

HEWLETT  PACKARD

P-65

SURVEYING PAC 1

HEWLETT  PACKARD

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INTRODUCTION

Programs for your HP-65 Surveying Pac I have been selected to provide solutions for many of the day-to-day problems you encounter.*

In general, the programs are grouped into common problem areas of traversing, curves, triangles and intersections, field reductions, predetermined area and earthwork.

Included in Surveying Pac I are 34 prerecorded magnetic cards, a card case, 20 pocket instruction cards, and this instruction booklet with program descriptions, formulas, example problems, user instructions and program listings.

We are confident that you will find this pac useful, and we welcome any comments or suggestions you may have.

*This pac is written using North American surveying conventions.

FORMAT OF USER INSTRUCTIONS

The following is an example of a set of user instructions (from Field Angle Check – Surveying I-25A):

LINE	INSTRUCTIONS	DATA	KEYS	DISPLAY
1	Enter program			
2	Input Ref Az away from pt	Ref Az	A	
3	If angle right	Ang Rt	B	
4	If angle left	Ang Lt	CHS B	
5	If deflection right	Defl Rt	C	
6	If deflection left	Defl Lt	CHS C	
7	Optional: Compute course brg		D	Brg
8	Optional: Compute quad code		R/S	Quad
9	Optional: Compute azimuth		R/S	Az
(Repeat lines 3-9 for each course)				
10	Compute angular error		E	Ang Error
11			R/S	Ang Corr

If checking traverse between two points, the closing reference azimuth is entered via key A; angular error is then obtained at line 10.

To run another problem, press **F1** **EF1** then return to line 2.

The instructions read from left to right starting with line 1; follow any indicated operations in this order. Lines having no numbers contain special notes to the user and are in parentheses under the INSTRUCTIONS column. An example is the comment between lines 9 and 10.

Always move sequentially from line to line unless a comment in the INSTRUCTIONS column indicates otherwise. Thus, the comment after line 9, "Repeat lines 3-9 for each course", means to return to line 3 following the instructions indicated until all necessary data has been entered. If there were no more courses, the user would proceed to line 10 for further instructions.

Information under the DATA column will be the instruction to enter a number or value, even though in many cases there is not a comment given in the INSTRUCTIONS column.

Generally, where an instruction is designated as "Optional", the results have already been computed and stored. Thus, skipping optional path may save time by not displaying results but does not affect calculations.

The DISPLAY column indicates results where applicable. In some cases, the calculator display may show a value which is an intermediate factor used in final calculations and may be ignored.

The function keys A through E are used for entering data and displaying solutions. Keys to the left are used for data entry and those to the right for solutions. Solution keys are always indicated by "SOLN". Data is entered by entering the value and pressing the appropriate function key. Solutions are obtained by first pressing the appropriate function key and then, if the particular solution consists of multiple values, pressing the **R/S** key successively until all the values have been displayed. The **R/S** key is never used for data entry.

POINTS TO REMEMBER

Turning the calculator off clears all storage registers, the operational stack, and program memory. Neither the storage registers nor the operational stack is disturbed when a program is loaded into the calculator.

When running successive problems with one program without turning the calculator off, clear the storage registers by pressing **[1] [REG]**. To insure that the program restarts execution properly, press **RUN** after **[1] [REG]**. The same rules apply when running one program after another unless data is utilized which was stored by a previous program. Failure to perform these steps may result in incorrect solutions.

When working with problems which involve the display of degrees, minutes, and seconds as output, set the decimal at four places (press **DSP** **[.]** **[4]**) to enable full display of minutes and seconds.

Input degrees, minutes, seconds in the form DDD.MMSS, i.e., 60 degrees, 05 minutes and 12 seconds is displayed as 60.0512.

CLX may not be used as an equivalent to an input of zero.

Do not perform manual calculations between program execution steps. In many cases the stack contains values necessary for program execution.

Quadrant codes for bearings are as follows: NE is 1, SE is 2, SW is 3, and NW is 4.



ENTERING A PROGRAM

From the card case supplied with this application pac, select a program card.

Set W/PRGM-RUN switch to RUN.

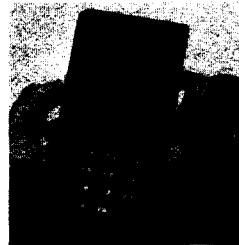
Turn the calculator ON. You should see 0.00

Gently insert the card (printed side up) in the right, lower slot as shown. When the card is part way in, the motor engages it and passes it out the left side of the calculator. Sometimes the motor engages but does not pull the card in. If this happens, push the card a little farther into the machine. Do not impede or force the card; let it move freely. (The display will flash if the card reads improperly. In this case, press **CLX** and reinsert the card.)



When the motor stops, remove the card from the left side of the calculator and insert it in the upper "window slot" on the right side of the calculator.

The program is now stored in the calculator. It remains stored until another program is entered or the calculator is turned off.



FIELD ANGLE TRAVERSE

FIELD ANGLE TRAVERSE			SURV 1-01B
BEG N-E REF AZ	ANGLE LT-RT	DEFL LT-RT	DIST. ZNTH ANG
N-E AREA SOLN			

This program will accept angles right, angles left, deflections right and deflections left as well as horizontal or slope distances. The coordinates of the next point are calculated, and area in square feet and acres are available upon completion of the traverse. Traversing between two known points is accomplished through a second program in which the coordinates of the closing point are entered. This same secondary program, Closure for Field Angle and Bearing Traverses (*Surveying 1-3A*), also computes area, closure for bearing and distance, total distance traversed and precision ratio.

Slope angles are assumed to be entered as zenith angles. To change the program to use vertical angles, the following sequence must be followed:

1. Enter program
2. Press **100 D**
3. Switch to program mode (W/PRGM)—14 should appear in the display
4. Press **BSI** (single step) three times—09 should appear in the display
5. Press **9 DEL** (delete)—09 should appear in the display
7. Press **BSI** eleven times—04 should appear in the display
7. Press **9 DEL** —31 should appear in the display
8. Press **5** —05 should appear in the display
9. Record changed program by inserting blank card in reader
10. Switch back to run mode
11. Enter changed program and test

Formulas used:

$$H \text{ Dist} = S \text{ Dist} \sin (\text{Znht ang})$$

$$N_{i+1} = N_i + H \text{ Dist} \cos Az$$

$$E_{i+1} = E_i + H \text{ Dist} \sin Az$$

$$\text{Area} = \frac{1}{2}[(N_2 + N_1)(E_2 - E_1) + (N_3 + N_2)(E_3 - E_2) + \dots + (N_n + N_1)(E_1 - E_n)]$$

Where: N, E = Northing, easting of a point

Subscript i refers to current point

Subscript n refers to next to last point

Numeric subscript refers to point number

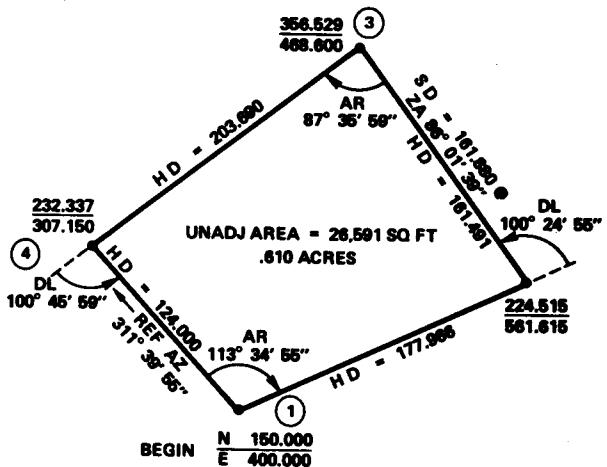
Az = Azimuth of a course

$H \text{ Dist}$ = Horizontal distance

$S \text{ Dist}$ = Slope distance

Znht ang = Zenith angle

Example:



Calculated Ending Coordinates $N = 149.905$
 $E = 399.783$

In this example, the Field Angle Traverse program is used until the calculated ending coordinates are established. The Closure for Field Angle and Bearing Traverse program is then loaded and the closing coordinates are entered ($N = 150.00$ and $E = 400.00$). From there, the remaining closure information can be obtained—see instructions for the Closure program (*Surveying 1-3A*).

