-1.464 *** ($\dot{x}$)

-137.499 *** ($\ddot{x}$)

6.000 ***

0.712 ***

-1.464 ***

-137.499 ***

7.000 ***

0.065 ***

-9.959 ***

-12.582 ***

8.000 ***

-0.681 ***

-3.223 ***

131.577 ***

9.000 ***
-0.386 ***
8.442 ***
74.510 ***
10.000 ***
0.500 ***
7.197 ***
-96.508 ***



Notes

EQUATIONS OF STATE

EQUATIONS OF STATE

P

V

n

R

T

This card provides both ideal gas and Redlich-Kwong equations of state. Given four of the five state variables, the fifth is calculated. For the Redlich-Kwong solution, the critical pressure and temperature of the gas must be known. They are not needed for ideal gas solutions.

Values of the Universal Gas Constants

Value of R	Units of R	Units of P	Units of V	Units of T
8.314	N - m/g mole - K	N/m ²	m ³ /g mole	K
83.14	cm ³ - bar/g mole - K	bar	cm ³ /g mole	K
82.05	cm ³ - atm/g mole - K	atm	cm ³ /g mole	K
0.7302	atm - ft ³ /lb mole - °R	atm	ft ³ /lb mole	°R
10.73	psi - ft ³ /lb mole - °R	psi	ft ³ /lb mole	°R
1545	psf - ft ³ /lb mole - °R	psf	ft ³ /lb mole	°R

Critical Temperatures and Pressures

Substance	T _c , K	T _c , °R	P _c , ATM
Ammonia	405.6	730.1	112.5
Argon	151	272	48.0
Carbon dioxide	304.2	547.6	72.9
Carbon monoxide	133	239	34.5
Chlorine	417	751	76.1
Helium	5.3	9.5	2.26
Hydrogen	33.3	59.9	12.8
Nitrogen	126.2	227.2	33.5
Oxygen	154.8	278.6	50.1
Water	647.3	1165.1	218.2
Dichlorodifluoromethane	384.7	692.5	39.6
Dichlorofluoromethane	451.7	813.1	51.0
Ethane	305.5	549.9	48.2
Ethanol	516.3	929.3	63
Methanol	513.2	923.8	78.5
n-Butane	425.2	765.4	37.5
n-Hexane	507.9	914.2	29.9
n-Pentane	469.5	845.1	33.3
n-Octane	568.6	1023.5	24.6
Trichlorofluoromethane	471.2	848.1	43.2

Equations:

Ideal gas:

$$PV = nRT$$

Redlich-Kwong:

$$P = \frac{nRT}{(V - b)} - \frac{a}{T^{1/2} V (V + b)}$$

$$a = 4.934 b nRT_c^{1.5}$$

$$b = 0.0867 \frac{nRT_c}{P_c}$$

where:

P is the absolute pressure;

V is the volume;

n is the number of moles present;

R is the universal gas constant;

T is the absolute temperature;

T_c is the critical temperature;

P_c is the critical pressure.

Remarks:

P, V, n and T must have units compatible with R.

At low temperatures or high pressures, the ideal gas law does not represent the behavior of real gases.

No equation of state is valid for all substances nor over an infinite range of conditions. The Redlich-Kwong equation gives moderate to good accuracy for a variety of substances over a wide range of conditions. Results should be used with caution and tempered by experience.

Solutions for V, n, R and T, using the Redlich-Kwong equation, require an iterative technique. Newton's method is employed using the ideal gas law to generate the initial guess. Iteration time is generally a function of the amount of deviation from ideal gas behavior. For extreme cases, the routine may fail to converge entirely, resulting in an "error".

Registers R₀, R₁ and R_{S0}—R_{S9} are available for user storage.

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
1	Load side 1 and side 2.			
2	Select Redlich-Kwong (1.00) or ideal gas (0.00) using mode toggle.		f A	1.00/0.00
3	If you selected ideal gas in step 2, skip to step 5.			
4	Input critical temperature and critical pressure.	T_c P_c	f B f C	T_c P_c
5	Input four of the following:			
	Absolute pressure	P	A	P
	Volume	V	B	V
	Number of moles	n	C	n
	Universal gas constant	R	D	R
	Absolute temperature	T	E	T
6	Calculate remaining value:			
	Absolute pressure		A	P
	Volume		B	V
	Number of moles		C	n
	Universal gas constant		D	R
	Absolute temperature		E	T
7	For a new case, go to steps 2, 4, or 5 and change values or mode.			

Example 1:

0.63 g moles of air are enclosed in a 25,000 cm³ space at 1200 K. What is the pressure in bars? Assume an ideal gas.

Keystrokes:

Outputs:

Select ideal gas by pressing **f** **A** until 0.00 is displayed.

f **A** **f** **A** →
25000 **B** .63 **C** 83.14 **D**
1200 **E** **A** →

0.00

2.51 (bars)

Example 2:

What is the specific volume (ft^3/lb) of a gas at atmospheric pressure and at a temperature of 513°R ? The molecular weight is 29. Assume an ideal gas.

Keystrokes:

f **A** $\longrightarrow$

513 **E** 29 **1/x** **C** 0.7302

D 1 **A** **B** $\longrightarrow$

Outputs:

0.00

12.92 (ft^3/lb)

What is the density?

1/x $\longrightarrow$

0.08 (lb/ft^3)

What is the density at 1.32 atmospheres and 555°R ?

1.32 **A** 555 **E** **B** **1/x** $\longrightarrow$

0.09 (lb/ft^3)

Example 3:

The specific volume of a gas in a container is $800 \text{ cm}^3/\text{g mole}$. The temperature will reach 400 K. What will the pressure be according to the Redlich-Kwong relation?

$$P_c = 48.2 \text{ atm}$$

$$T_c = 305.5 \text{ K}$$

$$R = 82.05 \text{ cm}^3 - \text{atm}/\text{g mole-K}$$

Keystrokes:

f **A** $\longrightarrow$

305.5 **f** **B** 48.2 **f** **C** 82.05

D 1 **C** 400 **E** 800 **B** **A** $\longrightarrow$

Outputs:

1.00

36.27 (atm)

Example 4:

6 gram moles of carbon dioxide gas are held at a pressure of 50 atmospheres, and at a temperature of 500 K. What is the volume in cubic centimeters? Use the Redlich-Kwong relation.

$$T_c = 304.2 \text{ K}$$

$$P_c = 72.9 \text{ atm}$$

$$R = 82.05 \text{ cm}^3 - \text{atm}/\text{g mole} - \text{K}$$

Keystrokes:

f **A** $\longrightarrow$

72.9 **f** **C** 304.2 **f** **B** 82.05

D 6 **C** 50 **A** 500 **E** **B** $\longrightarrow$

Outputs:

1.00

4695.86 (cm^3)

How many moles could be contained at this temperature and pressure in 5 liters?

5000 **B** **C** $\longrightarrow$

6.39 (g moles)

ISENTROPIC FLOW FOR IDEAL GASES



This card replaces isentropic flow tables for a specified specific heat ratio k . Inputs and outputs are interchangeable with the exception of k .

The following values are correlated:

M is the Mach number;

T/T_0 is the ratio of flow temperature T to stagnation or zero velocity temperature T_0 ;

P/P_0 is the ratio of flow pressure P to stagnation pressure P_0 ;

ρ/ρ_0 is the ratio of flow density ρ to stagnation density ρ_0 ;

A/A^*_{sub} and A/A^*_{sup} are the ratios of flow area A to the throat area A^* in converging—diverging passages. A/A^*_{sub} refers to subsonic flow while A/A^*_{sup} refers to supersonic flow.

Equations:

$$T/T_0 = \frac{2}{2 + (k - 1) M^2}$$

$$P/P_0 = (T/T_0)^{k/(k-1)}$$

$$\rho/\rho_0 = (T/T_0)^{1/(k-1)}$$

$$A/A^* = \frac{1}{M} \left[\left(\frac{2}{k + 1} \right) \left(1 + \frac{k - 1}{2} M^2 \right) \right]^{\frac{k + 1}{2(k - 1)}}$$

In the last equation M^2 is determined using Newton's method. The initial guess used is as follows with a positive exponent for supersonic flow:

$$M_0^2 = (\sqrt{\text{Frac}(A/A^*)} + A/A^*)^{\pm 3}$$

Remarks:

After an input of A/A^* , the program begins to iterate to find M^2 for future use. This iteration will normally take less than one minute, but may take longer on occasion. For extreme values of k (1.4 is optimum) the routine may fail to converge at all. An "Error" message will eventually halt the routine if it goes out of control.

A/A^* values of 1.00 are illegal inputs. Instead, input an M of 1.00.

The calculator uses flag 3 to decide whether to store or calculate a value. If you use the data input keys (setting flag 3) and then wish to calculate a parameter based on a prior input, clear flag 3 before pressing the appropriate user definable keys.

Registers R_0 , R_5 and $R_{80}-R_1$ are available for user storage.

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
1	Load side 1 and side 2.			
2	Input specific heat ratio.	k	f A	k
3	Input one of the following:			
	Mach number	M	A	M
	Temperature ratio	T/T_0	B	M
	Pressure ratio	P/P_0	C	M
	Density ratio	ρ/ρ_0	D	M
	Subsonic area ratio	A/A^*_{sub}	E	M
	Supersonic area ratio	A/A^*_{sup}	f E	M
4	Calculate one of the following:			
	Mach number		A	M
	Temperature ratio		B	T/T_0
	Pressure ratio		C	P/P_0
	Density ratio		D	ρ/ρ_0
	Area ratio (subsonic or supersonic)		E	A/A^*
4'	Calculate and output all values automatically.		f B	$k, M, T/T_0, P/P_0, \rho/\rho_0, A/A^*$
5	For another calculation based on same input, go to step 4 (or 4'). For a new input, go to step 3. For a new specific heat ratio, go to step 2.			

Example 1:

A pilot is flying at Mach 0.93 and reads on air temperature of 15 degrees Celsius (288 K) on a thermometer that reads stagnation temperature T_0 . What is the true temperature assuming that $k = 1.38$?

Keystrokes:

1.38 **f** **A** →
 .93 **A** →
B →
 288 **x** →
 273 **-** →

Outputs:

1.380
 0.930
 0.859 (T/T_0)
 247.352 (T , K)
 -25.648 (T , °C)

If the same pilot reads a stagnation pressure P_0 of 700 millimeters of mercury, what is the true air pressure?

(Since the data input flag was set when 288 was keyed in, we must either clear it, or input 0.93 again.)

.93 **A** **C** →
 700 **x** →

0.575 (P/P_0)
 402.843 (mm Hg)

Example 2:

A converging, diverging passage has supersonic flow in the diverging section. At an area ratio A/A^* of 1.60, what are the isentropic flow ratios for temperature, pressure and density? What is the Mach number? $k = 1.74$.

Keystrokes:

1.74 **f** **A** →
 1.60 **f** **E** →
B →
C →
D →

Outputs:

1.740
 2.105 (M)
 0.379 (T/T_0)
 0.102 (P/P_0)
 0.269 (ρ/ρ_0)

or, alternatively, using automatic output.

f **B** →

1.740 *** (k)
 2.105 *** (M)
 0.379 *** (T/T_0)
 0.102 *** (P/P_0)
 0.269 *** (ρ/ρ_0)
 1.600 *** (A/A^*)

Notes

CONDUIT FLOW



This program solves for the average velocity, or the pressure drop for viscous, incompressible flow in conduits.

Equations:

$$v^2 = \frac{\Delta P / \rho}{2 \left(f \frac{L}{D} + \frac{K_T}{4} \right)}$$

For laminar flow ($Re < 2300$)

$$f = 16/Re$$

For turbulent flow ($Re > 2300$)

$$\frac{1}{\sqrt{f}} = 1.737 \ln \frac{D}{\epsilon} + 2.28 - 1.737 \ln \left(4.67 \frac{D}{\epsilon Re \sqrt{f}} + 1 \right)$$

is solved by Newton's method.

$$\frac{1}{\sqrt{f_0}} = 1.737 \ln \frac{D}{\epsilon} + 2.28$$

is used as an initial guess in the iteration.

where:

Re is the Reynolds number, defined as $\rho Dv/\mu$;

D is the pipe diameter;

ϵ is the dimension of irregularities in the conduit surface (see table 2);

f is the Fanning friction factor for conduit flow;

ΔP is the pressure drop along the conduit;

ρ is the density of the fluid;

μ is the viscosity of the fluid;

ν is the kinematic viscosity of the fluid;

L is the conduit length;

v is the average fluid velocity;

K_T is the total of the applicable fitting coefficients in table 1.



Table 1
Fitting Coefficients

Fitting	K
Globe valve, wide open	7.5—10
Angle valve, wide open	3.8
Gate valve, wide open	0.15—0.19
Gate valve, $\frac{3}{4}$ open	0.85
Gate valve, $\frac{1}{2}$ open	4.4
Gate valve, $\frac{1}{4}$ open	20
90° elbow	0.4—0.9
Standard 45° elbow	0.35—0.42
Tee, through side outlet	1.5
Tee, straight through	.4
180° bend	1.6
Entrance to circular pipe	0.25—0.50
Sudden expansion	$(1 - A_{up}/A_{dn})^{2*}$
Acceleration from $v = 0$ to $v = v_{entrance}$	1.0

* A_{up} is the upstream area and A_{dn} is the downstream area.

Table 2
Surface Irregularities

Material	ϵ (feet)	ϵ (meters)
Drawn or Smooth Tubing	5.0×10^{-6}	1.5×10^{-6}
Commercial Steel or Wrought Iron	1.5×10^{-4}	4.6×10^{-5}
Asphalted Cast Iron	4.0×10^{-4}	1.2×10^{-4}
Galvanized Iron	5.0×10^{-4}	1.5×10^{-4}
Cast Iron	8.3×10^{-4}	2.5×10^{-4}
Wood Stave	6.0×10^{-4} to 3.0×10^{-3}	1.8×10^{-4} to 9.1×10^{-4}
Concrete	1.0×10^{-3} to 1.0×10^{-2}	3.0×10^{-4} to 3.0×10^{-3}
Riveted Steel	3.0×10^{-3} to 3.0×10^{-2}	9.1×10^{-4} to 9.1×10^{-3}

Reference:

Welty, Wicks, Wilson; *Fundamentals of Momentum, Heat and Mass Transfer*, John Wiley and Sons, Inc., 1969.

Remarks:

The correlation gives meaningless results in the region $2300 < Re < 4000$.

The solution requires an iterative procedure. The time for solution will range from 10 seconds for ΔP , to several minutes for v . The display setting is used to determine when the solution for v is adequately accurate. Time for solution of v is roughly proportional to the number or significant digits in the display setting.

If the conduit is not circular, an equivalent diameter may be calculated using the formula below:

$$D_{eq} = 4 \frac{\text{cross sectional area}}{\text{wetted perimeter}}$$

Unitary consistency must be maintained with the exception of the pressure drop ΔP . If all length units are feet, time is measured in seconds and mass is given in pounds, pressure may be input or output in pounds per square inch, using the **f** **E** keys.

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
1	Load side 1 and side 2.			
2	Input the following in any order			
	(units must be consistent):			
	Viscosity of fluid	μ	f A	
	or			
	Kinematic viscosity of fluid	ν	f B	ν
	Density	ρ	f C	ρ
	Surface irregularity	ϵ	f D	ϵ
	Length of conduit	L	A	L
	Equivalent diameter of			
	passage	D	B	D
	Total fitting coefficient	K_T	C	$K_T/4$
3	Input one of the following:			
	Fluid velocity	v	D	v
	Pressure drop in compatible			
	units	ΔP	E	ΔP
	or			
	Pressure drop in psi	$\Delta P(\text{psi})$	f E	144g ΔP

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
4	Calculate one of the following:			
	Fluid velocity		D	v
	Pressure drop in compatible			
	units		E	ΔP
	or			
	Pressure drop in psi		f E	$\Delta P(\text{psi})$
5	Optional: After calculation of			
	ΔP or v , display Reynolds			
	number		R+	Re
	and Fanning friction factor.		R+	f
6	For a new case, go to step 2 or			
	step 3 and change appropriate			
	inputs.			

Example 1:

A heat exchanger has 20, 3 meter tube passes (60 m of pipe) with 180 degree bends connecting each pair of tubes (from table 1, $K_T = 10 \times 1.6$). The fluid is water ($\nu = 9.3 \times 10^{-7} \text{ m}^2/\text{s}$, $\rho = 10^3 \text{ kg/m}^3$). The surface roughness is $3 \times 10^{-4} \text{ m}$ and the diameter is $2.54 \times 10^{-2} \text{ m}$. If the fluid velocity is 3.05 m/s, what is the pressure loss? What is the Reynolds number? What is the Fanning friction factor?

Keystrokes:

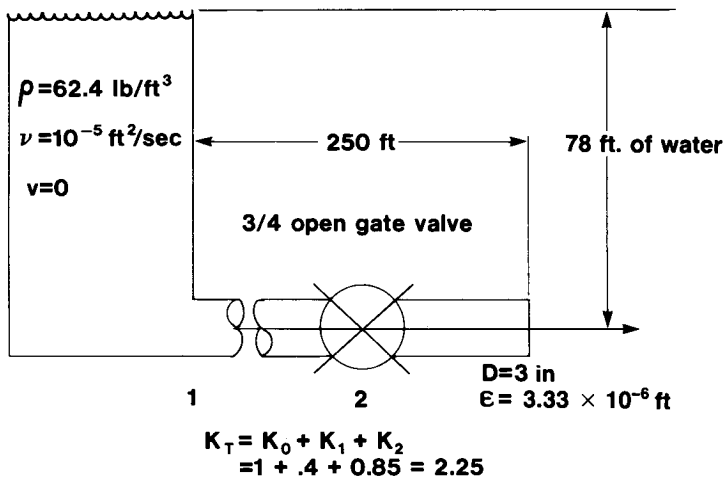
9.3 **EEX** **CHS** 7 **f** **B** **EEX** 3
f **C** 3 **EEX** **CHS** 4 **f** **D** 60
A 2.54 **EEX** **CHS** 2 **B** 16 **C**
3.05 **D** **E** $\longrightarrow$
R+ $\longrightarrow$
R+ $\longrightarrow$

Outputs:

522. 03 ($\Delta P, \text{N/m}^2$)
83.3 03 (Re)
10.2-03 (f)

Example 2:

For the system shown, what is the volume flow rate?



Keystrokes:

Outputs:

First calculate and store ΔP in psi from the given data.

78 **ENTER** 62.4 **×** 144 **÷**
f **E** $\longrightarrow$ 33,8 00 (ΔP , psi)

Now store the other values.

EEX **CHS** 5 **f** **B** 62.4 **f**
C 3.33 **EEX** **CHS** 6 **f** **D** 250
A 3 **ENTER** 12 **÷** **B** 2.25
C **D** $\longrightarrow$ 17.8 00 (v , ft/sec)

Calculate volume flow rate ($v \times \text{Area}$).

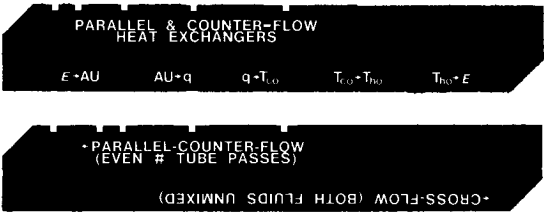
1.5 **ENTER** 12 **÷** **ENTER**
× **π** **×** **×** $\longrightarrow$ 873.-03 (ft^3/sec)

What will the height of the water be when the velocity is 15 ft/sec?

15 **D** **f** **E** $\longrightarrow$ 24.7 00 (ΔP , psi)
144 **×** 62.4 **÷** $\longrightarrow$ 57.0 00 (ft)

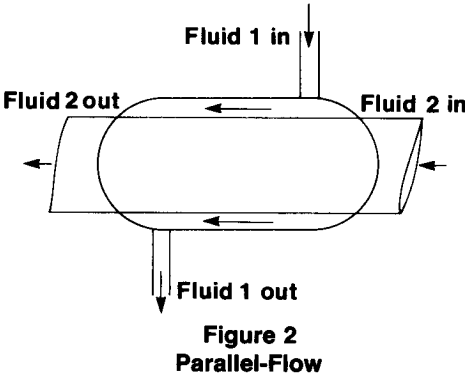
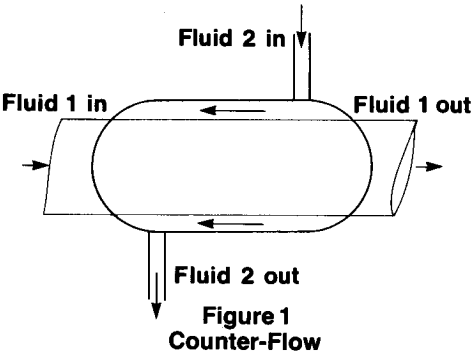
Notes

PARALLEL & COUNTER FLOW HEAT EXCHANGERS

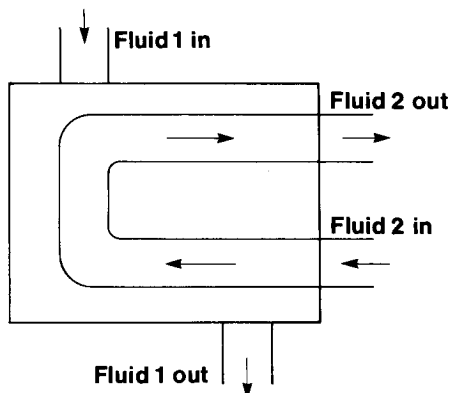


This two card set allows analysis of counter-flow, parallel-flow, parallel-counter flow, and cross-flow (both fluids unmixed) heat exchanges.

The program is organized in four segments. The first side of card 1 performs heat balance calculations and acts as controller for the three slave program segments. Slave program segment one, on side 2 of card 1, is applicable to parallel-flow and counter-flow heat exchanges. Counter-flow is selected by pressing **f** **E** until 1.00 appears. Parallel-flow is selected by pressing **f** **E** until 0.00 appears.

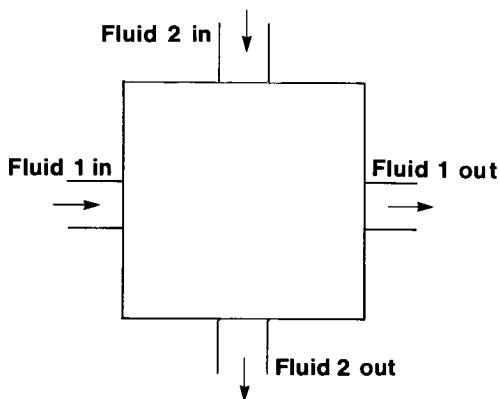


The slave segment for **parallel-counter-flow** configuration (with an even number of tube passes) is on side 1 of card 2.



**Figure 3 Parallel-Counter-Flow
(Even Number Of Tube Passes)**

The slave segment for **cross-flow** (with both fluids unmixed) is on side 2 of card 2.



**Figure 4 Cross Flow
(Both Fluids Unmixed)**

Equations:

Heat exchanger effectiveness E is the ratio of actual heat transfer to maximum possible heat transfer.

$$E = \frac{q}{C_{\min} (T_{\text{hin}} - T_{\text{cin}})} = \frac{C_h (T_{\text{hin}} - T_{\text{ho}})}{C_{\min} (T_{\text{hin}} - T_{\text{cin}})} = \frac{C_c (T_{\text{co}} - T_{\text{cin}})}{C_{\min} (T_{\text{hin}} - T_{\text{cin}})}$$

where:

q is the actual heat transfer;

T_{hin} and T_{cin} are the inlet temperatures of the hot and cold fluids, respectively;

T_{ho} and T_{co} are the outlet temperatures of the hot and cold fluids, respectively;

C_h and C_c are the heat capacities of the hot and cold fluids, respectively, e.g., $C_h = m_h \times c_{ph}$, where m_h is the flow rate and c_{ph} is the specific heat capacity of the hot fluid;

C_{min} and C_{max} (which are used later) are the smaller and larger values of C_h and C_c .

Effectiveness can be related to the product of the surface area of an exchanger and the overall transfer coefficient for specific geometries. This product is designated AU. The geometries considered in this pac have the following correlations:

Counter-Flow (See figure 1)

$$E = \frac{1 - e^{-\frac{AU}{C_{min}} \left(1 - \frac{C_{min}}{C_{max}}\right)}}{1 - (C_{min}/C_{max}) e^{-\frac{AU}{C_{min}} \left(1 - \frac{C_{min}}{C_{max}}\right)}}$$

For $C_{min}/C_{max} = 1$

$$E = \frac{AU/C_{min}}{1 + AU/C_{min}}$$

Parallel-Flow (See figure 2)

$$E = \frac{1 - e^{-\frac{AU}{C_{min}} (1 + C_{min}/C_{max})}}{1 + C_{min}/C_{max}}$$

For $C_{min}/C_{max} = 0$, C_{min} is set to 1.

Parallel-Counter-Flow; Shell Mixed with an Even Number of Tube Passes (See figure 3)

$$E = \frac{2}{\left(1 + \frac{C_{min}}{C_{max}}\right) + \sqrt{1 + \left(\frac{C_{min}}{C_{max}}\right)^2} \left[\frac{1 + e^{-x}}{1 - e^{-x}}\right]}$$

where:

$$x = \frac{AU}{C_{min}} \sqrt{1 + \left(\frac{C_{min}}{C_{max}}\right)^2}$$

Cross-Flow; Both Fluids Unmixed (See figure 4)

No exact expression exists for this case, but the following is a very good approximation. Note that it cannot be stated explicitly in terms of AU and thus requires an iterative solution.

$$E = 1 - e \left(e^{\left(-\frac{AU}{C_{\min}} \frac{C_{\min}}{C_{\max}} y \right)} - 1 \right) \left(\frac{C_{\max}}{C_{\min}} \frac{1}{y} \right)$$

where:

$$y = \left[\frac{C_{\min}}{AU} \right]^{0.22}$$

References:

W.M. Kays and A.L. London, *Compact Heat Exchangers*, National Press, 1955.

Eckert and Drake, *Heat and Mass Transfer*, McGraw-Hill.

Remarks:

Registers R_{S0} - R_{S9} , R_C , R_E , and R_I are available for user storage.

Solution for AU, using the cross-flow slave card takes significantly longer than other solutions because of the iterative technique required.

You should always solve for all values (AU, q, T_{co} , T_{ho} and E). It is quite possible for the heat balance equations to yield meaningless solutions for a particular type of heat exchange. By calculating all results, you are assured that the configuration being used is capable of the performance specified. An error message during calculation of AU or q usually indicates a violation of the second law of thermodynamics.

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
1	Load side 1 of card 1.			
2	Select proper configuration			
	card and side, and load:			
	a. Parallel or counter-flow			
	exchangers → card 1,			
	side 2.			
	b. Parallel-counter-flow			
	(even number of tube			
	passes) → card 2, side 1.			
	c. Cross-flow (both fluids			
	unmixed → card 2, side 2.			

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
3	If display says "Crđ" press CLX		CLX	0.00
4	If you loaded parallel/ counter-flow configurations in step 2, select counter flow (1) or parallel-flow (0) using mode toggle.		1 E	1.00/0.00
5	Input the following values			
	Cold fluid inlet temperature	T_{cin}	1 A	T_{cin}
	Cold fluid density flow rate	$\dot{m}_c$	ENTER	m_c
	<i>then</i>			
	Cold fluid heat capacity	C_{pc}	1 B	C_c
	<i>and</i>			
	Hot fluid inlet temperature	T_{hin}	1 C	T_{hin}
	Hot fluid density flow rate	$\dot{m}_h$	ENTER	m_h
	<i>then</i>			
	Hot fluid heat capacity	C_{ph}	1 D	C_h
6	If the remaining known is effectiveness, go to step 7. If area-conductance product, go to step 8. If heat transfer, go to step 9. If cold fluid outlet temperature, go to step 10. If hot fluid outlet temperature, go to step 11.			
7	With effectiveness displayed, calculate area-conductance product.	E	A	AU
8	With area-conductance product displayed, calculate heat transfer.	AU	B	q

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
9	With heat transfer displayed,			
	calculate cold fluid outlet			
	temperature.	q	C	T_{co}
10	With cold fluid outlet			
	temperature displayed,			
	calculate hot fluid outlet			
	temperature.	T_{co}	D	T_{ho}
11	With hot fluid outlet tempera-			
	ture displayed, calculate			
	effectiveness.	T_{ho}	E	E
12	Go back to step 6 and com-			
	plete calculation of all outputs.			
13	For a new configuration, go to			
	step 2. It is not necessary to			
	repeat the input process if			
	values remain unchanged.			
14	For new input values, go to			
	step 5 and change appropriate			
	variables.			

Example 1:

Water ($c_p = 1 \text{ Btu/lb-}^\circ\text{F}$) is used to cool an oil ($c_p = .53 \text{ Btu/lb-}^\circ\text{F}$) from 200°F to 110°F . The water flow rate is 20,000 pounds per hour while the oil flows at 37,000 pounds per hour. If the water inlet temperature is 55°F and U is $25 \text{ Btu/ft}^2\text{-hr-}^\circ\text{F}$ for the heat exchangers being considered, what are the area requirements for counter-flow, parallel-flow, parallel-counter-flow and cross-flow?

Knowns:

$$c_{pc} = 1.0 \text{ Btu/lb-}^\circ\text{F}$$

$$\dot{m}_c = 20,000 \text{ lb/hr}$$

$$c_{ph} = 0.53 \text{ Btu/lb-}^\circ\text{F}$$

$$\dot{m}_h = 37,000 \text{ lb/hr}$$

$$T_{cin} = 55^\circ\text{F}$$

$T_{hin} = 200^{\circ}\text{F}$
 $T_{ho} = 110^{\circ}\text{F}$
 $U = 25 \text{ Btu/ft}^2\text{-hr-}^{\circ}\text{F}$

Keystrokes:

Outputs:

Load side 1 and side 2 of card 1 and select counter-flow mode.

55 **f** **A** 20000 **ENTER** 1
f **B** 200 **f** **C** 37000 **ENTER**
.53 **f** **D** **f** **E** →

1.00 (Counter-flow mode on)

110 **E** →

0.62 (Effectiveness)

Since effectiveness is the same for all configurations, store it for later use.

STO **I** →

0.62

Calculate AU.

A →
25 **÷** →

31587.76 (AU)
1263.51 (ft²)

Switch to parallel configuration.

f **E** →
RCL **I** →
A →

0.00 (parallel selected)
0.62
Error (Violation of second law)

CL x →

-0.23

Load parallel-counter flow configuration on side 1 of card 2 and clear display of "Crd."

CL x →
RCL **I** **A** →

-0.23
Error (Violation of second law)

CL x →

-0.06

Load cross-flow configuration on side 2 of card 2 and clear display of "Crd".

CL x **RCL** **I** **A** →
25 **÷** →

39383.22 (AU)
1575.33 (ft²)

(Do not alter storage registers if you intend to continue with example 2.)

Example 2:

If a counter flow exchanger with an area of 1000 ft² and an overall heat transfer coefficient of 27 Btu/ft²-hr-°F is available, how close will the outlet temperature of the oil be to 110°F? What will the total heat transfer and outlet water temperature be? All unspecified values remain the same as example 1.

Keystrokes:**Outputs:**

Load counter-flow routine on side 2 of card 1 and select counter flow mode.

CLX **f** **E** →

1.00

Calculate AU product and calculate q.

27 **ENTER** 1000 **x** →

27000.00 (AU)

B →

1656452.69 (q, Btu/hr)

C →

137.82 (T_{co})

D →

115.53 (T_{ho})

E →

0.58 (E)

Notes



PROGRAM LISTINGS

The following listings are included for your reference. A table of keycodes and keystrokes corresponding to the symbols used in the listings can be found in Appendix E of your Owner's Handbook.

Program	Page
1. Vector Statics	L01-01
2. Section Properties	L02-01
Card 1	
Card 2	
3. Stress on an Element	L03-01
4. Soderberg's Equation for Fatigue	L04-01
5. Cantilever Beams	L05-01
6. Simply Supported Beams	L06-01
7. Beams Fixed at Both Ends	L07-01
8. Propped Cantilever Beams	L08-01
9. Helical Spring Design	L09-01
10. Four Bar Function Generator	L10-01
Card 1	
Card 2	
11. Progression of Four-Bar System	L11-01
12. Progression of Slider Crank	L12-01
13. Circular Cams	L13-01
14. Linear Cams	L14-01
15. Gear Forces	L15-01
16. Standard External Involute Spur Gears	L16-01
17. Belt Length	L17-01
18. Free Vibrations	L18-01
19. Vibration Forced by $F_0 \cos \omega t$	L19-01
20. Equations of State	L20-01
21. Isentropic Flow for Ideal Gases	L21-01
22. Conduit Flow	L22-01
23. Heat Exchangers	L23-01
Card 1	
Card 2	

Appendix A

MAGNETIC CARD

SYMBOLS AND CONVENTIONS

SYMBOL OR CONVENTION	INDICATED MEANING
White mnemonic: x A	White mnemonics are associated with the user-definable key they are above when the card is inserted in the calculator's window slot. In this case the value of x could be input by keying it in and pressing A .
Gold mnemonic: y x f E x↑y A	Gold mnemonics are similar to white mnemonics except that the gold f key must be pressed before the user-definable key. In this case y could be input by pressing f E . ↑ is the symbol for ENTER . In this case ENTER is used to separate the input variables x and y. To input both x and y you would key in x, press ENTER , key in y and press A .
X A	The box around the variable x indicates input by pressing STO A .
(x) A	Parentheses indicate an option. In this case, x is not a required input but could be input in special cases.
→x A	→ is the symbol for calculate. This indicates that you may calculate x by pressing key A .
→x, y, z A	This indicates that x, y, and z are calculated by pressing A once. The values would be printed in x, y, z order.
→x; y; z A	The semi-colons indicate that after x has been calculated using A , y and z may be calculated by pressing R/S .
→“x,” y A	The quote marks indicate that the x value will be “paused” or held in the display for one second. The pause will be followed by the display of y.
↔ x A	The two-way arrow ↔ indicates that x may be either output or input when the associated user-definable key is pressed. If numeric keys have been pressed between user-definable keys, x is stored. If numeric keys have not been pressed, the program will calculate x.

P? A	The question mark indicates that this is a mode setting, while the mnemonic indicates the type of mode being set. In this case a print mode is controlled. Mode settings typically have a 1.00 or 0.00 indicator displayed after they are executed. If 1.00 is displayed, the mode is on. If 0.00 is displayed, it is off.
START A	The word START is an example of a command. The start function should be performed to begin or start a program. It is included when initialization is necessary.
DEL A	This special command indicates that the last value or set of values input may be deleted by pressing A.