Closure distance = 0.237
 Error bearing = S 66° 19' 43" W
 Distance traversed = 667.147
 Precision = 2814

NOTE: If registers for the Closure for Field Angle and Bearing Traverse program (*Surveying 1-3A*) have been manually loaded, variations in the above may occur due to rounding.

LINE	INSTRUCTIONS	DATA	KEYS	DISPLAY
1	Enter program			
2		Begin N	A	Begin N
3		Begin E	A	Begin E
4	Input ref az away from pt	Ref Az	A	
5	If angle right	AR	B	
6	If angle left	AL	CHS B	
7	If deflection right	DR	C	
8	If deflection left	DL	CHS C	
9	Input distance (SD or HD)	Dist	D	
10	If horizontal distance		D	H Dist
11	If slope distance	Zn Ang	D	H Dist
12	Compute Coords		E	N
13	(Repeat lines 5-13 for successive courses. Lines 14 & 15 should be executed only after completion of polygon traverse.)		R/S	E
14	Optional: Compute sq ft		R/S	Sq Ft
15	Optional: Compute acres		R/S	Acres

For closure information and/or traverse between two points, proceed to program Closure for Field Angle & Bearing Traverse (*Surveying 1-3A*). To repeat field angle traverse go to line 2

BEARING TRAVERSE

BEARING TRAVERSE SURV 1-02A
 BEG N-E BRG QUAD DIST- N-E-AREA
 ZNTH ANG SOLN

This program uses bearings and horizontal or slope distances to calculate coordinates.

Traversing between two known points is accomplished through a second program in which the coordinates of the closing point are entered. This same secondary program, Closure for Field Angle and Bearing Traverse (*Surveying 1-3A*), also supplies area, closure bearing and distance, total distance traverses and precision ratio.

Slope angles are assumed to be entered as zenith angles. To change the program to use vertical angles, the following sequence must be followed:

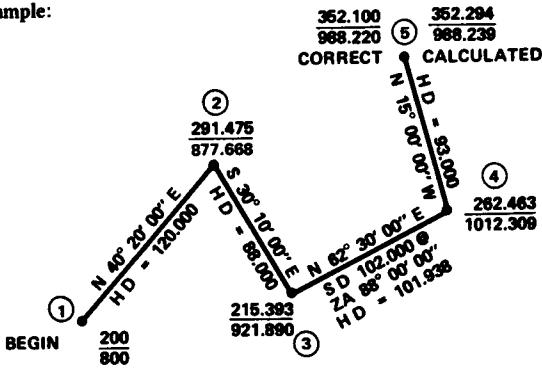
1. Enter program
2. Press **GTO D**
3. Switch to program mode (W/PRGM)—14 should appear in the display
4. Press **SST** (single step) three times—09 should appear in the display
5. Press **[9] DEL** (delete)—09 should appear in the display
6. Press **SST** 10 times—04 should appear in the display
7. Press **[9] DEL**—31 should appear in the display
8. Press **[5]**—05 should appear in the display
9. Record changed program by inserting blank card in reader slot
10. Switch back to run mode
11. Enter changed program and test

Formulas used:

$$\begin{aligned} H \text{ Dist} &= S \text{ Dist} \sin (\text{Znht ang}) \\ N_{i+1} &= N_i + H \text{ Dist} \cos Az \\ E_{i+1} &= E_i + H \text{ Dist} \sin Az \\ \text{Area} &= \frac{1}{2} [(N_2 + N_1)(E_2 - E_1) + (N_3 + N_2)(E_3 - E_2) + \\ &\quad \dots + (N_n + N_1)(E_1 - E_n)] \end{aligned}$$

Where:
 N, E = Northing, easting of a point
 Subscript i refers to current point
 Subscript n refers to next to last point
 Numeric subscript refers to point number
 Az = Azimuth of a course
 H Dist = Horizontal distance
 S Dist = Slope distance
 Znht ang = Zenith angle

Example:



In this example, the Bearing Traverse program is used until the calculated ending coordinates are established. The Closure for Field Angle & Bearing Traverse program is then loaded and the closing coordinates are entered (N = 352.100 and E = 988.220). From there, the remaining closure information can be obtained -- see instructions for the Closure program (*Surveying 1-3A*).

$$\begin{aligned} \text{Closure distance} &= 0.195 \\ \text{Error bearing} &= N 5^\circ 41' 31'' E \\ \text{Distance traversed} &= 402.938 \\ \text{Precision} &= 2068 \end{aligned}$$

NOTE: If registers for the Closure for Field Angle and Bearing Traverse program (*Surveying 1-3A*) have been manually loaded, variations in the above may occur due to rounding.

Notes

LINE	INSTRUCTIONS	DATA	KEYS	DISPLAY
1	Enter program			
2		Begin N	A	Begin N
3		Begin E	A	Begin E
4	Input bearing	Brg	B	
5	Input quadrant code	Quad	C	
6	Input distance (SD or HD)	Dist	D	
7	If horizontal distance		D	H Dist
8	If slope distance	Zn Ang	D	H Dist
9	Compute coords		E	N
10			R/S	E
(Repeat lines 4-10 for successive courses. Lines 11 & 12 should be executed only after completion of polygon traverse.)				
11	Optional: Compute sq ft		R/S	Sq Ft
12	Optional: Compute acres		R/S	Acres

For closure information and/or traverse between two points, proceed to program Closure for Field Angle & Bearing Traverse (Surveying 1-3A).

To restart this program after an error or for new data press **■** then **1** **RECALL** and go to line 2.

CLOSURE FOR FIELD ANGLE AND BEARING TRAVERSES

CLOSURE FOR FIELD ANGLE AND BEARING TRAVERSES				SURV 1-03A
CLOSING N-E	AREA SOLN	DIST-BRG SOLN	TOT DIST SOLN	PRCSN SOLN

This program, used in conjunction with either the Field Angle Traverse program (*Surveying 1-1B*) or the Bearing Traverse program (*Surveying 1-2A*), computes area, closure bearing and distance, total distance traversed, and precision ratio.

Key **A** is used only for entering the closing coordinates in the case of a traverse between two points (i.e., not a polygon).