VECTOR STATICS

TITLE _____

001 *LELA	Convert from polar to rectangular.	7 RCLB	
002 XZY		058 RCLD	
003 +R		059 x	
004 XZY		060 +	
005 *LBLa	Store x, y components of $\vec{V}_1$.	061 STOE	
006 STOB		062 PRTX	
007 XZY		063 RTN	
008 STOA		064 RCLC	
009 XZY		065 RCLA	
010 RTN		066 RCLB	
011 *LBLb	Convert from polar to rectangular.	067 +P	
012 XZY		068 XZY	Calculate angle between vectors.
013 +R		069 CLX	
014 XZY		070 RCLC	
015 *LBLb		071 RCLD	
016 STOD	Store x, y components of $\vec{V}_2$.	072 +P	
017 XZY		073 XZY	
018 STOC		074 R4	
019 XZY		075 x	
020 RTN		076 +	
021 *LBLd		077 COS ⁻¹	
022 XZY	Store F cos ϕ and F sin ϕ .	078 RCLC	
023 +R		079 XZY	
024 STOS		080 PRTX	
025 XZY		081 RTN	
026 STOS		082 *LBLc	
027 RTN		083 SPC	
028 *LBLC		084 RCLB	
029 SPC	$\vec{V}_1 + \vec{V}_2$	085 RCLA	
030 RCLD		086 +P	Calculate R_1 .
031 RCLB		087 CLX	
032 +		088 1	
033 RCLA		089 +R	
034 RCLC		090 STOA	
035 +		091 XZY	
036 +P		092 STOS	
037 PRTX		093 RCLD	
038 XZY		094 RCLC	
039 PRTX		095 +P	
040 RTN		096 CLX	
041 *LBLD		097 1	
042 SPC	$\vec{V}_1 \times \vec{V}_2$	098 +R	
043 RCLA		099 STOB	
044 RCLD		100 XZY	
045 x		101 STOT	
046 RCLC		102 R4	
047 RCLB		103 x	
048 x		104 R4	
049 -		105 x	
050 PRTX		106 R4	
051 RTN		107 -	
052 *LBLc	$\vec{V}_1 \cdot \vec{V}_2$	108 STOE	
053 SPC		109 RCL8	
054 RCLA		110 RCL7	
055 RCLC		111 x	
056 x		112 RCL9	

REGISTERS									
0	1	2	3	4 cos θ_1	5 sin θ_1	6 cos θ_2	7 sin θ_2	8 F cos ϕ	9 F sin ϕ
S0	S1	S2	S3	S4	S5	S6	S7	S8	S9
A	B	C	D	E	F	G	H	I	J
x ₁	y ₁	x ₂	y ₂	used					

VECTOR STATICS

TITLE _____

001 *LELA	Convert from polar to rectangular.	7 RCLB	
002 XZY		058 RCLD	
003 +R		059 x	
004 XZY		060 +	
005 *LBLa	Store x, y components of $\vec{V}_1$.	061 STOE	
006 STOB		062 PRTX	
007 XZY		063 RTN	
008 STOA		064 RCLC	
009 XZY		065 RCLA	
010 RTN		066 RCLB	
011 *LBLb	Convert from polar to rectangular.	067 +P	
012 XZY		068 XZY	Calculate angle between vectors.
013 +R		069 CLX	
014 XZY		070 RCLC	
015 *LBLb		071 RCLD	
016 STOD	Store x, y components of $\vec{V}_2$.	072 +P	
017 XZY		073 XZY	
018 STOC		074 R4	
019 XZY		075 x	
020 RTN		076 ÷	
021 *LBLd		077 COS ⁻¹	
022 XZY	Store F cos ϕ and F sin ϕ .	078 RCLC	
023 +R		079 XZY	
024 STOS		080 PRTX	
025 XZY		081 RTN	
026 STOS		082 *LBLc	
027 RTN		083 SPC	
028 *LBLC		084 RCLB	
029 SPC	$\vec{V}_1 + \vec{V}_2$	085 RCLA	
030 RCLD		086 +P	Calculate R_1 .
031 RCLB		087 CLX	
032 +		088 1	
033 RCLA		089 +R	
034 RCLC		090 STOD	
035 +		091 XZY	
036 +P		092 STOS	
037 PRTX		093 RCLD	
038 XZY		094 RCLC	
039 PRTX		095 +P	
040 RTN		096 CLX	
041 *LBLD		097 1	
042 SPC	$\vec{V}_1 \times \vec{V}_2$	098 +R	
043 RCLA		099 STOE	
044 RCLD		100 XZY	
045 x		101 STOD	
046 RCLC		102 R4	
047 RCLB		103 x	
048 x		104 R4	
049 -		105 x	
050 PRTX		106 R4	
051 RTN		107 -	
052 *LBLc	$\vec{V}_1 \cdot \vec{V}_2$	108 STOE	
053 SPC		109 RCLB	
054 RCLA		110 RCL7	
055 RCLC		111 x	
056 x		112 RCL9	

REGISTERS									
0	1	2	3	4 cos θ_1	5 sin θ_1	6 cos θ_2	7 sin θ_2	8 F cos ϕ	9 F sin ϕ
S0	S1	S2	S3	S4	S5	S6	S7	S8	S9
A	B	C	D	E	F	G	H	I	J
x ₁	y ₁	x ₂	y ₂	used					

DATE _____ AUTHOR _____

113 RCL6 114 x 115 - 116 RCLE 117 ÷ 118 PRTX 119 RCL9 120 RCL4 121 x 122 RCL8 123 RCL5 124 x 125 - 126 RCLE 127 ÷ 128 PRTX 129 RTN	----- Calculate R ₃ . -----		
--	--	--	--

LABELS					FLAGS	SET STATUS		
A	B	C	D	E	F	FLAGS		DISP
$r_1 \theta_1$	$r_2 \theta_2$	$C \rightarrow \vec{V}_1 + \vec{V}_2$	$D \rightarrow \vec{V}_1 \times \vec{V}_2$	$E \rightarrow V_1 \cdot V_2; \gamma$	0	ON	OFF	
a	$x_1 y_1$	$x_2 y_2$	c	$d F \theta$	$e \rightarrow R_1; R_2$	1		
0	1	2	3	4	2			
5	6	7	8	9	3			

DEG	☒
GRAD	☐
RAD	☐

FIX	☒
SCI	☐
ENG	☐

n 2

SECTION PROPERTIES

TITLE _____

001 #LBL a	Clear registers.	057 ST-1	Sum ΔI_{xy} .
002 CLRG		058 RCLC	
003 RTN	-----	059 RCLB	
004 #LBL a	Store coordinates.	060 x	
005 STOD		061 RCLA	
006 R†		062 RCLD	
007 STOA		063 x	
008 R†		064 -	
009 STOB		065 ENT1	
010 R†	-----	066 ENT1	
011 STOC	Sum ΔA .	067 4	
012 RCLA		068 ÷	
013 +		069 RCLB	
014 STC8		070 x	
015 RCLD		071 RCLA	
016 RCLB		072 RCLC	
017 -		073 x	
018 STO7		074 RCLC	
019 x		075 X²	
020 2		076 STOS	
021 ÷	-----	077 +	
022 ST-0	Sum ΔI_y .	078 RCLA	
023 1		079 X²	
024 2		080 ST+S	
025 ÷		081 +	
026 RCLC		082 RCL7	
027 RCLA		083 x	
028 -		084 3	
029 STO6		085 ÷	
030 X²		086 +	
031 RCLB	-----	087 x	
032 GSB4	Sum ΔI_x .	088 RCL9	
033 ST-4		089 8	
034 RCL6		090 ÷	
035 RCLB		091 RCL9	
036 RCLD		092 x	
037 +		093 RCL7	
038 STOS		094 X²	
039 x		095 x	
040 2		096 +	
041 4		097 RCL6	
042 ÷		098 X#0?	
043 RCL9		099 ÷	
044 X²		100 ST+5	
045 RCL7		101 RCLC	Recall x_i and y_i for next
046 GSB4	-----	102 RCLD	segment.
047 ST+3	Sum ΔM_x .	103 RTN	-----
048 RCL6		104 #LBL 1	Calculate ΔM_x and ΔM_y .
049 RCL9		105 X²	
050 RCL7		106 3	
051 GSB1		107 ÷	
052 ST+2	-----	108 XZV	
053 RCL7	Sum ΔM_y .	109 GSB4	
054 RCL8		110 8	
055 RCL6		111 ÷	
056 GSB1		112 RTN	-----

REGISTERS									
0 ΣA	1 ΣM_y	2 ΣM_x	3 ΣI_x	4 ΣI_y	5 ΣI_{xy}	6 $(x_{H+1} - x_i)$	7 $(y_{H+1} - y_i)$	8 $(x_{H+1} + x_i)$	9 $(y_{H+1} + y_i)$
S0	S1	S2	S3	S4	S5	S6	S7	S8	S9
A x_i	B y_i	C x_{H+1}		D y_{H+1}		E	I		

DATE _____ AUTHOR _____

113	*LBL4	Calculation subroutine. ----- Add to sums for circular regions.			
114	X ²				
115	+				
116	x				
117	RTN				
118	*LBLC				
119	ENT↑				
120	ABS				
121	x				
122	Pi				
123	x				
124	4				
125	÷				
126	STOA				
127	ST+0				
128	ENT↑				
129	ABS				
130	x				
131	Pi				
132	÷				
133	4				
134	÷				
135	STOB				
136	R↓				
137	STOC				
138	R↓				
139	STOD				
140	R↑				
141	x				
142	RCLA				
143	x				
144	ST+5				
145	RCLB				
146	RCLA				
147	RCLC				
148	X ²				
149	x				
150	+				
151	ST+3				
152	RCLB				
153	RCLA				
154	RCLD				
155	X ²				
156	x				
157	+				
158	ST+4				
159	RCLA				
160	RCLD				
161	x				
162	ST+1				
163	RCLA				
164	RCLC				
165	x				
166	ST+2				
167	CLX				
168	RTN				

LABELS					FLAGS	SET STATUS			
A	B	C	D	E	0	FLAGS		TRIG	DISP
x _{H+1} ↑ y _{H+1}		x ↑ y ↑ ± d				ON	OFF		
a	b	c	d	e	1	0	☐	DEG ☒	FIX ☒
0	1 Calculate	2	3	4 Calculate	2	1	☐	GRAD ☐	SCI ☐
5	6	7	8	9	3	2	☐	RAD ☐	ENG ☐
						3	☐		n <u>2</u>

(Card 2)

TITLE _____

001 *LBLA	Output $\bar{x}$, $\bar{y}$ and A.	057 RCLA	
002 GSB2		058 X^2	
003 PRTX		059 RCL0	
004 X^2Y		060 x	
005 PRTX		061 CHS	
006 RCL0		062 RCL3	
007 PRTX		063 $+$	
008 RTN		064 STOC	
009 *LBL2	Calculate $\bar{x}$ and $\bar{y}$.	065 $-$	
010 SPC		066 $X \neq 0$	
011 RCL2		067 $\div$	
012 RCL0		068 TAN $^{-1}$	
013 $\div$		069 RTN	
014 STOA		070 *LBLD	Calculate $I\bar{x}$, $I\bar{y}$, $I\bar{x}\bar{y}$ and output ϕ .
015 RCL1		071 GSB3	
016 RCL0		072 STOI	
017 $\div$		073 2	
018 STOB		074 $\div$	
019 RTN		075 PRTX	
020 *LBL5	Output Ix , Iy and Ixy .	076 *LBL6	Rotate to principal axis values.
021 SPC		077 1	
022 RCL3		078 $+F$	
023 PRTX		079 X^2	
024 RCL4		080 STOA	
025 PRTX		081 RCLC	
026 RCL5		082 x	
027 PRTX		083 X^2Y	
028 RTN		084 X^2	
029 *LBLC	Calculate $I\bar{x}$, $I\bar{y}$ and $I\bar{x}\bar{y}$ and ϕ .	085 STOB	
030 GSB3		086 RCLD	
031 RCLC		087 x	
032 PRTX		088 $+$	
033 RCLD		089 RCL1	
034 PRTX		090 SIN	
035 RCL5		091 RCL5	
036 PRTX		092 x	
037 RTN		093 $-$	
038 *LBL3		094 PRTX	
039 GSB2		095 LSTX	
040 RCL5		096 RCLA	
041 RCL0		097 RCLD	
042 RCLA		098 x	
043 RCL5		099 $+$	
044 x		100 RCLB	
045 x		101 RCLC	
046 $-$		102 x	
047 STOE		103 $+$	
048 ENT †		104 PRTX	
049 $+$		105 RTN	
050 RCL4		106 *LBLJ	Calculate Ix' , Iy' , J and Ixy' .
051 RCLB		107 ENT †	
052 X^2		108 $+$	
053 RCL0		109 STOI	
054 x		110 $F4$	
055 $-$		111 STOC	
056 STOD		112 $R4$	

REGISTERS

0 ΣA	1 ΣM_y	2 ΣM_x	3 ΣI_x	4 ΣI_y	5 ΣI_{xy}	6 $(x_{i+1} - x_i)$	7 $(y_{i+1} - y_i)$	8 $(x_{i+1} + x_i)$	9 $(y_{i+1} + y_i)$
S0	S1	S2	S3	S4	S5	S6	S7	S8	S9
A $x_i, \bar{y}, \cos^2 \phi$	B $y_i, \bar{x}, \sin^2 \phi$	C $x_{i+1}, I\bar{y}$	D $y_{i+1}, I\bar{x}$	E $I\bar{x}\bar{y}$	F 2ϕ				

DATE _____ AUTHOR _____

113	STOD	169	RCLI
114	GSB2	170	SIN
115	x	171	x
116	RCL0	172	RCL0
117	x	173	RCLI
118	CHS	174	COS
119	RCL5	175	x
120	+	176	+
121	RCLD	177	PRTX
122	RCL0	178	RTN
123	-		
124	RCLC		
125	RCLA		
126	-		
127	x		
128	RCL0		
129	x		
130	+		
131	STOE		
132	RCLC		
133	X ²		
134	RCLC		
135	RCLA		
136	x		
137	2		
138	x		
139	-		
140	RCL0		
141	x		
142	RCL3		
143	+		
144	STOC		
145	RCLC		
146	X ²		
147	RCLD		
148	RCL0		
149	x		
150	2		
151	x		
152	-		
153	RCL0		
154	x		
155	RCL4		
156	+		
157	STOD		
158	RCLI		
159	2		
160	÷		
161	GSB6		
162	+		
163	PRTX		
164	RCLC		
165	RCLD		
166	-		
167	2		
168	÷		

LABELS					FLAGS	SET STATUS		
A →x, y, φ	B →Ix, Iy, Ixy	C →IX, IY, IXY	D →IXφ, IYφ, IXYφ	E		FLAGS	TRIG	DISP
a	b	c	d →Ix', Iy', Ixy'	e	0	ON OFF		
0	1 tan ⁻¹	2 x, y	3 Ix, Iy, Ixy	4	1	0 ☐ ☒	DEG ☒	FIX ☒
5	6 Rotate	7	8	9	2	1 ☐ ☒	GRAD ☐	SCI ☐
					3	2 ☐ ☒	RAD ☐	ENG ☐
						3 ☐ ☒		n 2

STRESS ON AN ELEMENT

TITLE _____

001 #LBLa	Store code:	057 ST+6	Calculate $\tau_{\max}$ and $\frac{s_1 + s_2}{2}$ from strains.
002 1	1 = rectangular	058 GSB5	
003 GT00	2 = equiangular	059 RCLC	
004 #LBLb		060 RCL9	
005 2		061 1	
006 #LBL0		062 +	
007 ST01		063 ÷	
008 RTN	Store ν and E.	064 ST×5	
009 #LBLd		065 RCLC	
010 ST09		066 1	
011 R4		067 RCL9	
012 ST0E		068 -	
013 RTN		069 ÷	
014 #LBLA	Store e_a , e_b and e_c .	070 ST×6	
015 ST0C		071 RCLC	
016 R4		072 RCLB	
017 ST0B		073 -	
018 R4		074 3	
019 ST0A		075 TX	
020 RTN	Calculate e_1 and e_2 .	076 GT0i	
021 #LBLB		077 #LBL1	
022 RCLA		078 2	
023 GT0i		079 RCLB	
024 #LBL2		080 x	
025 RCLB		081 RCLA	
026 +		082 -	
027 #LBL1		083 RCLC	
028 RCLC		084 -	
029 +		085 RCLA	
030 ST06		086 RCLC	
031 0		087 GT04	
032 GT0i		088 #LBL2	
033 #LBL2		089 x	
034 RCLC		090 2	
035 RCLA		091 RCLA	
036 -		092 x	
037 #LBL1		093 RCLB	
038 RCLB		094 -	
039 RCLC		095 RCLC	
040 -		096 #LBL4	
041 +P		097 -	Output θ .
042 RCLA		098 GSB6	
043 RCLB		099 R4	
044 -		100 PRYX	
045 +P		101 RTN	
046 2		102 #LBLC	
047 TX		103 R1	
048 x		104 R1	
049 ST05		105 ST03	
050 2		106 ST06	
051 GT01		107 R1	
052 #LBL2		108 ST+6	
053 1		109 -	
054 +		110 ST04	
055 #LBL1		111 2	
056 ST+5		112 ST+6	

REGISTERS									
0	1	2	3	4	5	6	7	8	9
		20	s_x	$s_x - s_y$	$\tau_{\max}$	$(s_1 + s_2)/2$			ν
S0	S1	S2	S3	S4	S5	S6	S7	S8	S9
A	B	C	D	E	E	I	Control		
e_a	e_b	e_c							

DATE _____ AUTHOR _____

113	$\div$			
114	RT			
115	STO2			
116	ST+2			
117	+P			
118	STO5			
119	RCL2			
120	CHS			
121	RCL4			
122	#LBL6	Calculate θ and 2θ .		
123	X $\neq$ 0?			
124	$\div$			
125	TAN $\leftarrow$			
126	STO2			
127	2			
128	$\div$			
129	θ			
130	RTN			
131	#LBLD	Output s_1 , s_2 and r_{max} and θ .		
132	GSB5			
133	RCL5			
134	PRTX			
135	RCL2			
136	2			
137	$\div$			
138	PRTX			
139	RTN			
140	#LBL E	Calculate s and t from θ' .		
141	SPC			
142	ENT1			
143	+			
144	RCL2			
145	-			
146	RCL5			
147	+R			
148	RCL6			
149	+			
150	PRTX			
151	X $\neq$ Y			
152	PRTX			
153	PTN			
154	#LBL5	Calculate e_1 and e_2 or s_1 and s_2 .		
155	SPC			
156	RCL6			
157	RCL5			
158	+			
159	PRTX			
160	RCL6			
161	RCL5			
162	-			
163	PRTX			
164	RTN			

LABELS					FLAGS	SET STATUS			
A e_1, b, t, e_c	B $\rightarrow e_1, e_2, \theta$	C s_x, t, s_y, t, r_{xy}	D $\rightarrow s_1, s_2, r_{max}, \theta$	E $\theta' \rightarrow s, t$	0	FLAGS		TRIG	DISP
Rectangular	Equiangular	c	D E t p	e	1	ON	OFF	DEG ☒	FIX ☐
Store code	Rectangular	2 Equiangular	3	4 Output	2	1 ☐	☒	GRAD ☐	SCI ☐
Calc	θ	7	8	9	3	2 ☐	☒	RAD ☐	ENG ☒
						3 ☐	☒		n 3

SODERBERG'S EQUATION FOR FATIGUE

TITLE _____

001 #LBLA	If flag 3 is set, store s_{yp} .	057 #LBLB	Store or calculate K.						
002 STOB		058 STOB							
003 F3?		059 F3?							
004 RTN		060 RTN							
005 GSB1	If flag 3 is not set, calculate s_{yp} .	061 RCL8							
006 GSB2		062 RCLE							
007 RCLB		063 ÷							
008 x		064 GSB1							
009 RCL5		065 -							
010 ÷	066 GSB2								
011 CHS	067 RCL8								
012 RCLE	068 x								
013 1/X		069 RCL9							
014 +		070 ÷							
015 ÷		071 ÷							
016 STOB		072 STOB							
017 RTN		073 RTN							
018 #LBLA	Store or calculate s_e .	074 #LBLC	Store or calculate P_{max} .						
019 STOB		075 STOB							
020 F3?		076 F3?							
021 RTN		077 RTN							
022 GSB2		078 RCLA							
023 RCL8		079 ENT↑							
024 x		080 +							
025 RCLB		081 RCL8							
026 x		082 x							
027 GSB1		083 RCLE							
028 CHS	084 ÷								
029 RCL8	085 RCLB								
030 RCLE	086 RCL8								
031 ÷	087 x								
032 +	088 RCL9								
033 ÷	089 ÷								
034 STOB		090 1							
035 RTN		091 -							
036 #LBLA	Store or calculate A.	092 RCLD							
037 STOA		093 x							
038 F3?		094 +							
039 RTN		095 RCLB							
040 1		096 RCL8							
041 STOA		097 x							
042 GSB1		098 RCL9							
043 GSB2		099 ÷							
044 RCLB		100 1							
045 x		101 +							
046 RCL8	102 ÷								
047 x	103 STOB								
048 RCL9	104 RTN								
049 ÷	105 #LBLD	Store or calculate P_{min} .							
050 +	106 STOB								
051 RCL6	107 F3?								
052 ÷	108 RTN								
053 RCLE	109 RCLA								
054 x	110 ENT↑								
055 STOA	111 +								
056 RTN		112 RCL8							
REGISTERS									
0	1	2	3	4	5	6	7	8 s_{yp}	9 s_e
S0	S1	S2	S3	S4	S5	S6	S7	S8	S9
A	B	C	D	E	F	G	H	I	J
A	K	P_{max}	P_{min}	FS					

CANTILEVER BEAMS

TITLE _____

001 *LBL a	Initialize	057 F2?	
002 0		058 CLX	
003 ST03		059 ST0D	V_2'
004 ST04		060 R4	
005 ST05		061 RCL1	
006 RTN		062 4	
007 *LBL b	Store R and EI.	063 ÷	
008 ST02		064 RCLB	
009 R4		065 -	
010 x		066 RCL1	
011 ST0E		067 x	
012 RTN	Store P and a.	068 RCLB	
013 *LBL c		069 X²	
014 ST03		070 1	
015 X*Y		071 -	
016 ST0A		072 5	
017 RTN		073 x	
018 *LBL d	Store W and b.	074 +	
019 ST04		075 RCL1	
020 X*Y		076 X²	
021 ST0E		077 x	
022 RTN		078 RCLD	
023 *LBL e	Store M and c.	079 +	
024 ST05		080 RCL4	
025 X*Y		081 x	$V_1' + V_2'$
026 ST0C		082 -	
027 RTN		083 RCLC	
028 *LBLA	V_1'	084 GSB4	
029 ST0B		085 6	
030 RCLA		086 x	
031 GSB4		087 RCL1	
032 LSTX		088 3	
033 x		089 x	V_3'
034 CHS		090 X*Y	
035 3		091 F2?	
036 x		092 CLX	
037 F2?		093 +	
038 0		094 RCL5	
039 RCL1		095 x	
040 RCLA		096 RCL1	
041 3		097 x	
042 x		098 +	$V_1' + V_2' + V_3'$
043 -		099 6	
044 RCL1		100 ÷	
045 x		101 RCLB	V
046 +		102 +	
047 RCL3		103 RTN	
048 x		104 *LBLB	
049 RCL1		105 ST0B	
050 x		106 RCLA	
051 RCLB		107 GSB4	
052 GSB4		108 RCL1	θ_1'
053 RCLB		109 2	
054 3		110 ÷	
055 Y*		111 RCLA	
056 x		112 -	

REGISTERS

0 x	1 x'(a)	2 l	3 P	4 W	5 M	6	7	8	9
S0	S1	S2	S3	S4	S5	S6	S7	S8	S9
A	B	C	D	E	EI	I			
a	b	c							

AUTHOR

113	RCL3				169	X2			
114	x				170	2			
115	RCL1				171	÷			
116	x				172	+			
117	RCLB				173	RCL4			
118	GSB4				174	x			
119	R4				175	-			M ₁ + M ₂
120	RCL1				176	RCLC			
121	6	θ ₂ '			177	GSB4			
122	÷				178	CLX			M ₃
123	RCLB				179	RCL5			
124	2				180	X2Y			
125	÷				181	F2?			
126	-				182	+			
127	RCL1				183	RTN			M ₁ + M ₂ + M ₃
128	x				184	*LBLD			
129	RCLB				185	ST00			
130	X2				186	RCLA			V ₁
131	2				187	GSB4			
132	÷				188	0			
133	+				189	F2?			
134	RCL4				190	RCL3			
135	x				191	RCLB			
136	RCL1				192	GSB4			
137	x				193	CLX			
138	-				194	RCL1			
139	RCLC				195	RCLB			V ₂
140	GSB4				196	-			
141	R4	θ ₃ '			197	RCL4			
142	RCL5				198	x			
143	RCL1				199	-			
144	x				200	RTN			V
145	+				201	*LBL4			
146	RCLC	θ ₁ ' + θ ₂ ' + θ ₃ '			202	CF2			
147	÷				203	RCL0			Select smaller of x and a
148	RTN	0			204	ST01			(or b or c) and store as
149	*LBLC				205	X2Y			x'.
150	ST00				206	X2Y?			
151	RCLA	M ₁			207	ST01			
152	GSB4				208	X) Y?			
153	RCL1				209	SF2			If x > a set flag.
154	RCLA				210	-			
155	-				211	RTN			
156	RCL3								
157	x								
158	RCLB								
159	GSB4								
160	CLX								
161	RCL1	M ₂							
162	2								
163	÷								
164	RCLB								
165	-								
166	RCL1								
167	x								
168	RCLB								

LABELS					FLAGS	SET STATUS		
A x+y	B x→θ	C x→M _x	D x→V	E	0	FLAGS	TRIG	DISP
a Start	b ITE?r	c atP	d bTW	e cTM	1	ON OFF	DEG ☐	FIX ☐
0	1	2	3	4 Store x'	2	1 ☐	GRAD ☐	SCI ☐
5	6	7	8	9	3	2 ☐	RAD ☐	ENG ☐
						3 ☐		n 3

SIMPLY SUPPORTED BEAMS

TITLE _____

001 *LBL0	Store zeros for P, W, and M.	057 2	
002 0		058 4	
003 ST03		059 ÷	
004 ST04		060 RCL0	
005 ST05		061 X=Y	
006 RTN		062 x	
007 *LBL6	Store l and EI.	063 F0?	
008 ST02		064 LSTX	
009 R4		065 CHS	
010 x		066 GSB1	
011 ST0E		067 RCL1	
012 RTN		068 X ²	
013 *LBLc	Store P and a.	069 F0?	Compute y ₁ (EI) or θ ₁ (EI).
014 ST03		070 3	
015 X=Y		071 F0?	
016 ST0A		072 x	
017 RTN		073 RCLD	
018 *LBLd	Store W.	074 X ²	
019 ST04		075 +	
020 RTN		076 RCL2	
021 *LBL0	Store M and c.	077 X ²	
022 ST05		078 -	
023 X=Y		079 x	
024 ST0C		080 6	
025 RTN		081 ÷	
026 *LBLB	Set derivative flag.	082 GSB2	
027 SF0		083 RCL1	
028 GT0B		084 X ²	
029 *LBLA	Clear derivative flag.	085 RCL2	Compute y ₃ (EI) or θ ₃ (EI).
030 CF0		086 ÷	
031 *LBL0		087 6	
032 ST0B		088 ÷	
033 RCL2	Compute	089 F0?	
034 ENT↑		090 3	
035 x	y ₂ (EI) or θ ₂ (EI).	091 F0?	
036 LSTX		092 x	
037 x		093 RCL2	
038 RCL0		094 3	
039 F0?		095 ÷	
040 4		096 +	
041 F0?		097 RCLD	
042 x		098 X ²	
043 RCL2		099 2	
044 2		100 ÷	
045 x		101 RCL2	
046 F0?		102 ÷	
047 3		103 +	
048 F0?		104 RCLD	
049 x		105 -	
050 -		106 x	
051 RCL0		107 RCL2	
052 X ²		108 x	
053 x		109 RCL1	
054 +		110 +	
055 RCL4		111 RCL0	
056 x		112 ÷	
Y = y ₁ + y ₂ + y ₃ or θ = θ ₁ + θ ₂ + θ ₃			

REGISTERS									
0 x	1 x ₁ (x - l)	2 l	3 P	4 W	5 M	6	7	8	9
S0	S1	S2	S3	S4	S5	S6	S7	S8	S9
A a		B		C c		D (l-a), -a; c, l-c		E EI	F SUM

$$V = y_1 + y_2 + y_3$$

$$\text{or}$$

$$\theta = \theta_1 + \theta_2 + \theta_3$$

DATE _____ AUTHOR _____

113	RTN	-----	169	+	-----
114	*LBL0	Set derivative flag.	170	STO1	-----
115	SF0	-----	171	RCL0	Store x and c.
116	GTO0	-----	172	STO1	-----
117	*LCLC	Clear derivative flag.	173	RCLC	-----
118	CF0	-----	174	STO0	-----
119	*LBL0	-----	175	X>Y?	If c > x GTO 0.
120	STO0	Compute M_{x2}	176	GTO0	-----
121	2	or V_2	177	RCL0	Otherwise store x - ℓ
122	$\div$	-----	178	RCL2	for x and ℓ - c for c.
123	RCL2	-----	179	-	-----
124	F0?	-----	180	STO1	-----
125	2	-----	181	RCL2	-----
126	F0?	-----	182	RCLC	-----
127	$\div$	-----	183	-	-----
128	RCL0	-----	184	STO0	-----
129	-	-----	185	*LBL0	$\frac{M}{\ell}$
130	RCL4	-----	186	RCL5	-----
131	x	-----	187	RCL2	-----
132	x	-----	188	$\div$	-----
133	F0?	-----	189	F0?	-----
134	LSTX	-----	190	RTN	-----
135	GSB1	M_{x1} or V_1	191	RCL1	$\frac{M_x}{\ell}$
136	GSB2	M_{x3} or V_3	192	x	-----
137	RCL1	$M = M_{x1} + M_{x2} + M_{x3}$	193	RTN	-----
138	+	or			
139	RTN	$V = V_1 + V_2 + V_3$			
140	*LBL1	Store first results.			
141	STO1	-----			
142	RCL2	Store $\ell - a$			
143	RCL4	and			
144	-	x			
145	STO0	-----			
146	RCL0	-----			
147	STO1	If a > x GTO 0			
148	RCL4	-----			
149	X>Y?	-----			
150	GTO0	-----			
151	RCL4	Otherwise store -a for $\ell - a$			
152	CHS	and x - ℓ for x.			
153	STO0	-----			
154	RCL2	-----			
155	ST-1	-----			
156	*LBL0	-----			
157	RCL3	$\frac{P(\ell - a)}{\ell}$			
158	RCL0	-----			
159	x	-----			
160	RCL2	-----			
161	$\div$	-----			
162	F0?	-----			
163	RTN	$\frac{P(\ell - a)x}{\ell}$			
164	RCL1	-----			
165	x	-----			
166	RTN	-----			
167	*LBL2	Add first result to second.			
168	RCL1	-----			

LABELS					FLAGS	SET STATUS		
A x→y	B x→0	C x→M _x	D x→V	E RCL x	0 Derivative	FLAGS	TRIG	DISP
a Start	b IfE1 ℓ	c atP	d W	e c1M	1	ON OFF	DEG ☒	FIX ☐
0 Used	1 Con	2 Mom	3	4	2	1 ☐ ☒	GRAD ☐	SCI ☐
5	6	7	8	9	3	2 ☐ ☒	RAD ☐	ENG ☒
						3 ☐ ☒		n 3

BEAMS FIXED AT BOTH ENDS

TITLE

001 #LBLd		Store W.	057 x							
002 STG4			058 x ³							
003 RTN			059 XZY							
004 #LBLc		Store l and EI.	060 x							
005 STG2			061 Fθ?							
006 Pj			062 LSTX							
007 x			063 Fθ?							
008 STOE			064 -							
009 RTN			065 -							
010 #LBLc		Store P and a.	066 GSB6							
011 STG3			067 ε							
012 XZY			068 ÷							
013 STG4			069 Fθ?							
014 RTN			070 x							
015 #LBLc		Store M and c.	071 Fθ?							
016 STG5			072 x							
017 XZY			073 Fθ?							
018 STOC			074 GSB3							
019 RTN			075 GSB4							
020 #LBLc		Set derivative flag and start θ ₂ calculation.	076 RCLC							
021 SFθ			077 GSB1							Calculate y ₃ EI and/or θ ₃ EI.
022 STDθ			078 Fθ?							
023 GSB7			079 x ³							
024 RCL2			080 Fθ?							
025 x			081 x							
026 x			082 XZY							
027 RCLθ			083 Fθ?							
028 GSB7			084 GSB7							
029 GTθθ			085 +							
030 #LBLd		Clear derivative flag and start y ₂ calculation.	086 GSB6							
031 CFθ			087 GSB8							
032 STDθ			088 RCLE							Calculate y or θ.
033 X ²			089 ÷							
034 RCL2			090 RTN							
035 GSB7			091 #LBLD							Set derivative flag and start V ₂ calculation.
036 RCLθ			092 SFθ							
037 #LBLO			093 STDθ							
038 SF1			094 RCL2							
039 -		Complete calculation of θ ₂ EI or y ₂ EI.	095 XZY							
040 RCLθ			096 GSB7							
041 x			097 GTθθ							
042 RCL2			098 #LBLC							Clear derivative flag and start M ₂ calculation.
043 X ²			099 CFθ							
044 -			100 STDθ							
045 x			101 RCL2							
046 2			102 XZY							
047 4			103 -							
048 ÷			104 RCLθ							
049 RCL4			105 x							
050 x			106 RCL2							
051 RCLA			107 X ²							
052 GSB1		Calculate y ₁ EI or θ ₁ EI.	108 6							
053 RCL1			109 ÷							
054 x			110 #LBLO							
055 RCLD			111 SF1							Complete calculation of V ₂ or M ₂ .
056 RCL2			112 -							
REGISTERS										
0 x	1 x, (l - x)	2 l	3 P	4 W	5 M	6	7	8	9	
S0	S1	S2	S3	S4	S5	S6	S7	S8	S9	
A a	B	C c	D a, (l - a); c, (l - c)	E EI	F	G	H	I	J	SUM

DATE _____ AUTHOR _____

113	2			169	RCL2	
114	÷			170	RCL0	
115	RCL4			171	-	
116	X			172	ST01	
117	RCLA			173	*LBL0	
118	GSE1			174	RCL5	$\frac{P(l-a)^2}{q^3}$ or
119	F0?			175	F1?	
120	GTO0			176	RCL3	
121	RCL1	Calculate V_1 or M_1 .		177	RCL2	
122	X			178	RCLD	
123	RCLD			179	-	
124	RCL2			180	F1?	$\frac{M(l-a)}{q^3}$
125	X			181	X ²	
126	-			182	X	
127	*LBL0			183	RCL2	
128	X			184	3	
129	F0?			185	Y ^X	
130	GSE3			186	÷	
131	GSE4			187	RCL2	
132	RCLC			188	RCLD	
133	GSE1			189	F1?	
134	F0?	Calculate V_3 or M_3 .		190	GTO0	$\frac{(l-3a)l}{2}$
135	R4			191	3	
136	F0?			192	X	
137	CLX			193	-	
138	F0?			194	RCL2	
139	RCLD			195	X	
140	6			196	2	
141	X			197	÷	
142	XZY			198	RCLD	ax
143	GSE7			199	RCL1	
144	+			200	X	
145	X			201	RTN	
146	*LBL0			202	*LBL0	
147	F0?			203	GSE7	$(l+2a)$
148	GTO4	Sign change?		204	+	
149	GSE3			205	CF1	
150	*LBL1			206	RTN	
151	RCL1			207	*LBL3	
152	+	Calculate sum.		208	F2?	Sign change.
153	RTN			209	CHS	
154	*LBL1			210	RTN	
155	CF2	Store a or c and sum.		211	*LBL6	Calculation subroutine.
156	STOD			212	X	
157	R4			213	RCL1	
158	STO1			214	*LBL5	
159	RCLD			215	X ²	
160	RCL0			216	F0?	
161	STO1			217	FX	
162	X $\neq$?			218	X	
163	GTO0	Is x beyond loading point?		219	RTN	
164	SF2			220	*LBL7	
165	RCL2	Yes - set sign change flag and a = l - a or c = l - c and x = l - x.		221	ENT+	2X subroutine
166	RCLD			222	+	
167	-			223	RTN	
168	STOD					

LABELS					FLAGS	SET STATUS		
A x→y	B x→0	C x→M _x	D x→V	E	0 Derivative			
a	b 1fE1l	c aP	d W	e cM	1 P			
0 Used	1 Calc.	2	3 Sign	4 sum	2 Sign			
5 Calc.	6 Calc.	7 2x	8	9	3			

FLAGS		SET STATUS		
ON	OFF	DEG	GRAD	FIX
☐	☒	☐	☐	☐
☐	☒	☐	☐	☐
☐	☒	☐	☐	☐
☐	☒	☐	☐	☐

PROPPED CANTILEVER BEAMS

TITLE

001	*LBLa					057	÷			
002	0					058	RCL2			
003	STO3	Initialize				059	X²			
004	STO5					060	-			
005	*LBLd					061	STOD			
006	STO4	Store W.				062	x			
007	RTN					063	RCL1			
008	*LBLb					064	X²			
009	STO2	Store L and EI.				065	+			
010	R↓					066	GSB4			
011	x					067	F2?			
012	STOE					068	GTOD			
013	RTN					069	RCL0			
014	*LBLc					070	RCLA			
015	STO3	Store P and a.				071	-			
016	XZY					072	X²			
017	STOA					073	F0?			
018	RTN					074	LSTX			
019	*LBLe					075	F0?			
020	STO5	Store M and c.				076	x			
021	XZY					077	F0?			
022	STOC					078	3			
023	RTN					079	F0?			
024	*LBLf	Store x, clear integral flag, load constants.				080	÷			
025	CF0					081	-			
026	STO0					082	*LBL0			
027	5					083	3			
028	ENT1					084	x			
029	8					085	RCL3			
030	STOB					086	x			
031	*LBLA	Store x, set integral flag, load constants.				087	ST+1		EI (y₁ + y₂)	
032	SF0					088	6		EI (θ₁ + θ₂)	
033	STOB					089	ST÷1			
034	3					090	GSB1			
035	ENT1					091	RCLD			
036	2					092	x			
037	*LBL0					093	3			
038	RCL0	Calculate 6 y₂				094	x			
039	x	EI or				095	RCL2			
040	RCL2	6θ₂ EI.				096	+			
041	÷					097	GSB4			
042	-					098	F2?			
043	RCL0					099	GTOD			
044	X²					100	RCL0			
045	x					101	GSB4			
046	RCL2					102	0			
047	X²					103	F0?			
048	-					104	R↓			
049	RCL2					105	F0?			
050	x					106	RCLC			
051	GSB5	Calculate 6y₁ EI or 6θ₁ EI.				107	X²			
052	RCL0					108	+			
053	X²					109	F0?			
054	F0?					110	2			
055	3					111	F0?			
056	F0?					112	÷			
REGISTERS										
0	x	1 sum	2 l	3 D	4 W	5 M	6	7	8	9
S0	S1	S2	S3	S4	S5	S6	S7	S8	S9	
A	a	B	C	c	D	(x²/3 - k²)	E	EI	I	(l - a); c