If this program is not used immediately after the Field Angle Traverse program (*Surveying 1-1B*) or the Bearing Traverse program (*Surveying 1-2A*), or if the storage registers have been altered, or if the calculator power has been turned off since either of the traverse programs were run, enter the following data into the specified storage registers (this is done by entering the data in the display and pressing **STO** followed by the register number for each of the five parameters):

REGISTER	PARAMETERS TO BE STORED
2	Total distance traversed
4	2 X area (sq. ft.)
5	Correct closing easting
6	Correct closing northing
7	Calculated ending easting
8	Calculated ending northing

Formulas used:

$$\text{Closure distance} = \sqrt{(N_c - N_L)^2 + (E_c - E_L)^2}$$

$$\text{Precision ratio} = \Sigma \text{Dist}/\text{Closure distance}$$

$$\text{Error bearing} = \tan^{-1} \frac{E_c - E_L}{N_c - N_L}$$

Where: N_c, E_c = Correct closing northing and easting

N_L, E_L = Calculated closing northing and easting

ΣDist = Total length of traverse

Example:

Values stored in the registers given below are those stored by the Field Angle Traverse (*Surveying 1-1B*) example.

REGISTER VALUE

2	667.147	Total distance traversed
4	53182.000	Area x 2 (sq ft)
5	400.000	Correct closing easting
6	150.000	Correct closing northing
7	399.783	Calculated ending easting
8	149.905	Calculated ending northing

Using these values, the closure information is calculated.

$$\text{Area} = 26,591 \text{ sq ft} = 0.610 \text{ Acres}$$

$$\text{Closure distance} = 0.237 \text{ feet}$$

$$\text{Error bearing} = S 66^\circ 19' 43'' W^*$$

$$\text{Total distance traversed} = 667.147 \text{ feet}$$

$$\text{Precision} = 2814^*$$

*These values will not be exact if values are stored manually. This is because of rounding of the input values.

LINE	INSTRUCTIONS	DATA	KEYS	DISPLAY
1	Enter program			
	(Skip lines 2-3 if registers loaded			
	manually)			
2	Input correct closing N	Close N	A	Close N
3	Input correct closing E	Close E	A	Close E
4	Optional: If polygon recall			
	area		B	Sq Ft
5	Optional		R/S	Acres
6	Compute closure dist		C	Dist
7	Compute error brg		R/S	Brg
8	Compute quad code		R/S	Quad
9	Compute total dist traversed		D	Tot Dist
10	Compute precision ratio*		E	Prcsn

*Flashing zeros indicate perfect closure

INVERSE FROM COORDINATES

INVERSE FROM COORDINATES			SURV 1-04A		
BEG N-E	NEXT N-E	DIST SOLN	BRG-QUAD SOLN	AREA-TOT DIST-SOLN	5

This program uses coordinates to calculate distance and bearing between points of a traverse. The area in square feet and acres, plus a summation of distance inversed are also computed.

Formulas used:

$$H \text{ Dist} = \sqrt{(N_i - N_{i-1})^2 + (E_i - E_{i-1})^2}$$

$$Az = \tan^{-1} \frac{E_i - E_{i-1}}{N_i - N_{i-1}}$$

$$\text{Area} = \frac{1}{2} [(N_2 + N_1)(E_2 - E_1) + (N_3 + N_2)(E_3 - E_2) + \dots + (N_n + N_1)(E_1 - E_n)]$$

Where: N, E = Northing, easting of a point

Subscript i refers to current point

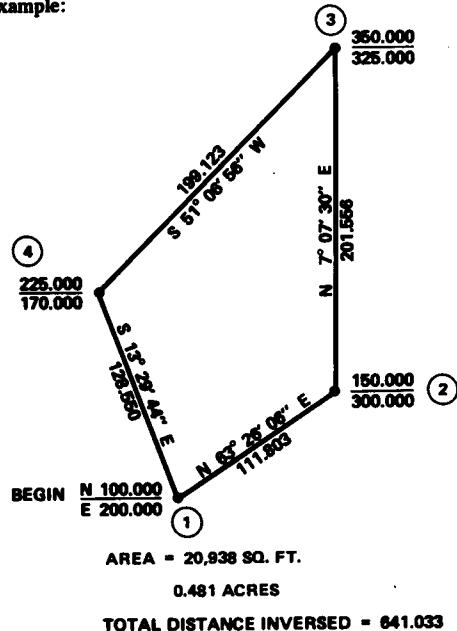
Subscript n refers to next to last point

Numeric subscript refers to point number

H Dist = Horizontal distance

Az = Azimuth of a course

Example:



LINE	INSTRUCTIONS	DATA	KEYS	DISPLAY
1	Enter program			
2	Beg N		A	Begin N
3	Beg E		A	Begin E
4	Next N		B	Lat.
5	Next E		B	Dep.
6	Compute distance		C	Dist
7	Compute bearing		D	Brg
8	(Repeat lines 4-8 for successive courses.)		R/S	Quad
9	Optional: Compute area		E	Sq. Ft.
10	Optional:		R/S	Acres
11	Optional: total dist inversed		R/S	Tot Dist

To compute area correctly, lines 4-8 must be executed for each leg.

To repeat Inverse From Coordinates go to line 2.

SIDESHOTS

SIDE SHOTS			SURV 1-05B		
REF BRG- OCC N-E	ANGLE LT-RT	DIFFL LT-RT	DIST. ZNTH ANG N-ESOLN	SIDESHOT	END

This program may be used alone or in conjunction with one of the traverse programs (*Surveying 1-1B* or *Surveying 1-2A*). Used as a stand-alone program, the reference bearing from a backsight is entered along with the coordinates of the occupied point. If used with a traverse program, these steps are omitted and data stored by a traverse program is used. In either case, the stored data is not destroyed, and the traverse operation may be carried out from the point occupied.

Slope angles are assumed to be entered as zenith angles. To change the program to use vertical angles, the following sequence must be followed:

1. Enter program
2. Press **GIG D**
3. Switch to program mode (W/PRGM) - 14 should appear in the display
4. Press **SSI** (single step) four times - 03 should appear in the display
5. Press **9 DEL** (delete) - 44 should appear in the display
6. Press **SSI** 15 times - 04 should appear in the display
7. Press **9 DEL** - 31 should appear in the display
8. Press **5** - 05 should appear in the display
9. Record changed program by inserting blank card in reader slot.
10. Switch back to run mode
11. Enter changed program and test

Formulas used:

$$H \text{ Dist} = S \text{ Dist} \sin (\text{Znht ang})$$

$$N = N_i + H \text{ Dist} \cos Az$$

$$E = E_i + H \text{ Dist} \sin Az$$

Where: N, E = Northing, easting of sideshot

N_i, E_i = Northing, easting of occupied point

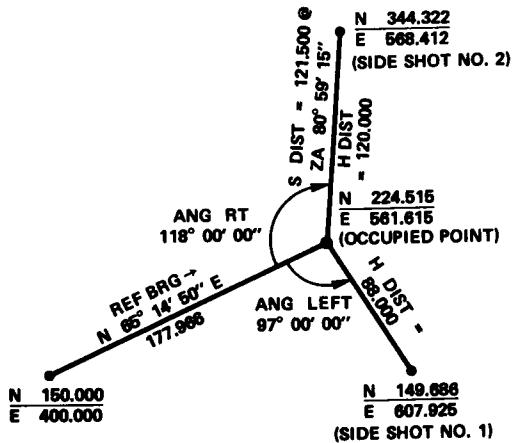
$H \text{ Dist}$ = Horizontal distance

$S \text{ Dist}$ = Slope distance

Znht ang = Zenith angle

Az = Azimuth to side shot

Example:



LINE	INSTRUCTIONS	DATA	KEYS	DISPLAY
1	Enter program			
	(Skip lines 2-5 if using in con-			
	junction with a traverse program)			
2	Input Ref Brg into occ pt	Ref Brg	A	
3		Quad	A	
4		Occ N	A	
5		Occ E	A	
6	If angle right	Ang Rt	B	
7	If angle left	Ang Lt	CHS B	
8	If deflection right	Defl Rt	C	
9	If deflection left	Defl Lt	CHS C	
10		Dist	D	
11	If horizontal distance		D	H Dist
12	If slope distance	Zn Ang	D	H Dist
13	Compute sideshot coordinates		E	N
			R/S	E

To execute another side shot from the same point go to line 6,
for a different point go to line 2.

Notes



COORDINATE TRANSFORMATION

COORDINATE TRANSFORMATION			SURV 1-06A		
OLD N-E	ROTATION	SCALE	NEXT	TRANSFRMD	
NEW N-E	ANGLE	FACTOR	N-E	N-E SOLN	

This program translates, rotates, and rescales coordinates. Traverse rotation angle is entered as a positive value for counterclockwise rotation and negative for clockwise rotation. The translation factors are calculated by entering old and new grid system coordinates for the same point; rotation is also about this point.

Formulas used:

$$Az_R = \phi + \tan^{-1} \frac{E_i - E_p}{N_i - N_p}$$

$$H\ Dist_S = S \sqrt{(N_i - N_p)^2 + (E_i - E_p)^2}$$

$$N = N_p + H\ Dist_S \cos(Az_R) + T_N$$

$$E = E_p + H\ Dist_S \sin(Az_R) + T_E$$

$$T_N = N_{T_1} - N_p$$

$$T_E = E_{T_1} - E_p$$

Where: Az_R = Rotated azimuth

ϕ = Rotation angle

N_i, E_i = Northing, easting of current point before transformation

N_p, E_p = Original northing, easting of pivot point

$H\ Dist_S$ = Scaled horizontal distance

S = Scale factor

N, E = Northing, easting after transformation

N_{T_1}, E_{T_1} = Northing, easting of pivot point after transformation

Example:

Coordinates before transformation are those computed by Compass Rule Adjustment (*Surveying 1-7A*).

COORDINATES IN OLD SYSTEM	COORDINATES IN NEW SYSTEM
N 150.000*	N 100.000*
E 400.000	E 350.000
N 224.540	N 165.977
E 561.673	E 515.353
N 356.577	N 302.698
E 468.710	E 429.427
N 232.414	N 187.151
E 307.327	E 261.767

* Rotated about this point

Rotation Angle = $-3^\circ 00' 00''$

Scale Factor = 1.00

LINE	INSTRUCTIONS	DATA	KEYS	DISPLAY
1	Enter program			
	(Skip lines 4-5 if no translation is desired.)			
2	Input N in old system	Old N	A	
3	Input E in old system	Old E	A	
4	Input N in new system	New N	A	
5	Input E in new system	New E	A	
6	Optional: Input rotation angle	Angle	B	
7	Input scale factor	Scale	C	
8		Next N	D	
9		Next E	D	
10	Compute transformed coord		E	N
11			R/S	E

Return to line 8 for next N,E. For new case start at line 2.

COMPASS RULE ADJUSTMENT*

COMPASS RULE ADJUSTMENT		SURV 1-07A	
UNADJ N	UNADJ E	ADJ N SOLN	ADJ E SOLN

This program adjusts a traverse by the compass rule. It is intended to follow the program Closure For Field Angle and Bearing Traverses (*Surveying 1-3A*). However, if the correct coordinates of the last point, the computed coordinates of the last point, and the total distance traversed are known, these parameters can be used in lieu of executing the closure program.

If this program is not used immediately after Closure for Field Angle and Bearing Traverse (*Surveying 1-3A*) or the storage registers have been altered or the calculator turned off since the closure program was run, enter the following data into the specified storage registers. (This is done by entering the data in the display and pressing **STO** followed by the register number for each of the five parameters).

REGISTER	PARAMETERS TO BE STORED
2	Total distance traversed
5	Correct closing easting
6	Correct closing northing
7	Calculated ending easting
8	Calculated ending northing

The Inverse From Coordinates program (*Surveying 1-4A*) may be used to obtain adjusted bearings, distances and area.

*This is also known as the Bowditch adjustment

To adjust a traverse between two points (non-polygon), run the Closure program (*Surveying 1-3A*) as usual. Then upon entering the Compass Rule Adjustment program:

Press **A**

Enter starting northing, press **STO** **2**, **STO** **6**

Enter starting easting, press **STO** **1**, **STO** **5**

Proceed to line 2 of the operating instructions.

Note: Coordinates must be reentered in the same sequence as originally traversed, starting at the second point.

Formulas used:

$$C_L = \frac{(\Delta N) (\text{Dist})}{\Sigma \text{Dist}} \quad C_D = \frac{(\Delta E) (\text{Dist})}{\Sigma \text{Dist}}$$

Where: C_L = Correction to latitude of a course
 C_D = Correction to departure of a course
 ΔN = Closing latitude
 ΔE = Closing departure
 Dist = Length of course to be corrected
 ΣDist = Total length of traverse

Example:

Values stored in the registers given below are those stored by the Field Angle Traverse (*Surveying 1-1B*) example.

REGISTER	VALUE	
2	667.147	Total distance traversed
5	400.000	Correct closing easting
6	150.000	Correct closing northing
7	399.783	Calculated ending easting
8	149.905	Calculated ending northing

Using these values, the compass rule method of adjustment yields the following results:

POINT NO.	UNADJUSTED COORDINATES	ADJUSTED COORDINATES
2	N = 224.515 E = 561.615	N = 224.540 E = 561.673
3	N = 356.529 E = 468.600	N = 356.577 E = 468.710
4	N = 232.337 E = 307.150	N = 232.414 E = 307.327
Ending & Beginning	N = 149.905 E = 399.783	N = 150.000 E = 400.000

LINE	INSTRUCTIONS	DATA	KEYS	DISPLAY
1	Enter program			
2		Unadj N	A	
3		Unadj E	B	
4	Compute adjusted coordinates		C	Adj N
5			D	Adj E

Return to line 2 for next point.

TRANSIT RULE ADJUSTMENT

TRANSIT RULE ADJUSTMENT			SURV 1-08A	
START	UNADJ N	UNADJ E	PRE-ADJUST	ADJ N-E SOLN

This program adjusts a traverse by the transit rule method. It is intended to follow the program Closure for Field Angle or Bearing Traverses (*Surveying 1-3A*).

Because of storage register limitation and requirements of the transit rule method, it is necessary to enter the unadjusted coordinates twice.

If the storage registers have been altered in any way since one of the traverse programs or the closure program was run, store the following data in the specified registers (this is done by entering the data in the display and pressing **STO** followed by the register number for each of the parameters).

REGISTER	PARAMETER TO BE STORED
5	Correct closing easting
6	Correct closing northing
7	Calculated ending easting
8	Calculated ending northing

The Inverse from Coordinates program (*Surveying 1-4A*) may be used to obtain bearings, distances and area from the adjusted coordinates. The starting and closing coordinates must be the same.

NOTE: Coordinates must be reentered in the same sequence as originally traversed, starting at the second point.