DATE _____ AUTHOR _____

113	GT00				169	RCL1		or
114	*LBL6				170	RTN		$V = V_1 + V_2 + V_3$
115	RCLC				171	*LBL4		Multiply by x if integral
116	GSB4				172	F0?		flag is set.
117	*LBL0				173	RCL0		
118	-				174	F0?		
119	GSB8				175	x		
120	RCLC				176	RTN		
121	÷				177	*LBL5		Finish y_2 , θ_2 , M_2 and
122	RTN				178	RCL4		V_2 calculations.
123	*LBLD				179	x		
124	CF0				180	GSB4		
125	ST00				181	8		
126	2				182	÷		
127	x				183	ST01		
128	GT00				184	CF1		Store b.
129	*LBLC				185	RCL2		
130	SF0				186	RCL4		
131	ST00				187	-		
132	*LBL0				188	ST01		
133	3				189	LSTX		
134	RCL2				190	GT00		
135	x				191	*LBL1		Store c.
136	X $\leftrightarrow$ Y				192	RCLC		
137	4				193	ST01		
138	x				194	*LBL0		
139	-				195	CF2		Set x $\leftarrow$ to a or c flag.
140	GSB5				196	RCL0		
141	GSB4				197	X $\leftrightarrow$ Y?		
142	F2?				198	SF2		
143	GT00				199	RCL1		Calculate
144	1				200	3		
145	GSB4				201	x		
146	-				202	F1?		$3a^2q - a^3$
147	F0?				203	RCL2		$2q^3$
148	RCL4				204	RCL2		
149	F0?				205	x		First pass, then
150	+				206	RCL1		
151	*LBL0				207	X 2		
152	RCL3				208	-		
153	x				209	2		
154	ST+1				210	F1?		$\frac{q^2 - c^2}{4q^3}$ on
155	GSB1				211	X 2		
156	6				212	÷		Second pass.
157	x				213	RCL2		
158	GSB4				214	3		
159	F2?				215	Y*		
160	GT00				216	÷		
161	F0?				217	F1?		
162	1				218	RTN		
163	F0?				219	SF1		
164	-				220	RCL1		
165	*LBL8				221	x		
166	RCL5				222	RTN		
167	x							
168	ST+1							

LABELS					FLAGS		SET STATUS		
A Start	B ItE1x	C aTP	D W	E cTM	0 Integral		FLAGS	TRIG	DISP
a x→y	b x→θ	c x→M _x	d x→V	e	1 Moment		ON OFF	DEG ☐	FIX ☐
0 Used	1 P	2	3	4 x mult	2 x $\leq$ d or c		0 ☐ ☐	GRAD ☐	SCI ☐
5 W - P	6 Used	7	8 Mult & Sum	9			1 ☐ ☐	RAD ☐	ENG ☐
							2 ☐ ☐		n <u> 9 </u>

HELICAL SPRING DESIGN

TITLE _____

001 *LBL6	Store β , α , and G.	057 X^2	Calculate free length.						
002 ST08		058 LSTX							
003 R4		059 x							
004 ST0A		060 $\div$							
005 R4		061 RCL5							
006 ST09		062 $+$							
007 RTN		063 ST0C							
008 *LBL6		064 PRTX							
009 ST02		065 RTN							
010 X^2Y		066 *LBL8		Calculate solid length.					
011 ST01	067 SPC								
012 RTN	068 RCL1								
013 *LBL4	069 RCL5								
014 ST04	070 $\div$								
015 X^2Y	071 RCL2								
016 ST03	072 $+$								
017 RCL1	073 ST0D								
018 $-$	074 RCLC								
019 RCL2	075 2	Calculate stress at solid.							
020 RCL4	076 $+$								
021 $-$	077 RCL6								
022 $\div$	078 x								
023 ST05	079 ST0E								
024 SPC	080								
025 PRTX	081 RCL5								
026 RTN	082 x								
027 *LBL6	083 RCL6								
028 SPC	084 RCL8		Output dimensions.						
029 x	085 $\div$								
030 ST06	086 CSE1								
031 CLX	087 x								
032 LSTX	088 RCL6								
033 RCL3	089 x								
034 x	090 RCL8								
035 8	091 X^2								
036 x	092 $\div$								
037 P4	093 RCL8								
038 $\div$	094 $\div$	Calculate number of coils.							
039 X^2Y	095 8								
040 ST08	096 x								
041 ST-6	097 P4								
042 3	098 $\div$								
043 Y^x	099 ST08								
044 $+$	100 PRTX								
045 PRTX	101 RTN								
046 RTN	102 *LBL6								
047 *LBLA	103 SPC								
048 SPC	104 RCLD	Calculate uncorrected stress at point 2.							
049 RCL5	105 PRTX								
050 RCL8	106 RCL6								
051 X^2	107 PRTX								
052 X^2	108 RCL6								
053 x	109 PRTX								
054 8	110 RCL8								
055 $\div$	111 $+$								
056 RCL6	112 PRTX								
REGISTERS									
0 s_2	1 P_1	2 L_1	3 P_2	4 L_2	5 k	6 OD, D	7 s_2	8 d	9 G
S0	S1	S2	S3	S4	S5	S6	S7	S8	S9
A α	B β	C N	D L_f	E L_s	F	G	H	I	TS

DATE

AUTHOR

113 RTN		169 RCL0		173 RTN	Spring is acceptable.
114 *LBLa	Ferrous/non-ferrous toggle.	170 XZY?		174 *LBL4	Spring may be over-
115 F0?		171 GT04		175 RCL6	designed. Try smaller
116 GT08		172 5		176 4	wire.
117 SF0		173		177 RTN	
118 0		174		178 GT05	Smaller wire input.
119 RTN		175		179 *LBL2	Compute wire tensile
120 *LBL0		176		180 RCL8	strength from α and β .
121 1		177		181 LN	
122 CF0		178		182 RCLB	
123 RTN		179		183 x	
124 *LBLC		180		184 RCLA	
125 RCL4	If coil-to-coil clearance is	181		185 +	
126 RCL6	adequate, branch to label	182		186 ENT↑	
127 -	zero.	183		187 ST01	
128 RCLD		184		188 .	
129 RCL4		185		189 3	Convert to f_{max} .
130 -		186		190 5	
131 .		187		191 ENT↑	
132 1		188		192 .	
133 x		189		193 1	
134 XZY?		190		194 F0?	
135 GT08		191		195 CLX	
136 GSB2	Check stress with in-	192		196 +	
137 R4	adequate clearance.	193		197 x	
138 RCL0		194		198 XZY	
139 XZY?		195		199 LSTX	Convert to YS.
140 GT03		196		200 .	
141 1		197		201 2	
142 RTN	Change criteria.	202		203 +	
143 *LBL3		203		204 x	
144 RCL8		204		205 RTN	
145 2	Try smaller wire.	206		206 *LBL1	Compute Wahl factor.
146 RTN		207		207 4	
147 ST08	Store smaller wire size and	208		208 x	
148 GT04	branch.	209		209 1	
149 *LBL0	Check stress with adequate	210		210 -	
150 GSB2	clearance.	211		211 ENT↑	
151 RCL0		212		212 ENT↑	
152 XZY?		213		213 3	
153 GT03		214		214 -	
154 RCL8	Try larger wire.	215		215 ÷	
155 3		216		216 .	
156 RTN		217		217 6	
157 *LBL5		218		218 1	
158 RCL8	Store larger wire size and	219		219 5	
159 ST+6	branch.	220		220 RCL0	
160 R4		221		221 ÷	
161 ST08		222		222 +	
162 ST-6		223		223 RTN	
163 GT04					
164 *LBL3	Check to see if spring is				
165 RCL1	over-designed.				
166 .					
167 3					
168 x					

LABELS					FLAGS	SET STATUS			
A → N	B → s ₀	C → code	D	E (→ L ₁ L ₂ D ₀ D ₁)	0 Ferrous?	FLAGS	TRIG	DISP	
^a Fe?	^b G ₁ αβ	^c P ₁ L ₁	^d P ₂ ↑L ₂ →k	^e d ₁ f ₀ ↑D _H →S ₂	1	ON OFF	DEG ☒	FIX ☐	
⁰ Used	¹ Wahl	² TS	³ code 2,4,5	⁴ code 4	2	1 ☐ ☒	GRAD ☐	SCI ☐	
⁵ Larger d	⁶	⁷	⁸	⁹	3	2 ☐ ☒	RAD ☐	ENG ☒	n <u>3</u>
						3 ☐ ☒			

FOUR BAR FUNCTION GENERATOR

TITLE

001 *LBLA	Store d, c, b and a.	057 ST03	θ_1 and						
002 ST04		058 R4	calculate θ_2 .						
003 R4		059 ST01							
004 ST03		060 R†							
005 R4		061 -							
006 ST02		062 RCLA							
007 R4		063 RCLB							
008 ST01		064 -							
009 RTN		065 x							
010 *LBLB		066 RCLC							
011 RCL1	Calculate R_1, R_2 and R_3 .	067 RCLA							
012 RCL4		068 -							
013 ÷		069 ÷							
014 ST0A		070 RCL1							
015 RCL1		071 +							
016 RCL2		072 ST02							
017 ÷		073 P=S							
018 ST0B		074 RTN							
019 RCL1		075 *LBLA							
020 X^2		076 P=S	Store ϕ_3 and ϕ_1 and						
021 RCL2		077 ST06	calculate ϕ_2 .						
022 X^2		078 R4							
023 +		079 ST04							
024 RCL4		080 R†							
025 X^2		081 -							
026 +		082 CMS							
027 RCL3		083 ST00							
028 X^2		084 RCLA							
029 -		085 GSBC							
030 RCL2		086 ST01							
031 RCL4		087 ST0E							
032 x		088 RCLC							
033 2		089 GSBC							
034 x		090 RCL1							
035 ÷		091 -							
036 ST0C		092 ST01							
037 DSP4		093 RCLB							
038 RCLA		094 GSBC							
039 SPC		095 RCLE							
040 PRTX		096 -							
041 RCLB		097 RCL1							
042 PRTX		098 ÷							
043 RCLC		099 RCL0							
044 PRTX		100 x							
045 RTN		101 RCL4							
046 *LBLC	f(x) - your function.	102 +							
047 RTN		103 ST05							
048 *LBLD	Store x_3, x_2, x_1 .	104 P=S							
049 ST0C		105 RTN							
050 R4									
051 ST0B									
052 R4									
053 ST0A									
054 RTN									
055 *LBLB	Store θ_3 and								
056 P=S									
REGISTERS									
0 Used	1 a, cos θ_1	2 b, cos θ_2	3 c, cos θ_3	4 d, cos ϕ_1	5 cos ϕ_2	6 cos ϕ_3	7 1	8 1	9 1
S0 Used	S1 θ_1	S2 θ_2	S3 θ_3	S4 ϕ_1	S5 ϕ_2	S6 ϕ_3	S7 R_1	S8 R_2	S9 R_3
A $R_1, x_1, \cos(\theta_1 - \phi_1)$	B $R_2, x_2, \cos(\theta_2 - \phi_2)$	C $R_3, x_3, \cos(\theta_3 - \phi_3)$	D Det	E Used	F Used	G	H	I	J

DATE _____ AUTHOR _____

LABELS					FLAGS	SET STATUS			
A atbtctd	B $\rightarrow R_1, R_2, R_3$	C f(x)	D $x_1 \uparrow x_2 \uparrow x_3$	E $\theta_1 \uparrow \theta_2 \rightarrow \theta_3$	0				
a $\phi_1 \uparrow \phi_2 \rightarrow \phi_3$	b	c	d	e	1				
0	1	2	3	4	2				
5	6	7	8	9	3				
						FLAGS 0 ☐ ON ☒ OFF 1 ☐ ☒ 2 ☐ ☒ 3 ☐ ☒	TRIG DEG ☒ GRAD ☐ RAD ☐	DISP FIX ☒ SCI ☐ ENG ☐ n <u>2</u>	

(Card 2)

TITLE

001 *LBL6	Calculate $R_1, R_2, \text{ and } R_3.$	057 PRTX	----- Calculate determinant.						
002 GSB6		058 X^2							
003 *LBL5		059 RCL0							
004 GSB6		060 RCL7							
005 STOD		061 $\div$							
006 RCLA		062 STOD							
007 STOI		063 X^2							
008 RCL6		064 $+$							
009 STOI		065 RCL0							
010 RCLC		066 X^2							
011 STOI		067 $+$							
012 GSB0		068 RCL0							
013 RCLD		069 RCL6							
014 $\div$		070 $\div$							
015 STOI		071 RCL0							
016 PRTX		072 RCL7							
017 GSB6		073 $\div$							
018 RCLA		074 $\times$							
019 STOI		075 2							
020 RCL6		076 $\times$							
021 STOI		077 RCL9							
022 RCLC		078 $\times$							
023 STOI		079 $-$							
024 GSB0		080 TX							
025 RCLD		081 STOC							
026 $\div$		082 PRTX							
027 STOI		083 RCLD							
028 PRTX		084 $\text{F}\div\text{S}$							
029 GSB6		085 PRTX							
030 RCLA		086 SPC							
031 STOI		087 RTN							
032 RCL6		088 *LBL0							
033 STOI		089 RCL5							
034 RCLC		090 RCL9							
035 STOI		091 $\times$							
036 GSB0		092 RCL8							
037 RCLD		093 RCL6							
038 $\div$		094 $\times$							
039 PRTX		095 $-$							
040 SPC		096 RCL1							
041 $\text{F}\div\text{S}$		097 $\times$							
042 STOI		098 RCL4							
043 RCL6		099 RCL9							
044 STOI		100 $\times$							
045 RCL1		101 RCL7							
046 STOI		102 RCL6							
047 RCL9		103 $\times$							
048 $\text{F}\div\text{S}$		104 $-$							
049 RTN		105 RCL2							
050 *LBL0		106 $\times$							
051 STOI	107 $-$								
052 $\text{F}\div\text{S}$	108 RCL4								
053 STOI	109 RCL8								
054 RCL8	110 $\times$								
055 $\div$	111 RCL7								
056 STOI	112 RCL5								
REGISTERS									
0 Used	1 $\cos \theta_1$	2 $\cos \theta_2$	3 $\cos \theta_3$	4 $\cos \phi_1$	5 $\cos \phi_2$	6 $\cos \phi_3$	7 1	8 1	9 1
S0 Used	S1 θ_1	S2 θ_2	S3 θ_3	S4 ϕ_1	S5 ϕ_2	S6 ϕ_3	S7 R_1	S8 R_2	S9 R_3
A $\cos(\theta_1 - \phi_1), a$	B $\cos(\theta_2 - \phi_2), b$	C $\cos(\theta_3 - \phi_3), c$	D Det, d	E Used	F Used	G Used	H Used	I Used	

DATE _____ AUTHOR _____

113	x		169	R4	
114	-		170	ST03	
115	RCL3		171	1	
116	x		172	ST07	
117	+		173	ST08	
118	RTN		174	ST09	
119	4LBL6		175	RTN	
120	P2S	Calculate the coefficients for the system of linear equations.			
121	RCL1				
122	COS				
123	LSTX				
124	RCL4				
125	-				
126	LSTX				
127	COS				
128	CHS				
129	X2Y				
130	COS				
131	ST04				
132	R4				
133	P2S				
134	ST04				
135	R4				
136	ST01				
137	P2S				
138	RCL2				
139	COS				
140	LSTX				
141	RCL5				
142	-				
143	LSTX				
144	COS				
145	CHS				
146	X2Y				
147	COS				
148	ST08				
149	R4				
150	P2S				
151	ST05				
152	R4				
153	ST02				
154	P2S				
155	RCL3				
156	COS				
157	LSTX				
158	RCL6				
159	-				
160	LSTX				
161	COS				
162	CHS				
163	X2Y				
164	COS				
165	ST0C				
166	R4				
167	P2S				
168	ST06				

LABELS						FLAGS	SET STATUS		
A	B	C	D	E	F	FLAGS		TRIG	DISP
a	b → R ₁ , R ₂ , R ₃	c a → b, c, d	d	e	f	0	☐ ON ☒ OFF	DEG ☒	FIX ☒
0 Determinant	1	2	3	4	2	1	☐ ☒	GRAD ☐	SCI ☐
5 R ₁ , R ₂ , R ₃	6 Coefficients	7	8	9	3	2	☐ ☒	RAD ☐	ENG ☐
						3	☐ ☒		n 2

[illegible][illegible]

THE UNIVERSITY OF CHICAGO

DATE _____ AUTHOR _____

113	*LBLE	Convert $d\phi/d\theta$ to RPM.			
114	STO9				
115	RCL3				
116	x				
117	RTN				
118	*LBLE		Calculate $d^2\phi/d\theta^2$.		
119	STO2				
120	RCL7				
121	RCL4				
122	-				
123	1				
124	→R				
125	1				
126	RCL3				
127	-				
128	X^2				
129	x				
130	RCLA				
131	RCLB				
132	÷				
133	RCL4				
134	$X \rightarrow Y$				
135	→R				
136	$X \rightarrow Y$				
137	R↑				
138	-				
139	STO1				
140	CLX				
141	RCL3				
142	X^2				
143	x				
144	+				
145	CMS				
146	RCL7				
147	COS				
148	RCLA				
149	x				
150	RCL5				
151	÷				
152	+				
153	RCL1				
154	÷	Convert to RPM ² .			
155	ENT1				
156	+				
157	Pi				
158	x				
159	RCL9				
160	X^2		Add in contribution of input link acceleration.		
161	x				
162	RCL2				
163	RCL3				
164	x				
165	+				
166	RTN				