Formulas used:

$$C_L = \Delta N | L | / \Sigma | L |$$

$$C_D = \Delta E | D | / \Sigma | D |$$

Where: C_L = Correction to latitude of a course

C_D = Correction to departure of a course

ΔN = Closing latitude

ΔE = Closing departure

L = Latitude of a course

D = Departure of a course

Example:

Values stored in the registers given below are those stored by the Field Angle Traverse (*Surveying 1-1B*) example.

REGISTER	VALUE	
5	400.000	Correct closing easting
6	150.000	Correct closing northing
7	399.783	Calculated ending easting
8	149.905	Calculated ending northing

Using these values, the transit rule method of adjustment yields the following results:

POINT NO.	UNADJUSTED COORDINATES	ADJUSTED COORDINATES
2	N = 224.515 E = 561.615	N = 224.532 E = 561.684
3	N = 356.529 E = 468.600	N = 356.576 E = 468.709
4	N = 232.337 E = 307.150	N = 232.413 E = 307.327
Ending & Beginning	N = 149.905 E = 399.783	N = 150.000 E = 400.000

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
1	Enter program			
2	Compute closing lat, dep (start)		A	Closing Lat
3	Optional: Display closing departure		x-y	Closing Dep
4		Unadj N	B	
5		Unadj E	C	
6	Compute sum of absolute values of latitudes and departures (pre-adjust). (Repeat lines 4-8)		D	
	until last point has been pro- cessed, then proceed to line 7.)			
7		Unadj N	B	
8		Unadj E	C	
9	Compute adjusted coords		E	Adj N
			R/S	Adj E

Repeat lines 7-9 until all coordinates have been entered and adjusted.

TWO INSTRUMENT RADIAL SURVEY

TWO INSTRUMENT RADIAL SURVEY SURV 1-09A

POINT 1	POINT 2	POINT 1	POINT 2	N-E	SOLN
N-E	N-E	BRG-DIST	BRG-DIST		

This program determines the coordinates of a point using a two instrument radial survey technique. The coordinates of the two instrument locations are entered. The bearing and distance to the target point are measured from each of the instrument locations. The solution makes two independent calculations of the coordinates of the target point and outputs the average coordinates of the target point. As an optional check, the program outputs the distance between the two calculated locations of the target point.

Formulas used:

$$N = [(N_1 + HD_1 \cos Az_1) + (N_2 + HD_2 \cos Az_2)]/2$$

$$E = [(E_1 + HD_1 \sin Az_1) + (E_2 + HD_2 \sin Az_2)]/2$$

Where: N, E = Northing, easting of target point

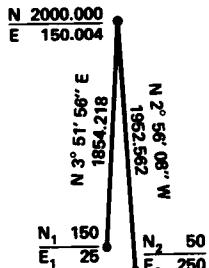
N_1, E_1 = Northing, easting of first instrument point

N_2, E_2 = Northing, easting of second instrument point

HD_i = Horizontal distance—point of origin is designated by subscript.

Az_i = Azimuth (converted from bearing)—point of origin is designated by subscript.

Example:



Data at Pt 1
Bearing $3^{\circ} 51' 56''$
Quad 1
Distance 1854.218

Data at Pt 2
Bearing $2^{\circ} 56' 08''$
Quad 4
Distance 1952.562

Distance between target point solutions = 0.001

LINE	INSTRUCTIONS	DATA	KEYS	DISPLAY
1	Enter program			
2		N_1	A	
3		E_1	A	
4		N_2	B	
5		E_2	B	
6		Brg 1	C	
7		Quad 1	C	
8		Dist 1	C	
9		Brg 2	D	
10		Quad 2	D	
11		Dist 2	D	
12	Compute coordinates		E	N
13			R/S	E
14	Optional: (straight line distance between the two target point solutions)		R/S	Distance

For successive points measured from the same instrument locations, return to line 6.
For new case go to line 2.

CURVE SOLUTION—GIVEN Δ & R OR Δ & T

Given the central angle and either the radius or tangent distance, this program computes four remaining parameters plus the sector, segment and fillet areas.

Formulas used:

$$T = R \tan(\frac{1}{2}\Delta)$$

$$C = 2T \cos(\frac{1}{2}\Delta)$$

$$R = T/\tan(\frac{1}{2}\Delta) = C/(2 \sin(\frac{1}{2}\Delta))$$

$$L = \Delta \pi R/180$$

$$\text{Sector area} = LR/2$$

$$\text{Segment area} = \text{Sector area} - \frac{1}{2} CR \cos(\frac{1}{2}\Delta)$$

$$\text{Fillet area} = T R - \text{Sector area}$$

Where: T = Tangent distance

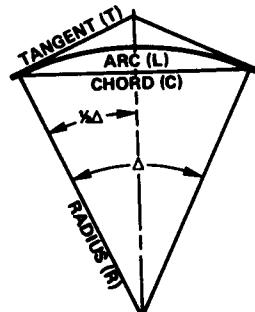
C = Chord length

L = Arc length

R = Radius

Δ = Central angle

Example:



$$R = 223.181$$

$$\Delta = 45^\circ 30' 23''$$

$$\frac{1}{2}\Delta = 22^\circ 45' 11''$$

$$C = 172.636$$

$$T = 93.602$$

$$L = 177.258$$

$$\text{Sector area } (\nabla) = 19,780$$

$$\text{Segment area } (\overbrace{\hspace{1cm}}) = 2,015$$

$$\text{Fillet area } (\overbrace{\hspace{1cm}}) = 1,110$$

LINE	INSTRUCTIONS	DATA	KEYS	DISPLAY
1	Enter program			
2			A	
3	If radius known*		R	B
4	If tangent known*		T	C
5	Optional: Compute area			D
6	Optional		R/S	
7	Optional		R/S	
8	Compute curve solution		E	R
9			R/S	
10			R/S	
11			R/S	
12			R/S	
13			R/S	

*Input radius or tangent, not both.

Lines 5-7 can be executed at any time after initial parameters have been input.

For new case go to line 2.

CURVE SOLUTION—GIVEN R & T OR R & L

CURVE SOLUTION-GIVEN R & T OR R & L				SURV 1-11A
RADIUS	TANGENT	ARC LENGTH	AREA SOLN	CURVE SOLN

Given the radius and either the tangent or arc length, this program computes four remaining parameters plus the sector, segment and fillet areas.