LABELS					FLAGS	SET STATUS			
A	B	C	D	E	0	FLAGS		TRIG	DISP
$\theta \rightarrow \phi (\alpha)$		$\theta \rightarrow \phi (\alpha)$		$\theta \rightarrow \phi (\alpha)$	α	ON OFF			
a1b1c1d		connector		$\theta1m\Delta\theta1RPM$	1	0	☐ ON ☐ OFF	DEG ☐	FIX ☐
0 connector	1	2	3	4	2 Δ	1	☐ GRAD ☐	SCI ☐	
5	6	7	8	9 loop	3	2	☐ RAD ☐	ENG ☐	
						3	☐ ☐		n 2

PROGRESSION OF SLIDER CRANK

TITLE _____

001 #LBL0		057 RTN	
002 ST00	Store θ , calculate x and ϕ .	058 #LBL0	Output $x_{\max}$ and $x_{\min}$.
003 #LBL7		059 SPC	
004 SPC		060 CF1	
005 GSB2		061 GSB0	
006 COS		062 SF1	
007 ST04		063 ST04	
008 RCLC		064 GSB0	
009 x		065 RTN	
010 RCL0		066 #LBL6	Calculate $\phi_{\max}$ and $\phi_{\min}$.
011 COS		067 SPC	
012 ST03		068 1	
013 RCLD		069 SIN ⁻¹	
014 x		070 GSB2	
015 +		071 ST04	
016 ST01		072 PRTX	
017 PRTX		073 1	
018 RCL0		074 CHS	
019 GSB2		075 SIN ⁻¹	
020 PRTX		076 GSB2	
021 RTN		077 PRTX	
022 #LBLA	Store R, L, E, and N and calculate ω .	078 RTN	
023 ST0D		079 #LBL2	Subroutine for ϕ .
024 R4		080 SIN	
025 STOC		081 RCLD	
026 R4		082 x	
027 STOB		083 RCL0	
028 R4		084 +	
029 STOA		085 RCLC	
030 RCLA		086 ÷	
031 P4		087 SIN ⁻¹	
032 x		088 ST02	
033 3		089 RTN	
034 0		090 #LBLC	Calculate v and ϕ .
035 ÷		091 SPC	
036 STOE		092 RCL0	
037 SPC		093 RCL2	
038 PRTX		094 +	
039 RTN		095 SIN	
040 #LBL0	Calculate $x_{\max}$ or $x_{\min}$.	096 CHS	
041 RCL0		097 RCL4	
042 RCLC		098 ÷	
043 RCLD		099 RCLF	
044 F1?		100 x	
045 CHS		101 RCLD	
046 +		102 x	
047 ÷		103 PRTX	
048 SIN ⁻¹		104 RCL4	
049 COS		105 RCLC	
050 RCLC		106 x	
051 RCLD		107 RCLD	
052 F1?		108 ÷	
053 CHS		109 1/X	
054 +		110 ST05	
055 x		111 RCL3	
056 PRTX		112 x	

REGISTERS									
0 θ	1 x	2 ϕ	3 $\cos \theta$	4 $\cos \phi$	5 $R/(L \cos \phi)$	6 $(\theta_1 - \theta_2)/h$	7 θ_1	8 θ_2	9 n
S0	S1	S2	S3	S4	S5	S6	S7	S8	S9
A N	B E	C L	D R	E ω	I Index				

DATE _____

AUTHOR _____

113	RCL		169	-	
114	x		170	CHS	
115	PRTX		171	RCL5	
116	PTH		172	÷	
117	*LBLD	Calculate a and ϕ .	173	ST06	
118	SPC		174	*LBL4	
119	RCL3		175	SPC	
120	X ²		176	SPC	
121	RCLD		177	RCL7	
122	x		178	PRTX	
123	RCLC		179	ST08	
124	÷		180	CF1	
125	RCL4		181	GSB7	
126	3		182	GSB0	
127	Y ^x		183	GSB0	
128	÷		184	SF1	
129	RCL0		185	DSZ1	
130	RCL2		186	GT03	
131	+		187	RTN	
132	COS		188	*LBL3	
133	RCL4		189	RCL6	
134	÷		190	ST+7	
135	+		191	GT04	
136	CHS		192	RTN	
137	RCLD				
138	x				
139	RCL				
140	X ²				
141	x				
142	PRTX				
143	RCL2				
144	TAN				
145	RCL5				
146	RCL3				
147	x				
148	X ²				
149	x				
150	RCL0				
151	SIN				
152	RCL5				
153	x				
154	-				
155	RCL				
156	X ²				
157	x				
158	PRTX				
159	RTN				
160	*LBL				
161	ST09				
162	ST01	Automatically output θ , x, ϕ , v, ϕ , a, and ϕ , for n intervals between θ_1 and θ_2 .			
163	ISZ1				
164	R4				
165	ST08				
166	R4				
167	ST07				
168	R1				

LABELS					FLAGS	SET STATUS		
A N1ET1R → ω	B $\theta \rightarrow x, \phi$	C $\rightarrow v, \phi$	D $\rightarrow a, \theta$	E $\theta_1, \theta_2, n \rightarrow \text{List}$	0			
a $\rightarrow x_{\max}, x_{\min}$	b $\rightarrow \phi_{\max}, \phi_{\min}$	c	d	e	1 Max - Min			
0 $x_{\max}$	1	2 ϕ	3 Used	4 Used	2			
5	6	7 Used	8	9	3			

FLAGS		SET STATUS	
ON	OFF	TRIG	DISP
0 ☐	0 ☐	DEG ☒	FIX ☒
1 ☐	1 ☐	GRAD ☐	SCI ☐
2 ☐	2 ☐	RAD ☐	ENG ☐
3 ☐	3 ☐		n <u>2</u>

CIRCULAR CAMS

TITLE _____

001 *LBL0	Flat or roller toggle.	057 PRTX	
002 F0?		058 GSB0	
003 GT00		059 RCL5	
004 1		060 PRTX	
005 SF0		061 RTN	
006 RTN		062 *LBLC	Output $dy/d\theta$ and $d^2y/d\theta^2$.
007 *LBL0		063 SPC	
008 0		064 RCL4	
009 CF0		065 PRTX	
010 RTN		066 RCL3	
011 *LBL6	Function code store, and clear flag 1.	067 PRTX	
012 CF1		068 RTN	
013 STOI		069 *LBLD	Output α .
014 RTN		070 SPC	
015 *LBLC		071 RCL2	
016 STOC	Store increment, duration, angle, π (according to angular mode of calculator) and initialize θ' register.	072 PRTX	
017 R4		073 RTN	
018 STOB		074 *LBLE	Output r_θ and ϕ .
019 R4		075 SPC	
020 STOT		076 RCL0	
021 1		077 PRTX	
022 CHS		078 RCL1	
023 COS+		079 PRTX	
024 STOE		080 RTN	
025 0		081 *LBL0	Harmonic if flag 1 is set.
026 STOE		082 1	
027 RTN		083 F1?	
028 *LBL4	Store lift.	084 STOI	
029 STOD		085 RCL6	$\theta/\beta \rightarrow R_E$
030 RTN		086 RCLB	
031 *LBLE		087 +	
032 STOI	Store R_θ and R_ϕ or $R_r - R_\theta$ for roller cams.	088 STOE	
033 R4		089 GSB1	Lift function.
034 STOA		090 RCLD	Calculate lift = $h f(\theta/\beta)$.
035 F0?		091 x	
036 RTN		092 STOS	
037 -		093 RCLD	
038 STOA		094 RCLB	Calculate velocity.
039 RTN		095 +	
040 *LBLA		096 RCL4	
041 GSB6	Calculate values automatically.	097 x	
042 GSB0		098 STOA	
043 GSB0		099 RCLD	
044 GSB0		100 RCLB	Calculate acceleration.
045 RCLB		101 x^2	
046 RCL6	Check for completion and bring θ into display.	102 +	
047 $x \leq y?$		103 RCL3	
048 GTOA		104 x	
049 RCL7		105 STOS	
050 RCLC		106 RCLB	Calculate pressure angle.
051 -		107 RCL9	
052 RTN		108 RCL5	
053 *LBLB	Output θ and y .	109 +	
054 SPC		110 STOI	
055 SPC		111 +	
056 RCL7		112 P1	

REGISTERS									
0 r_θ	1 h	2 α	3 y''	4 y'	5 y	6 θ'	7 θ	8	9 R_θ
S0	S1	S2	S3	S4	S5	S6	S7	S8	S9
A R_θ or $(R_r - R_\theta)$	B β	C Inc	D h	E θ'/β	F	G	H	I	Control

DATE _____

AUTHOR _____

113	+		169	RCLB	$f'(\theta/\beta)$
114	RCL4		170	x	
115	x		171	Pi	
116	TAN ⁻¹		172	2	
117	STD2	If flat follower go to LBL0.	173	+	
118	F0?		174	→R	
119	GT00		175	Pi	
120	RCL1	Calculate grinder radius.	176	x	
121	→R		177	ST03	
122	RCL4		178	R4	$f'(\theta/\beta)$
123	-		179	ST04	$f(\theta/\beta)$
124	→P		180	1	
125	ST00		181	RCLB	
126	RCL4	Calculate grinder angular offset.	182	RCLB	
127	XZY		183	x	
128	+		184	COS	
129	RCL2		185	-	
130	SIN		186	2	
131	x		187	+	
132	SIN ⁻¹		188	RTN	
133	GT09		189	*LBL2	
134	*LBL0	Calculate grinder radius.	190	ENT↑	Cycloidal cam: $f'(\theta/\beta)$
135	LSTX		191	+	
136	RCL1		192	RCLB	
137	x		193	x	
138	LSTX		194	1	
139	→P		195	→R	
140	ST01		196	CNS	
141	RCL2		197	1	
142	RCL4		198	+	
143	→R		199	ST04	
144	RCL1		200	RJ	
145	+		201	ST01	$f'(\theta/\beta)$
146	→P		202	ENT↑	
147	ST00		203	+	
148	RCL4	Calculate grinder angular offset.	204	Pi	
149	RCL2		205	x	
150	COS		206	ST03	
151	x		207	RCLB	
152	RCL1		208	RCL1	$f(\theta/\beta)$
153	+		209	2	
154	XZY		210	+	
155	+		211	Pi	
156	COS ⁻¹		212	+	
157	RCL2		213	-	
158	-		214	RTN	
159	CNS				
160	*LBL9	Calculate angle of grinder.			
161	RCL7				
162	+				
163	ST01	Increment angle.			
164	RCLC				
165	ST+6				
166	ST+7				
167	RTN				
168	*LBL1	Harmonic cams			

LABELS					FLAGS	SET STATUS		
A Auto	B →θ, γ	C →γ', γ''	D →α	E →r _g , φ	0 FLT/RLR	FLAGS	TRIG	DISP
^a FLT/RLR	^b HAR, CYC	^c θ ₀ †β†Δθ	^d h	^e (R ₀ †R _g †R _h)	¹ HAR	ON OFF	DEG ☐	FIX ☐
⁰ Used	¹ Harmonic	² Cycloidal	³	⁴	²	1 ☐ ☐	GRAD ☐	SCI ☐
⁵	⁶	⁷	⁸	⁹ r _g , φ	³	2 ☐ ☐	RAD ☐	ENG ☐
						3 ☐ ☐		n <u>3</u>

LINEAR CAMS

TITLE _____

001 #LBL _a	Store function code and clear flag 1.	057 PRTX	
002 CF1		058 RTN	
003 STOI		059 #LBL _E	Output x_g and y_g .
004 RTN		060 SPC	
005 #LBL _b	Store increment, duration angle, and initialize x' register.	061 RCL ₈	
006 STOC		062 PRTX	
007 R4		063 RCL1	
008 STOB		064 PRTX	
009 RJ		065 RTN	
010 STOT		066 #LBL ₈	Harmonic if flag 1 is set.
011 0		067 1	
012 STOE		068 FI?	
013 RTN		069 STOI	
014 #LBL _c	Store lift.	070 RCL6	Store x'/L in R_E .
015 STOD		071 RCL ₈	
016 RTN		072 ÷	
017 #LBL _d	Store base lift.	073 STOE	
018 STOS		074 GSB1	
019 RTN		075 RCLD	Multiply by lift.
020 #LBL _e		076 ST×3	
021 STOE	Store $R_g - R_r$.	077 ST×4	
022 -		078 x	
023 STOA		079 RCL9	Y
024 RTN		080 +	
025 #LBL _f		081 STOS	
026 GSB ₈	Calculate values automatically.	082 RCL ₈	
027 GSB _C		083 ST÷4	Divide by L.
028 GSB _D		084 ST÷3	
029 GSB _E		085 ST÷3	
030 RCL ₈		086 RCL4	
031 RCL6	Check for completion and bring x into display.	087 TAN ⁻¹	Calculate α .
032 $X \angle Y?$		088 STO2	
033 STOA		089 RCL _A	$(R_g - R_r) \sin \alpha$
034 RCL7		090 +R	$(R_g - R_r) \cos \alpha$
035 RCLC		091 RCL5	
036 -		092 +	y_g
037 RTN		093 STOI	
038 #LBL ₈		094 XZ _Y	
039 SPC	Output x and y.	095 CHS	x_g
040 SPC		096 RCL7	
041 RCL7		097 +	
042 PRTX		098 STOB	
043 GSB ₈		099 RCLC	
044 RCL5		100 ST+6	Increment x.
045 PRTX		101 ST+7	
046 RTN		102 RTN	
047 #LBL _C	Output dy/dx and d^2y/dx^2 .	103 #LBL1	
048 SPC		104 DEG	Harmonic function.
049 RCL4		105 1	
050 PRTX		106 8	
051 RCL3		107 0	
052 PRTX		108 x	
053 RTN		109 FI	
054 #LBL _D	Output α .	110 2	
055 SPC		111 ÷	
056 RCL2		112 +R	

REGISTERS

0 x_g	1 y_g	2 α	3 y''	4 y'	5 y	6 x'	7 x	8 R_r	9 y_b
S0	S1	S2	S3	S4	S5	S6	S7	S8	S9
A $R_g - R_r$	B L	C Δx	D h	E x'/L	F	G	H	I	J Control

DATE _____ AUTHOR _____

113	PI			169	X ²		
114	x			170	2		
115	ST03			171	x		
116	R4			172	RTN		
117	ST04			173	*LBL0	x > .5	
118	1			174	CLX		
119	RCLE			175	4		
120	1			176	CHS		
121	0			177	ST03		
122	0			178	1		
123	x			179	RCLE		
124	COS			180	-		
125	-			181	x		
126	2			182	CHS		
127	÷			183	ST04		
128	RTN			184	LSTX		
129	*LBL2			185	X ²		
130	DEG	Cycloidal function.		186	ENT†		
131	ENT†			187	+		
132	+			188	CHS		
133	1			189	1		
134	0			190	+		
135	0			191	RTN		
136	x						
137	1						
138	→P						
139	CHS						
140	1						
141	+						
142	ST04						
143	R4						
144	ST01						
145	ENT†						
146	+						
147	PI						
148	x						
149	ST03						
150	RCLE						
151	RCL1						
152	2						
153	÷						
154	PI						
155	÷						
156	-						
157	RTN						
158	*LBL3						
159	.						
160	5	Parabolic function.					
161	X≤Y?						
162	GT00						
163	CLX						
164	4	x < .5					
165	ST03						
166	x						
167	ST04						
168	RCLE						

LABELS					FLAGS	SET STATUS		
A Auto	B →x, y	C y', y''	D →α	E →x _g , y _g	0	FLAGS	TRIG	DISP
a (1, 2, 3)	b x ₀ ± L1Δx	c h	d v _b	e R _g † R _r	1 Har	0 ON OFF	DEG ☒	FIX ☐
0	1 Harmonic	2 Cycloidal	3 Parabolic	4	2	1 ☒ ☐	GRAD ☐	SCI ☐
5	6	7	8	9	3	2 ☐ ☒	RAD ☐	ENG ☒
						3 ☐ ☒		n <u>3</u>

GEAR FORCES

TITLE _____

001 *LBLA	Calculate F_t .	057 $R\uparrow$	
002 $\div$		058 $+$	
003 ST06		059 $R\downarrow$	
004 RTN	Store α .	060 $-$	
005 *LBLB		061 $R\uparrow$	
006 ST0A		062 PRTX	
007 RTN		063 $X\neq Y$	
008 *LBLC	Store ϕ_n .	064 PRTX	
009 ST05		065 RTN	
010 RTN		066 *LBLd	Store coefficient of friction.
011 *LBLD	Convert ϕ to ϕ_n and store.	067 ST04	
012 TAN		068 RTN	
013 RCLA		069 *LBLe	Calculate F_{ws} , F_{gex} .
014 COS		070 SPC	
015 $\times$		071 RCL5	
016 TAN $\downarrow$		072 SIN	
017 ST05		073 LSTX	
018 RTN		074 COS	
019 *LBLE	Calculate F_{ga} and F_{gex} .	075 RCLA	
020 SPC		076 SIN	
021 RCL6		077 $\times$	
022 RCLA		078 RCLA	
023 TAN		079 COS	
024 $\times$		080 RCL4	
025 RCL5		081 $\times$	
026 TAN		082 $+$	
027 RCLA		083 $\div$	
028 COS		084 RCL6	
029 $\div$		085 $\times$	
030 RCL6		086 PRTX	
031 $\times$		087 1	
032 PRTX		088 RCLA	
033 $X\neq Y$		089 TAN	
034 PRTX		090 RCL4	
035 RTN	Store bevel gear cone angle.	091 $\times$	
036 *LBLa		092 RCL5	
037 ST0B		093 COS	
038 RTN	Calculate F_{bpax} and F_{bgex} .	094 $\div$	
039 *LBLb		095 $-$	
040 SPC		096 RCLA	
041 RCLB		097 TAN	
042 RCL5		098 RCL4	
043 TAN		099 RCL5	
044 RCLA		100 COS	
045 COS		101 $\div$	
046 $\div$		102 $+$	
047 RCL6		103 $\div$	
048 $\times$		104 RCL6	
049 $\rightarrow R$		105 $\times$	
050 RCL6		106 PRTX	
051 RCLA		107 RTN	
052 TAN			
053 $\times$			
054 RCLB			
055 $X\neq Y$			
056 $\rightarrow R$			