Formulas used:

$$\frac{1}{2}\Delta = \tan^{-1}(T/R) = \sin^{-1}(\frac{1}{2}C/R) = 90L/\pi R$$

$$T = R \tan \frac{1}{2}\Delta$$

$$C = 2 T \cos (\frac{1}{2}\Delta)$$

$$L = \Delta \pi R / 180$$

$$\text{Sector area} = LR/2$$

$$\text{Segment area} = \text{Sector area} - \frac{1}{2} C R \cos (\frac{1}{2}\Delta)$$

$$\text{Fillet area} = T R - \text{Sector area}$$

Where: T = Tangent Distance

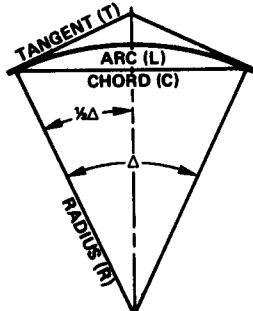
C = Chord length

L = Arc length

R = Radius

Δ = Central angle

Example:



$$\begin{aligned} R &= 223.181 \\ \Delta &= 45^\circ 30' 23'' \\ \frac{1}{2}\Delta &= 22^\circ 45' 11'' \\ C &= 172.636 \\ T &= 93.602 \\ L &= 177.258 \end{aligned}$$

$$\text{Sector area } (\triangle) = 19,780$$

$$\text{Segment area } (\square) = 2,015$$

$$\text{Fillet area } (\wedge) = 1,110$$

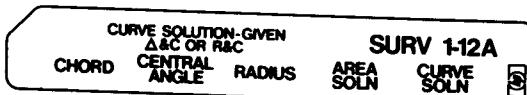
LINE	INSTRUCTIONS	DATA	KEYS	DISPLAY
1	Enter program			
2		Radius	A	
3	If tangent known*	T	B	
4	If arc length known*	L	C	
5	Optional: Compute area		D	Sec Area
6	Optional		R/S	Seg Area
7	Optional		R/S	Fil Area
8	Compute curve solution		E	R
9			R/S	Δ
10			R/S	$\frac{1}{2}\Delta$
11			R/S	C
12			R/S	T
13			R/S	L

*Input tangent or arc length, not both.

Lines 5-7 can be executed any time after initial parameters are entered.

For new case go to line 2.

CURVE SOLUTION—GIVEN Δ & C OR R & C



Given the chord length and either the central angle or radius, this program computes four remaining parameters plus the sector, segment and fillet areas.

Formulas used:

$$R = C/(2 \sin(\frac{1}{2}\Delta))$$

$$\Delta = 2 \sin^{-1}(1/2 C/R)$$

$$T = R \tan(\frac{1}{2}\Delta)$$

$$L = \Delta \pi R/180$$

$$\text{Sector area} = LR/2$$

$$\text{Segment area} = \text{Sector area} - \frac{1}{2} C R \cos(\frac{1}{2}\Delta)$$

$$\text{Fillet area} = T R - \text{Sector area}$$

Where: T = Tangent distance

C = Chord length

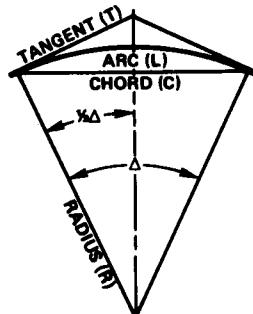
L = Arc length

R = Radius

Δ = Central angle



Example:



LINE	INSTRUCTIONS	DATA	KEYS	DISPLAY
1	Enter program			
2		C	A	
3	If central angle known*	Δ	B	
4	If radius known*	R	C	
5	Optional: Compute area	D		Sec Area
6	Optional	R/S		Seg Area
7	Optional	R/S		Fil Area
8	Compute curve solution	E		R
9		R/S		Δ
10		R/S		$\frac{1}{2}\Delta$
11		R/S		C
12		R/S		T
13		R/S		L

*Input central angle or radius, not both.

Lines 5-7 can be executed any time after initial parameters are entered.

For new case go to line 2.

ELEVATIONS ALONG A VERTICAL CURVE

ELEVATIONS ALONG A VERTICAL CURVE			SURV 1-13A		
BEG-END GRADE (%)	BEG STA ELEV & L	NEXT STATION	MAX-MIN SOLN	ELEV STA SOLN	(S)

This program computes elevation at any specified station along a vertical curve as well as the elevation at the highest or lowest point on the curve and the station at that point. Program inputs are beginning and ending grades, length of curve, the station and elevation at the beginning of the curve and station at which elevation is desired.

In the program, stations are entered in the form xxxx.xx for station xx + xx.xx. For example, 20 + 10.00 is entered as 2010.00.

Formulas used:

$$\text{Elevation at any station} = \frac{1}{2} AZ^2 + G_1 Z + E_0$$

$$\text{Distance in stations from beginning station to station of lowest elevation} = -G_1/A$$

Where: E_0 = Elevation at beginning of curve

Z = Distance in 100 foot stations - measured from beginning of curve

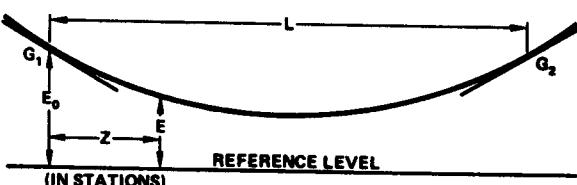
G_1 = Grade in % at beginning of curve

G_2 = Grade in % at end of curve

$A = 100(G_2 - G_1)/L$

L = Length of curve in feet

Example:



G_1 (Beginning Grade) = -1.065%
 G_2 (Ending Grade) = 1.600%
 L (Length of Curve) = 340 ft.
 E_0 (Elevation at G_1) = 614 ft.
 Beginning station = 17 + 00.00

STATION ELEVATION (E)

18 + 00.00	613.327
19 + 00.00	613.438
20 + 00.00	614.332
20 + 40.00	614.910

Station of lowest elevation = 18 + 35.87

Lowest elevation = 613.276

LINE	INSTRUCTIONS	DATA	KEYS	DISPLAY
1	Enter program			
2	Input begin grade in %	Grade 1	A	
3	Input end grade in %	Grade 2	A	
4	Input beginning station	Beg Sta	B	
5	Input beginning elevation	E_0	B	
6	Input curve length	L	B	
7	Input station	Sta	C	
8	If seeking max or min elev		D	
9	Compute elev solution		E	Elev
10			R/S	Sta

Lines 7-10 may be repeated if there are no changes in data entered in lines 2-6.

Lines 8-10 may be executed any time after initial curve data is entered.

For a new case go to line 2.

HORIZONTAL CURVE LAYOUT

HORIZONTAL CURVE LAYOUT SURV 1-14A					
RADIUS	PC STA	NEXT STA	DEFL. ANG.	CHORD SOLN	CHORD SOLN

Given the curve radius, the point of curvature station (P C) and the station on the curve, this program computes deflection angles from the tangent and long chord lengths from the point of curvature.

If regular stationing intervals are used, the short chord will remain constant, thus eliminating calculation of the chord for all but odd interval stations.

In the program, stations are entered in the form xxxx.xx for station xx + xx.xx. For example, 20 + 10.00 is entered as 2010.00.

Formulas used:

$$\text{Deflection/ft.} = 90/\pi R$$

$$\text{Deflection angle} = L \text{ (Deflection/ft.)}$$

$$\text{Short chord} = 2 R \sin (\text{Deflection angle})$$

Where: R = Radius

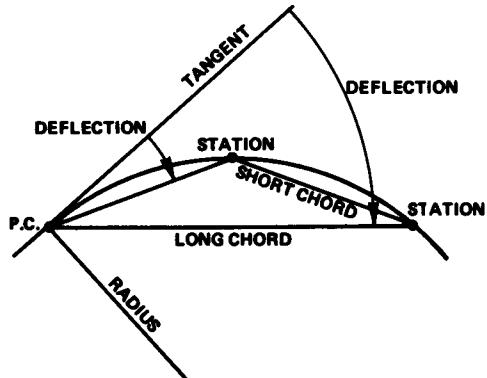
L = Arc length

Example:

$$\text{Radius} = 900.00 \text{ Ft.}$$

Station	Arc Length	Deflection	Long Chord
12 + 57.000	(Point of Curvature, PC)		
12 + 75.00	18.00	00° 34' 22"	18.00
12 + 88.50	31.50	01° 00' 10"	31.50
13 + 00.00	43.00	01° 22' 07"	43.00
13 + 25.00	68.00	02° 09' 52"	67.98
13 + 50.00	93.00	02° 57' 37"	92.96

Arc length = Difference in stations



LINE	INSTRUCTIONS	DATA	KEYS	DISPLAY
1	Enter program			
2		R	A	
3		PC Sta	B	
4		Sta	C	
5	Compute deflection angle		D	Defl Ang
6	Compute chord length		E	Chord

Repeat lines 4-6 for successive stations. PC Sta may be changed any time by executing line 3. For new case start at line 2.

TRIANGLE SOLUTION - GIVEN SSS OR SAS

TRIANGLE SOLUTION - GIVEN SSS OR SAS			SURV 1-15A	
SIDE	ANGLE	SSS SOLN	SAS SOLN	AREA SOLN

This program computes the area and the unknown sides and interior angles of two cases of triangles—one which requires three sides to be known and the other which requires two sides and the included angle to be known.

If one case is to be solved immediately after the other, the known parameters must be reentered.

Formulas used:

$$\text{Area} = \frac{1}{2} B C \sin c$$

$$A^2 = B^2 + C^2 - 2 B C \cos a$$

Where: A = Length of side A

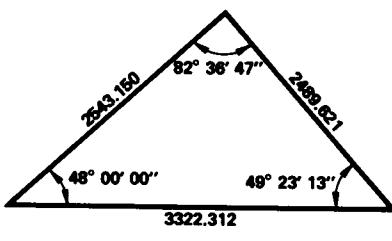
B = Length of side B

C = Length of side C

a = Angle opposite side A

c = Angle opposite side C

Example:



LINE	INSTRUCTIONS	DATA	KEYS	DISPLAY
1	Enter program			
2		Side	A	
3	If side angle side	Angle	B	
4		Side	A	
5	If side side side	Side	A	
6	If side side side soln desired		C	Side
7	If side angle side soln desired		D	Side
8		R/S		Opp Ang
9		R/S		Side
10		R/S		Opp Ang
11		R/S		Side
12		R/S		Opp Ang
13	Compute area		E	Area

For new case start at line 2.

TRIANGLE SOLUTION—GIVEN SSA

TRIANGLE SOLUTION-GIVEN SSA
 SIDE ANGLE SOLN A SOLN B AREA SOLN

SURV 1-16A
 SIDE ANGLE SOLN A SOLN B AREA SOLN

This program computes the area and the unknown sides and interior angles of a triangle in which two sides and a non-included angle are the known parameters. Both possible solutions are calculated without reentering the known parameters.

Formulas used:

$$\text{Area} = \frac{1}{2} BC \sin c$$

$$A^2 = B^2 + C^2 - 2 BC \cos a$$

Where: A = Length of side A

B = Length of side B

C = Length of side C

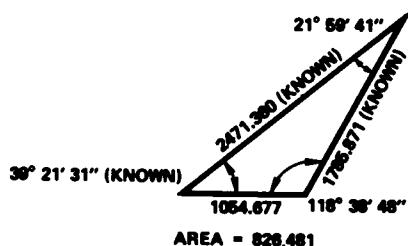
a = Angle opposite side A

b = Angle opposite side B

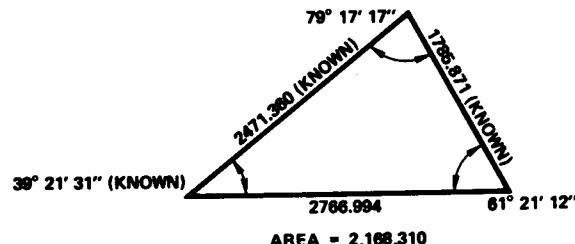
c = Angle opposite side C

Example:

Solution A



Solution B



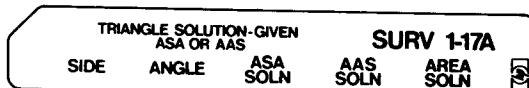
LINE	INSTRUCTIONS	DATA	KEYS	DISPLAY
1	Enter program			
2	*	Side	A	
3		Side	A	
4	Input ang opposite 2nd side	Angle	B	
5	If soln A desired		C	Side
6	If soln B desired		D	Side
7		R/S		Opp Ang
8		R/S		Side
9		R/S		Opp Ang
10		R/S		Side
11		R/S		Opp Ang
12	Optional: Compute area		E	Area

If alternate solution desired, go to line 5 or 6.

*For oblique triangles input longest side first.

For new case start at line 2.

TRIANGLE SOLUTION - GIVEN ASA OR AAS



This program computes the area and the unknown sides and interior angles of two cases of triangles—one which requires two angles and the included side and the other which requires two angles and a non-included side.

If one case is to be solved immediately after the other, the known parameters must be reentered.

Formulas used:

$$\text{Area} = \frac{1}{2} BC \sin a$$

$$A/\sin a = B/\sin b = C/\sin c$$

Where: A = Length of side A

B = Length of side B

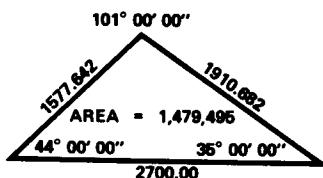
C = Length of side C

a = Angle opposite side A

b = Angle opposite side B

c = Angle opposite side C

Example:



LINE	INSTRUCTIONS	DATA	KEYS	DISPLAY
1	Enter program			
2			Angle	B
3	If angle side angle	Side	A	
4		Angle	B	
5	If angle angle side input side			
	opposite second angle	Side	A	
6	If angle side angle soln desired		C	Side
7	If angle angle side soln desired		D	Side
8		R/S		Opp Ang
9		R/S		Side
10		R/S		Opp Ang
11		R/S		Side
12		R/S		Opp Ang
13	Compute area		E	Area

For new case start at line 2.

BEARING-BEARING INTERSECT

BEARING-BEARING INTERSECT		SURV 1-18A		
POINT 1 N-E	POINT 2 N-E	LINE 1 BRG-QUAD	LINE 2 BRG-QUAD	N-E SOLN

This program computes the point of intersection coordinates of two lines for which the bearing of each line is known and the coordinates of a point on each line are known.

Formulas used:

$$N = ((E_1 - N_1 \tan Az_1) - (E_2 - N_2 \tan Az_2)) / (\tan Az_2 - \tan Az_1)$$

$$E = E_1 - N_1 \tan Az_1 + N \tan Az_1$$

Where: Az_1 = Azimuth of line 1

Az_2 = Azimuth of line 2

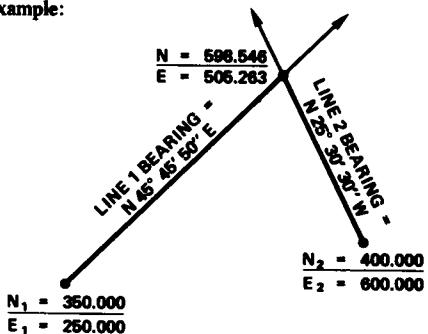
N_1, E_1 = Northing, easting of point 1

N_2, E_2 = Northing, easting of point 2

N, E = Northing, easting of intersect point

NOTE: Program will not give a solution if one of the bearings is due east or west

Example:



LINE	INSTRUCTIONS	DATA	KEYS	DISPLAY
1	Enter program			
2		N_1	A	
3		E_1	A	
4		N_2	B	
5		E_2	B	
6		Brg 1	C	
7		Quad 1	C	
8		Brg 2	D	
9		Quad 2	D	
10	Compute intersect coord		E	N
			R/S	E

For new case start at line 2.