REGISTERS									
0	1	2	3	4	5	6	7	8	9
				f	ϕ_n	F_t			
S0	S1	S2	S3	S4	S5	S6	S7	S8	S9
A	α	B	cone L	C	D	E		F	

DATE _____ AUTHOR _____

LABELS					FLAGS	SET STATUS		
A $T \rightarrow F_t$	B α	C ϕ_n	D ϕ	E F_{ge}, F_{gax}	0	1	2	3
$a \text{ cone } L$	$D \rightarrow F_{bpax}, F_{bgax}$	c	d f	$a \rightarrow F_{we}, F_{gax}$	1	2	3	4
0	1	2	3	4	5	6	7	8
5	6	7	8	9	10	11	12	13
						ON OFF 0 ☐ ☒ 1 ☐ ☒ 2 ☐ ☒ 3 ☐ ☒ DEG ☒ GRAD ☐ RAD ☐ FIX ☒ SCI ☐ ENG ☐ n <u>2</u>		

STANDARD EXTERNAL INVOLUTE SPUR GEARS

TITLE

001	*LBLA					057	3		
002	STO1					058	Y*		
003	X*Y					059	STO7		
004	STO2					060	*LBL1		
005	÷					061	RCL6		
006	STO5					062	RCL7		
007	SFC					063	+		
008	PRTX					064	RCL7		
009	Pi					065	TAN		
010	2					066	-		
011	=					067	LSTX		
012	RCL2					068	ENT†		
013	÷					069	x		
014	STO8					070	÷		
015	PRTX					071	ST+7		
016	RTN					072	RCL7		
017	*LBLB					073	÷		
018	STO3					074	ABS		
019	X*Y					075	EEX		
020	STO4					076	CHS		
021	RTN					077	6		
022	*LBLC					078	X*Y?		
023	RCL8					079	GT01		
024	RCL5					080	RCL7		
025	÷					081	SIN		
026	RCL4					082	DEG		
027	TAN					083	SIN†		
028	+					084	STO7		
029	RCL4					085	GT09		
030	Pi					086	*LBLB		
031	x					087	RCL5		
032	1					088	2		
033	8					089	÷		
034	0					090	RCL4		
035	÷					091	COS		
036	-					092	x		
037	RCL3					093	RCL7		
038	RCL5					094	COS		
039	÷					095	÷		
040	RCL4					096	STOE		
041	COS					097	2		
042	÷					098	x		
043	+					099	RCL3		
044	Pi					100	RCL1		
045	RCL1					101	2		
046	÷					102	÷		
047	-					103	FRC		
048	STO6					104	X=0?		
049	K+D					105	GT03		
050	GT09					106	R↓		
051	*LBLD					107	X*Y		
052	RAD					108	9		
053	RCL6					109	0		
054	3					110	RCL1		
055	x					111	÷		
056	.					112	COS		

REGISTERS									
0	1	2	3	4	5	6	7	8	9
	N	P	d_w	ϕ	D	inv ϕ_w	ϕ_w	t	Used
S0	S1	S2	S3	S4	S5	S6	S7	S8	S9
A	B	C	D	M	E	q	I		

BELT LENGTH

TITLE

001 *LBLA	Toggle for printing belt tangent points.	057 RCL1	
002 0		058 RCL4	
003 F2?		059 -	
004 RTN		060 X ²	
005 SF2		061 -	
006 1		062 JX	
007 RTN		063 ST+8	
008 *LBLA	Input x_1, y_1, R_1	064 RCL1	
009 CLRG		065 RCL4	
010 SF1		066 -	
011 ST00		067 X ² Y	
012 ST01		068 GSB1	
013 R↓		069 ST07	
014 ST08		070 +	
015 R↓		071 RCL1	
016 ST0A		072 X	
017 1		073 RCLC	
018 CHS		074 =	
019 COS ⁻¹		075 P↓	
020 ST0C		076 X	
021 RCL0		077 ST+8	
022 RTN		078 F2?	
023 *LBLB	Input x_1, y_1, R_1 and make calculation.	079 GSBc	
024 ST04		080 RCL4	
025 CLX		081 ST01	
026 RCL3		082 CF1	
027 P±S		083 RTN	
028 ST03		084 *LBLB	
029 P±S		085 -	$\theta_1 - \alpha_1$
030 X ² Y		086 1	
031 ST03		087 +R	
032 X ² Y		088 +P	
033 -		089 X	
034 X ² Y		090 ABS	
035 RCL2		091 RCL7	
036 P±S		092 -	
037 ST02		093 RTN	
038 P±S		094 *LBLC	
039 X ² Y		095 RCL4	
040 ST02		096 RCLB	
041 X ² Y		097 RCL0	
042 -		098 GSB8	
043 +P		099 RCL6	
044 X ²		100 RCL5	
045 X ² Y		101 GSB8	
046 X(0?)		102 RCL1	
047 GSB8		103 X	
048 F1?		104 RCLC	
049 ST05		105 =	
050 F1?		106 P↓	
051 ST06		107 X	
052 RCL6		108 ST+8	
053 X ² Y		109 RCL8	
054 ST06		110 RTN	
055 GSB8		111 *LBL0	
056 X ² Y		112 RCLC	

REGISTERS									
0 R ₁	1 R ₁₋₁	2 x ₁	3 y ₁	4 R ₁	5 θ_1	6 θ_1	7 α	8 Σ Length	9 Used
S0	S1	S2 x ₁₋₁	S3 y ₁₋₁	S4	S5	S6	S7	S8	S9
A x ₁	B y ₁	C 180°	D $\theta_{1-1}, i + 90^\circ - \alpha$	E					

DATE _____

AUTHOR _____

113 + 114 LSTX 115 + 116 RTN 117 #LBL1 118 +P 119 R1 120 COS 121 X<θ? 122 CTDS 123 CLX 124 LSTX 125 RTN 126 #LBL9 127 CLX 128 LSTX 129 RCLC 130 + 131 1 132 →R 133 +P 134 R1 135 RTN 136 #LBL6 137 1 138 SIN- 139 RCL6 140 + 141 RCL7 142 - 143 STOD 144 RCL1 145 →R 146 P=S 147 RCL2 148 + 149 PRTX 150 X=Y 151 RCL3 152 + 153 PRTX 154 SPC 155 P=S 156 RCLD 157 RCL4 158 →R 159 RCL2 160 + 161 PRTX 162 X=Y 163 RCL3 164 + 165 PRTX 166 SF2 167 SPC 168 SPC	Add 180° ----- Adjustment for angles. ----- Obtain θ or α. ----- Calculation for belt tangent points.	169 RTN	
--	---	---------	--

LABELS				FLAGS		SET STATUS			
A x_1, y_1, r_1	B x_1, y_1, r_1	C →L	D	E $\theta_1 - \alpha_1$	0 last?	FLAGS		TRIG	DISP
a points?	b for last i	c points	d	e	1 first	ON	OFF	DEG ☒	FIX ☒
0	1 2π	2	3	4	2 points	0	☐	GRAD ☐	SCI ☐
5	6	7	8	9 θ or α	3	1	☐	RAD ☐	ENG ☐
						2	☐		
						3	☐		n 2

FREE VIBRATIONS

TITLE _____

001 #LBLA	Store k, c, and m and calculate ω .	057 x	
002 CLRG		058 CHS	
003 ST04		059 e*	
004 R4		060 STOC	
005 ST03		061 RCL5	
006 R4		062 X<0?	
007 ST02		063 GT0c	
008 RCL4		064 X=0?	
009 GSB0		065 GT0k	
010 RTN		066 #LBLa	
011 #LBL0	Calculate $\left[\frac{k}{m} - \left(\frac{c}{2m} \right)^2 \right]^{1/2}$	067 RCLD	For $c > c_r$.
012 RCL2		068 RCL0	
013 +		069 x	
014 ST0E		070 RCL1	
015 RCL3		071 +	
016 RCL2		072 RCL5	
017 2		073 +	
018 x		074 RCL0	
019 +		075 +P	
020 ST0D		076 ST0A	
021 X?		077 R4	
022 -		078 ST0E	
023 RND		079 RCL5	
024 X<0?		080 RCL7	
025 GT01		081 x	
026 X=0?		082 -	
027 RTN		083 CHS	
028 #LBL3		084 ST09	
029 LSTX		085 COS	
030 JX		086 RCLC	
031 ST05		087 x	
032 RTN		088 RCL4	
033 #LBL1		089 x	
034 LSTX		090 ST02	
035 ST05		091 PRTX	
036 1		092 RCLD	
037 CHS		093 x	
038 RTN		094 RCL9	
039 #LBLB	Calculate c_{cr} .	095 SIN	
040 RCL4		096 RCLC	
041 RCL2		097 x	
042 x		098 RCL5	
043 JX		099 x	
044 2		100 RCL4	
045 x		101 x	
046 RTN		102 +	
047 #LBLC		103 CHS	
048 ST01	Store initial displacement and velocity.	104 PRTX	
049 R4		105 GT0e	
050 ST0B		106 #LBLb	
051 RTN		107 RCLD	For $c = c_r$.
052 #LBLD		108 RCL0	
053 SPC		109 x	
054 #LBL4	Calculate displacement, velocity and acceleration at time t.	110 RCL1	
055 ST0T		111 +	
056 RCLD		112 ST0B	

REGISTERS									
0 x_0	1 $\dot{x}_0$	2 $m, x(t)$	3 c, r_1	4 k, r_2	5 $\omega, \sqrt{-\omega^2}$	6 $(t_1 - t_2)/n$	7 t, t_1	8 $\dot{x}(t)$	9 $\omega t - \delta$
S0	S1	S2	S3	S4	S5	S6	S7	S8	S9
A R, A_{cr}, A_{ov}	B δ, B_{cr}, B_{ov}	C $e^{-c/2m t}$	D $c/2m$	E k/m	I n				

DATE _____

AUTHOR _____

113	RCL7		169	x	
114	x		170	e*	
115	RCL0		171	RCL8	
116	+		172	x	
117	RCLC		173	ST+2	
118	x		174	RCL4	
119	ST02		175	x	
120	PRTX		176	ST+8	
121	RCLD		177	RCL2	
122	x		178	PRTX	
123	CHS		179	RCL8	
124	RCLB		180	PRTX	
125	RCLC		181	*LBL e	
126	x		182	RCLD	
127	+		183	2	
128	PRTX		184	x	
129	ST0 e		185	x	
130	*LBL c		186	RCL2	
131	CHS	For c < c _r .	187	RCL2	
132	FX		188	x	
133	ENT†		189	+	
134	ENT†		190	CHS	
135	RCLD		191	PRTX	
136	-		192	RTN	
137	ST03		193	*LBL e	
138	XZ Y		194	ST01	
139	2		195	R4	
140	x		196	XZ Y	
141	-		197	ST07	
142	ST04		198	-	
143	RCL1		199	RCL1	
144	RCL3		200	÷	
145	RCL0		201	ST06	
146	x		202	ISZ†	
147	-		203	*LBL9	
148	RCL4		204	RCL7	
149	RCL3		205	SPC	
150	-		206	PRTX	
151	÷		207	GSB4	
152	ST08		208	DSZ†	
153	RCL0		209	GT08	
154	-		210	RTN	
155	CHS		211	*LBL0	
156	ST0A		212	RCL6	
157	RCL3		213	ST+7	
158	RCL7		214	GT09	
159	x		215	RTN	
160	e*				
161	RCL A				
162	x				
163	ST02				
164	RCL3				
165	x				
166	ST08				
167	RCL4				
168	RCL7				

LABELS					FLAGS	SET STATUS			
A m t c k + ω	B → c _r	C x ₀ t x ₀	D t → x, x̄, x̄	E t ₁ t ₂ t ₃ t _n → List	0	ON OFF			
a c > c _r	b c = c _r	c c < c _r	d x̄	e Used	1	0 ☐ ☒	DEG ☐	FIX ☒	
0 ω	1 c > c _r	2 c = c _r	3 c < c _r	4 Used	2	1 ☐ ☒	GRAD ☐	SCI ☐	
5	6	7	8 Used	9 t → x	3	2 ☐ ☒	RAD ☒	ENG ☐	
						3 ☐ ☒		n 3	

VIBRATIONS FORCED BY $F_0 \cos \omega t$

TITLE

001 #LBLA	Store k, c, and m and calculate ω_0 , ω_n and ξ .	057 RCL2	
002 SPC		058 x	
003 CLRG		059 RCL9	
004 SFB		060 RCL3	
005 ST04		061 x	
006 R4		062 XZY	
007 ST03		063 +P	
008 R4		064 ST0C	
009 ST02		065 RCL8	
010 RCL4		066 XZY	
011 GSB0		067 ÷	
012 PRTX		068 PRTX	
013 RCL3		069 R4	
014 RCL4		070 ST0B	
015 RCL2		071 RTN	
016 x		072 #LBLC	Store F_0 and ω and calculate AMP and δ .
017 JX		073 SPC	
018 2		074 ST08	
019 x		075 R4	
020 ÷		076 ST09	
021 PRTX		077 R4	
022 RTN		078 RCL6	
023 #LBL0	Calculate ω_0 and ω_n .	079 RCL9	
024 RCL2		080 GSB4	
025 ÷		081 R+D	
026 ST0E		082 PRTX	
027 JX		083 PTN	
028 PRTX		084 #LBLD	Input t and calculate x(t), $\dot{x}(t)$ and $\ddot{x}(t)$.
029 RCL6		085 SPC	
030 RCL3		086 #LBL6	
031 RCL2		087 ST06	
032 2		088 RCL9	
033 x		089 x	
034 ÷		090 RCLB	
035 ST0D		091 -	
036 X ²		092 COS	
037 -		093 LSTX	
038 RND		094 SIN	
039 X<0?		095 XZY	
040 CTO1		096 RCL8	
041 X=0?		097 x	
042 RTN		098 RCLC	
043 #LBL3		099 ÷	
044 LSTX		100 PRTX	
045 JX		101 RCL4	
046 ST05		102 x	
047 RTN		103 ST0B	
048 #LBL1		104 XZY	
049 LSTX		105 RCL8	
050 ST05		106 x	
051 1		107 RCLC	
052 CHS		108 ÷	
053 RTN		109 RCL9	
054 #LBL4		110 x	
055 X ²		111 CHS	
056 -		112 PRTX	

REGISTERS

0	1	2	3	4	5	6	7	8	9
k x(t)	c $\dot{x}(t)$	m	c	k	$\omega_n \sqrt{1-\xi^2}$	t, t ₁	ω_{res}^2	F ₀	ω
S0	S1	S2	S3	S4	S5	S6	S7	S8	S9
A (t ₁ - t ₂)/n	B δ	C Δ	D c/2m	E k/m	F 0.00				

DATE _____

AUTHOR _____

113 RCL3 114 x 115 ST01 116 CHS 117 RCL0 118 - 119 RCL5 120 RCL6 121 x 122 COS 123 RCL8 124 x 125 + 126 RCL2 127 + 128 PRTX 129 RTN 130 #LBL6 131 CF0 132 RCL6 133 RCLD 134 X ² 135 2 136 x 137 - 138 X>0? 139 GT09 140 ABS 141 JX 142 ST07 143 RTN 144 #LBL9 145 JX 146 ST07 147 DSP9 148 DSP3 149 RTN 150 #LBL6 151 ST01 152 R4 153 X ² Y 154 ST06 155 - 156 RCL1 157 = 158 ST0A 159 ISZ1 160 #LBL7 161 SPC 162 RCL6 163 PRTX 164 GSB6 165 DSZ1 166 GT08 167 RTN 168 #LBL6	----- Calculate ω_{reg}. ----- Calculate $x(t)$, $\dot{x}(t)$ and $\ddot{x}(t)$ and output the values automatically.	169 RCL4 170 ST+6 171 GT07 172 RTN	-----
---	---	---	--------------

LABELS					FLAGS	SET STATUS			
A m t c k	B $\rightarrow \omega_{reg}$	C $\omega t F_0 \rightarrow AMP, \delta$	D $t \rightarrow x, \dot{x}, \ddot{x}$	E $t_1 t_2 t_n \rightarrow \dots$	0	FLAGS		TRIG	DISP
a	b	c	d	e	1	ON	OFF		
0 ω_0, ω_n	1 $c > c_{cr}$	2	3 $c < c_{cr}$	4 AMP, δ	2	0	☐	DEG ☐	FIX ☒
5	6 Used	7 $t \rightarrow x_1$	8 $t + \Delta t$	9 ω_{reg}	3	1	☐	GRAD ☐	SCI ☐
						2	☐	RAD ☒	ENG ☐
						3	☐		n <u>3</u>

EQUATIONS OF STATE

TITLE _____

001 *LBL0	Redlich-Kwong; ideal gas	057 *LBL8	Ideal gas solution for n,
002 F0?	toggle.	058 SF1	R and T.
003 GT00		059 *LBL9	
004 0		060 RCL5	
005 SF0		061 RCL6	
006 RTN		062 x	
007 *LBL0		063 RCL7	
008 1		064 ÷	
009 CF0		065 RCL8	
010 RTN		066 ÷	
011 *LBL0	Store T _c .	067 RCL9	
012 CF3		068 ÷	
013 ST00		069 ST01	
014 RTN		070 *LBL0	Stop if ideal gas is desired.
015 *LBL0	Store P _c .	071 F0?	
016 CF3		072 RTN	
017 ST00		073 GSB1	
018 RTN		074 GT00	Calculate P by Redlich-
019 *LBL0	P code.	075 *LBL2	Kwong.
020 5		076 F1?	
021 GT00		077 GSB1	
022 *LBL0	V code.	078 *LBL0	
023 6		079 RCL6	
024 GT00		080 RCL9	
025 *LBL0	n code.	081 x	
026 7		082 RCL6	
027 GT00		083 RCL8	
028 *LBL0	R code.	084 -	
029 8		085 ST04	
030 GT00		086 ÷	
031 *LBL0	T code.	087 RCL0	
032 9		088 RCL9	
033 *LBL0		089 JX	
034 CF1	Store input.	090 ÷	
035 ST01		091 ST02	
036 R4		092 RCL6	
037 ST01		093 ÷	
038 F3?		094 LSTX	
039 RTN		095 RCL8	
040 1		096 +	
041 ST01	Dummy 1.00 for unknown	097 ST03	
042 GT01	and GTO ideal gas.	098 ÷	
043 *LBL5	Ideal gas solution for P	099 -	
044 *LBL0	and V.	100 RCL5	Calculate f(P).
045 RCL7		101 -	
046 RCL8		102 GSB1	Calculate f'(P).
047 x		103 ÷	
048 RCL9		104 ST-1	
049 x		105 RCL1	Loop again?
050 RCL5		106 ÷	
051 RCL6		107 ABS	
052 x		108 EEY	
053 ÷		109 CHS	
054 ST01		110 4	
055 GT00		111 X≤Y?	
056 *LBL7		112 GT02	

REGISTERS									
0	1	2 a/T ^{1/2}	3 (V + b)	4 (V - b)	5 P	6 V	7 n	8 R	9 T
S0	S1	S2	S3	S4	S5	S6	S7	S8	S9
A a	B b	C T _c	D P _c	E nR	I Control				

DATE _____

AUTHOR _____

113 RCL1 114 RTN 115 *LBL6 116 RCL6 117 ENT+ 118 + 119 RCLB 120 + 121 RCL2 122 x 123 RCL3 124 RCL6 125 x 126 X ² 127 ÷ 128 RCLE 129 RCL9 130 x 131 RCL4 132 X ² 133 ÷ 134 - 135 RTN 136 *LBL9 137 RCLE 138 RCL4 139 ÷ 140 RCL2 141 2 142 ÷ 143 RCL9 144 ÷ 145 RCL6 146 ÷ 147 RCL3 148 ÷ 149 + 150 RTN 151 *LBL7 152 *LBL8 153 RCL9 154 RCL6 155 x 156 RCL4 157 X ² 158 ÷ 159 RCL6 160 ENT+ 161 + 162 RCLB 163 + 164 RCLE 165 ÷ 166 RCL6 167 ÷ 168 RCL3	Display result of iteration. ----- $\frac{\partial P}{\partial V}$ ----- $\frac{\partial P}{\partial T}$ ----- $\frac{\partial P}{\partial n}$ or $\frac{\partial P}{\partial R}$ -----	169 X ² 170 ÷ 171 RCL2 172 x 173 - 174 RCLE 175 x 176 RCL1 177 ÷ 178 RTN 179 *LBL5 180 LSTX 181 + 182 STOE 183 R/S 184 *LBL1 185 RCL7 186 RCL8 187 x 188 STOE 189 . 190 0 191 8 192 6 193 7 194 RCLD 195 ÷ 196 X ² 197 RCLC 198 x 199 x 200 STOE 201 LSTX 202 x 203 RCLC 204 TX 205 x 206 4 207 . 208 9 209 3 210 4 211 x 212 STOE 213 RTN	----- Display P. ----- ----- Calculate a and b. ----- -----
--	--	--	---

LABELS					FLAGS	SET STATUS		
A ↔ P	B ↔ V	C ↔ n	D ↔ R	E ↔ T	0 R - K	FLAGS	TRIG	DISP
a R - K?	b T _c	c P _c	d	e	1 a, b	ON OFF		
0 Used	1 a, b	2 Iter	3	4	2	0 ☐ ☒	DEG ☒	FIX ☒
5 P	6 V	7 n	8 R	9 T	3 calc	1 ☐ ☒	GRAD ☐	SCI ☐
						2 ☐ ☒	RAD ☐	ENG ☐
						3 ☐ ☒		n <u>2</u>

ISENTROPIC FLOW FOR IDEAL GASES

TITLE _____

001 *LBL0	Store k, k - 1, 1/(k - 1).	057 SF3	
002 ST02		058 GT08	
003 1		059 *LBLD	Output p/p_0 .
004 -		060 F3?	
005 ST03		061 GT08	
006 1/X		062 GSB8	
007 ST04		063 RCL4	
008 RCL2		064 Y*	
009 RTN	Output M.	065 RTN	
010 *LBLA		066 *LBL0	Convert p/p_0 to T/T_0 and GT0 B.
011 F3?		067 SF3	
012 GT08		068 RCL3	
013 RCL1		069 Y*	
014 JX		070 GT08	
015 RTN		071 *LBL0	Set -3 in display for subsonic guess.
016 *LBL0	Store M^2 .	072 3	
017 X*		073 CHS	
018 ST01		074 X*Y	
019 JX		075 F3?	
020 RTN		076 GT01	
021 *LBL0	Output T/T_0 .	077 GT03	
022 F3?		078 *LBL1	
023 GT08		079 ENT+	Make guess of M^2 .
024 2		080 ST06	
025 RCL1		081 FRC	
026 RCL3		082 JX	
027 x		083 +	
028 2		084 X*Y	
029 +		085 Y*	
030 ÷		086 ST01	
031 RTN	Convert T/T_0 to M^2 .	087 *LBL2	
032 *LBL0		088 RCL6	
033 2		089 GSB3	
034 X*Y		090 ÷	
035 ÷		091 1	
036 2		092 -	
037 -		093 .	
038 RCL3		094 5	
039 ÷		095 RCL8	
040 ST01		096 ÷	
041 JX		097 .	
042 RTN		098 5	
043 *LBL0	Output P/P_0 .	099 RCL1	
044 F3?		100 ÷	
045 GT08		101 -	
046 GSB8		102 ÷	
047 RCL2		103 ST+1	
048 RCL3		104 RCL1	
049 ÷		105 ÷	
050 Y*		106 ABS	
051 RTN		107 EE*	
052 *LBL0		108 CHS	
053 RCL3	Convert P/P_0 to T/T_0 and GT0 B.	109 4	
054 RCL2		110 X*Y?	
055 ÷		111 GT02	
056 Y*		112 RCL1	

REGISTERS									
0	1 M^2	2 k	3 k - 1	4 1/k - 1	5	6 A/A*	7 (k-1)/k+1	8 Used	9 Used
S0	S1	S2	S3	S4	S5	S6	S7	S8	S9
A	B	C	D	E	F	G	H	I	J

DATE _____ AUTHOR _____

113	JX			
114	RTN			
115	#LBL6	Set +3 in display for super-sonic guess.		
116	3			
117	X ² Y			
118	F3?			
119	GT01			
120	#LBL3	Convert M ² to A/A*.		
121	2			
122	RCL2			
123	1			
124	+			
125	÷			
126	RCL3			
127	LSTX			
128	÷			
129	ST07			
130	RCL1			
131	x			
132	+			
133	ST06			
134	RCL7			
135	2			
136	x			
137	1/X			
138	YX			
139	RCL1			
140	JX			
141	÷			
142	RTN			
143	#LBL6	Output values.		
144	SPC			
145	CF3			
146	RCL2			
147	PRTX			
148	SPC			
149	GSBA			
150	PRTX			
151	GSBB			
152	PRTX			
153	GSBC			
154	PRTX			
155	GSBD			
156	PRTX			
157	GSBE			
158	PRTX			
159	RTN			

LABELS					FLAGS	SET STATUS			
A M→M	B T/T ₀ →M	C P/P ₀ →M	D ρ/ρ ₀ →M	E A/A* _{sub} →M	0	FLAGS		TRIG	DISP
^a k	^b →k,M,T/T ₀ ...	^c	^d	^e A/A* _{sup} →M	1	0	ON OFF	DEG ☒	FIX ☒
0 Used	1 M ² guess	2 M ² iter	3 A/A*	4	2	1	☐ ☒	GRAD ☐	SCI ☐
5	6	7	8	9	3 DATA?	2	☐ ☒	RAD ☐	ENG ☐
						3	☐ ☒		n <u>3</u>

CONDUIT FLOW

TITLE _____

001 *LBLA	Set divide by ρ flag.	057 ST04	Set f and Re in display.
002 SF2	-----	058 RCL5	
003 GT00	-----	055 1/X	
004 *LBL6	Clear divide by ρ flag.	060 X ²	
005 CF2	-----	061 RCL1	
006 *LBL0	-----	062 RCL4	Store velocity.
007 ST09	Store μ or ν .	063 RTN	
008 GT00	-----	064 *LBL0	
009 *LBL6	Store ρ .	065 ST02	
010 ST0A	-----	066 F3?	Guess v.
011 GT00	Store ϵ .	067 RTN	-----
012 *LBL4	-----	069 SF0	Iterate to find v.
013 ST0E	-----	069 GSB9	
014 GT00	-----	070 *LBL3	
015 *LBLA	Store L.	071 RND	
016 ST03	-----	072 ST00	
017 GT00	-----	073 GSB6	
018 *LBL6	Store D.	074 RND	
019 ST0D	-----	075 RCL0	
020 GT00	-----	076 X2Y	
021 *LBL6	Store $K_T/4$.	077 X*Y?	
022 4	-----	078 GT03	Set f, Re and v in display.
023 +		079 RCL5	
024 ST08		080 1/X	
025 *LBL0	-----	081 X ²	
026 CF3	Clear data input flag.	082 RCL1	
027 RTN	-----	083 RCL2	
028 *LBL6	-----	084 RTN	Calculate constants.
029 4		085 *LBL9	
030 6	Convert input psi to lb/ft-sec ² and store.	086 RCL4	
031 3	-----	087 F2?	
032 2		088 ST÷9	
033 X	-----	089 RCLD	
034 ST04		090 RCL5	
035 LSTX	Convert lb/ft-sec ² to psi and display.	091 +	
036 +	-----	092 ST06	
037 F3?		093 LN	
038 RTN	-----	094 1	
039 GSB6		095 .	
040 4		096 7	
041 6	Store pressure.	097 3	
042 3	-----	098 7	
043 2		099 ST07	
044 +		100 X	
045 RTN	-----	101 2	
046 *LBL6		102 .	
047 ST04	Compute pressure drop.	103 2	
048 F3?	-----	104 8	
049 RTN		105 +	
050 CF0		106 ST0C	
051 GSB9		107 ST05	
052 RCL2		108 F0?	
053 X ²		109 GT07	Is flow turbulent?
054 X		110 *LBL8	
055 RCL4		111 4	
056 X		112 6	

REGISTERS									
0 v	1 Re	2 v	3 L	4 ΔP	5 $1/\sqrt{f}$	6 D/ ϵ	7 1.737	8 $K_T/4$	9 ν, μ
S0	S1	S2	S3	S4	S5	S6	S7	S8	S9
A ρ	B Used	C $1/\sqrt{f_0}$	D D	E ϵ	I				

AUTHOR

113	RCL2					169	CMS				
114	RCLD					170	3				
115	x					171	X&Y?				
116	RCL9					172	GT02				
117	=					173	*LBL7				
118	STO1					174	RCL5				
119	2					175	1/X				
120	3					176	X²				
121	0					177	RCL3				
122	0					178	x				
123	X&Y?					179	RCLD				
124	GT02					180	=				
125	R4					181	RCL6				
126	=					182	+				
127	JX					183	2				
128	1/X					184	x				
129	STO5					185	RCL4				
130	GT0?					186	RCLA				
131	*LBL2					187	=				
132	RCLC					188	X=V				
133	RCL5					189	F0?				
134	-					190	GT00				
135	4					191	RTN				
136	.					192	*LBL0				
137	6					193	=				
138	7					194	IX				
139	RCL6					195	STO2				
140	x					196	RTN				
141	RCL1										
142	=										
143	RCL5										
144	x										
145	1										
146	+										
147	STOB										
148	LN										
149	RCL7										
150	x										
151	-										
152	RCLB										
153	1/X										
154	CMS										
155	1										
156	+										
157	RCL7										
158	x										
159	RCL5										
160	=										
161	1										
162	+										
163	=										
164	ST+5										
165	RCL5										
166	=										
167	ABS										
168	EEX										

Iterate to find
 $\frac{1}{\sqrt{f}}$ for turbulent flow.

Finish v calculation.

Start calculation of ΔP or v.

HEAT EXCHANGERS (Card 1)

TITLE

001 #LBLa	Store T_{cin} .	057 RCL1							
002 ST02		058 -							
003 RTN		059 CHS							
004 #LBLb	Store C_c .	060 RTN							
005 x		061 #LBLc	Calculate E from T_{co} .						
006 ST03		062 ST05							
007 RTN		063 GSB1							
008 #LBLc	Store T_{hin} .	064 RCL4							
009 ST01		065 RCL7							
010 RTN		066 ÷							
011 #LBLd	Store C_h .	067 RCL1							
012 x		068 RCL5							
013 ST04		069 -							
014 RTN		070 x							
015 #LBLd	Clear flag 1 for counter	071 RCL1							
016 F1?	flow, set for parallel flow.	072 RCL2							
017 GT00		073 -							
018 0		074 ÷							
019 SF1		075 ST05							
020 RTN		076 RTN							
021 #LBL0		077 #LBL0	Calculate AU for $C_{min}/$						
022 1		078 X#0?	$C_{max} = 0$.						
023 CF1		079 GT00							
024 RTN		080 1							
025 #LBLA	Calculate AU from E .	081 RCL5							
026 ST05		082 -							
027 GSB1		083 LN							
028 GSB0		084 CHS							
029 ST08		085 RTN							
030 RTN		086 #LBL2	Calculate E for $C_{min}/$						
031 #LBLB	Calculate q from AU.	087 X#0?	$C_{max} = 0$.						
032 ST08		088 GT02							
033 GSB1		089 1							
034 GSB2		090 RCL8							
035 RCL7		091 CHS							
036 x		092 e ^x							
037 RCL1		093 -							
038 RCL2		094 RTN							
039 -		095 #LBL1	Store C_{min} and $C_{min}/$						
040 x		096 RCL3	C_{max} .						
041 ST06		097 RCL4							
042 RTN		098 X>Y?							
043 #LBLC	Calculate T_{co} from q .	099 X<Y							
044 ST06		100 ST07							
045 RCL3		101 X<Y							
046 ÷		102 ÷							
047 RCL2		103 ST00							
048 +		104 RTN							
049 RTN									
050 #LBLD	Calculate T_{ho} from T_{co} .								
051 RCL2									
052 -									
053 RCL3									
054 x									
055 RCL4									
056 ÷									
REGISTERS									
0 C_{min}/C_{max}	1 T_{hin}	2 T_{cin}	3 C_c	4 C_h	5 E	6 q	7 C_{min}	8 AU	9 C_{max}
S0	S1	S2	S3	S4	S5	S6	S7	S8	S9
A	B	C	D	E	F	G	H	I	J

(Parallel-Flow and Counter-Flow)

DATE _____

AUTHOR _____

113	*LBL0	Counter-flow AU	169	e*	
114	F1?	calculations.	170	1	
115	GT08		171	XZY	
116	RCL5		172	-	
117	1/X		173	LSTX	
118	-		174	RCL0	
119	1		175	x	
120	LSTX		176	1	
121	-		177	XZY	
122	÷		178	-	
123	LN		179	X=0?	
124	1		180	GT09	
125	RCL0		181	÷	
126	-		182	RTN	
127	X=0?		183	*LBL9	Counter-flow E calculation
128	GT07		184	RCL6	where $C_{min}/C_{max} = 1$.
129	÷		185	RCL7	
130	RCL7		186	÷	
131	x		187	ENT↑	
132	RTN		188	ENT↑	
133	*LBL7		189	1	
134	RCL5	Counter-flow for $C_{min}/$	190	+	
135	1	$C_{max} = 1$.	191	÷	
136	RCL5		192	RTN	
137	-		193	*LBL8	Parallel-flow E
138	÷		194	1	calculation.
139	RCL7		195	+	
140	x		196	RCL8	
141	RTN		197	RCL7	
142	*LBL8	Parallel-flow AU	198	÷	
143	RCL0	calculation.	199	x	
144	1		200	CHS	
145	+		201	e*	
146	RCL5		202	CHS	
147	x		203	1	
148	CHS		204	+	
149	1		205	1	
150	+		206	RCL0	
151	LN		207	+	
152	CHS		208	÷	
153	1		209	RTN	
154	RCL0				
155	+				
156	÷				
157	RCL7				
158	x				
159	RTN				
160	*LBL2	Counter flow E calculation.			
161	F1?				
162	GT08				
163	1				
164	-				
165	RCL8				
166	RCL7				
167	÷				
168	x				

LABELS					FLAGS	SET STATUS		
A	B	C	D	E	0	FLAGS		DISP
E→AU	AU→q	q→T _{co}	T _{co} →T _{ho}	T _{ho} →E	0			
T _{co}	m _c T _{co}	T _{hin}	m _h T _{co}	CNT?	1	CNT?		
E→AU	C _{min}	AU→E	3	4	2			
5	6	C _{min} /C _{max} =1	8 parallel	9 C _{min} /C _{max} =1	3			

ON OFF		TRIG		DISP	
0	☐ ☒	DEG	☒	FIX	☒
1	☒ ☐	GRAD	☐	SCI	☐
2	☐ ☒	RAD	☐	ENG	☒
3	☐ ☒			n	

TITLE

[illegible]

(Side 2: Cross-Flow)

DATE _____

AUTHOR _____

113	*LBL0	Calculate AU for cross-flow.	169	e*	
114	FIX		170	CHS	
115	0		171	1	
116	STOA		172	+	
117	1		173	PTN	
118	RCL5				
119	CHS				
120	STOD				
121	+				
122	LN				
123	CHS				
124	STDS				
125	*LBL6				
126	RCL8				
127	GSB2				
128	RCL5				
129	-				
130	STOB				
131	RCLA				
132	RCL8				
133	STOA				
134	-				
135	RCLD				
136	RCLB				
137	STOD				
138	-				
139	÷				
140	x				
141	ST-8				
142	RCL8				
143	÷				
144	RND				
145	X#0?				
146	GT06				
147	RCL8				
148	RTN				
149	*LBL2	Calculate E for cross-flow.			
150	RCL8				
151	RCL7				
152	+				
153	ENT†				
154	ENT†				
155	.				
156	2				
157	2				
158	Y*				
159	RCL0				
160	÷				
161	÷				
162	LSTX				
163	X2Y				
164	CHS				
165	e*				
166	1				
167	-				
168	x				

LABELS					FLAGS	SET STATUS			
A	B	C	D	E	0	FLAGS		TRIG	DISP
a	b	c	d	e	1	ON	OFF		
0 E→AU	1	2 AU→E	3	4	2	0	☐	DEG ☐	FIX ☐
5	Iterate	7	8	9	3	1	☐	GRAD ☐	SCI ☐
						2	☐	RAD ☐	ENG ☐
						3	☐		n _____



1000 N.E. Circle Blvd., Corvallis, OR 97330