BEARING-DISTANCE INTERSECT

BEARING-DISTANCE INTERSECT		SURV 1-19A		
POINT 1 N-E	POINT 2 N-E	LINE 1 BRG-QUAD	LINE 2 DIST	N-E SOLN

This program calculates the coordinates of the point of intersection of two lines—one of known bearing through known coordinates and the other of known length from a point of known coordinates. Both solutions are computed.

The far solution is obtained by entering the bearing from point 1, and the near solution by entering the bearing into point 1.

Formulas used:

$$Az_{12} = \tan^{-1} \frac{E_2 - E_1}{N_2 - N_1}$$

$$h = Dist_{12} \sin \phi$$

$$b = \sqrt{Dist_{12}^2 - h^2}$$

$$N = N_1 + ((Dist_{12} \cos \phi) + b) \cos (Az_1)$$

$$E = E_1 + ((Dist_{12} \cos \phi) + b) \sin (Az_1)$$

Where: Az_{12} = Azimuth of line from point 1 to point 2

Az_1 = Azimuth of line 1

ϕ = Angle between line 1 and line from point 1 to point 2

h = Perpendicular distance from point 2 to line 1

b = Distance from point of intersection to the point where the perpendicular (h) intersects line 1

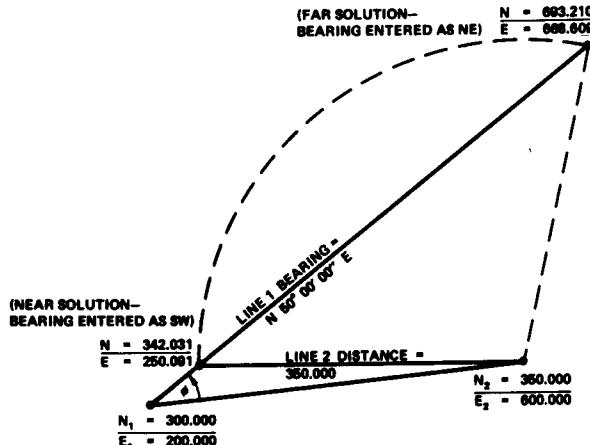
$Dist_2$ = Length of line 2 (the known distance)

N_1, E_1 = Northing, easting of point 1

N_2, E_2 = Northing, easting of point 2

$Dist_{12}$ = Distance from point 1 to point 2

Example:



LINE	INSTRUCTIONS	DATA	KEYS	DISPLAY
1	Enter program			
2		N_1	A	
3		E_1	A	
4		N_2	B	
5		E_2	B	
6		$Brg\ 1$	C	
7		$Quad\ 1^*$	C	
8		$Dist\ 2$	D	
9	Compute intersect coord		E	N
10			R/S	E

*There can be two solutions. To obtain the 'near' solution, enter the bearing as into point 1; for the 'far' solution, enter the bearing as away from point 1. For new case start at line 2.

DISTANCE-DISTANCE INTERSECT

DISTANCE-DISTANCE INTERSECT		SURV 1-20A		
POINT 1 N-E	POINT 2 N-E	LINE 1 DIST	LINE 2 DIST	N-E SOLN

Given two lines, each of known length and originating from two known points, this program computes the intersection coordinates. There are two possible solutions; this program calculates the one found by proceeding in a clockwise direction from the first known point to the second known point. The other solution is found by reversing the entry of the known point coordinates.

Formulas used:

$$\phi = \cos^{-1} \frac{\text{Dist}_{12}^2 + \text{Dist}_1^2 - \text{Dist}_2^2}{2(\text{Dist}_1)(\text{Dist}_{12})}$$

$$Az = \tan^{-1} \frac{E_2 - E_1}{N_2 - N_1}$$

$$I = N_1 + \text{Dist}_1 \cos(Az - \phi)$$

$$C = E_1 + \text{Dist}_1 \sin(Az - \phi)$$

Where: ϕ = Angle between line 1 and line 1 → 2

Dist_{12} = Distance from point 1 to point 2

Dist_1 = Known distance along line 1

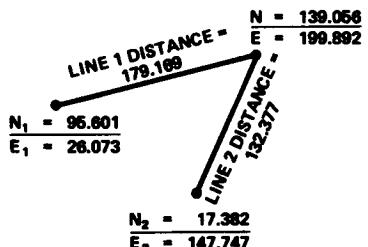
Dist_2 = Known distance along line 2

N_1, E_1 = Northing, easting of point 1

N, E = Northing, easting of intersection point

Az = Azimuth of line from point 1 to point 2

Example:



NOTE: Computed solution is always clockwise from point 1 to 2. For alternate solution, start at Point 2.

LINE	INSTRUCTIONS	DATA	KEYS	DISPLAY
1	Enter program			
2		N_1	A	
3		E_1	A	
4		N_2	B	
5		E_2	B	
6		Dist 1	C	
7		Dist 2	D	
8	Compute intersect coord		E	N
9			R/S	E

For new case start at line 2.

DISTANCE FROM A POINT TO A LINE

DISTANCE FROM A POINT TO A LINE

BASE N-E	LINE BRG-QUAD	OFFSET N-E	N-E SOLN	DIST SOLN	<input type="checkbox"/>
-------------	------------------	---------------	-------------	--------------	--------------------------

SURV 1-21A

Given a point of known coordinates with a line of known bearing passing through it and a second point of known coordinates, this program calculates the offset distance from the second point to the line, the distance from the intersection to the first known point, and the coordinates of the intersection.

Formulas used:

$$\text{Dist}_{BO} = \sqrt{(N_O - N_B)^2 + (E_O - E_B)^2}$$

$$\text{Dist}_{BI} = \sqrt{(N_O - N_I)^2 + (E_O - E_I)^2}$$

$$N_I = \frac{E_O - E_B + N_O \operatorname{ctn}(Az_{BI}) + N_B \tan(Az_{BI})}{\operatorname{ctn}(Az_{BI}) + \tan(Az_{BI})}$$

$$E_I = E_B + (N_I - N_B) \tan(Az_{BI})$$

Where: Dist_{BO} = Distance from base point to offset point

 Dist_{BI} = Distance from base point to intersection point

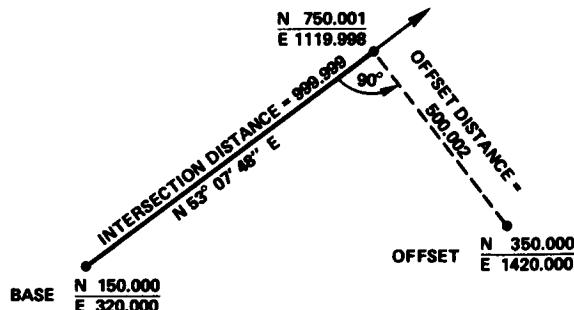
 Dist_{IO} = Distance from intersection point to offset point

 N_O, E_O = Northing, easting of offset point

 N_B, E_B = Northing, easting of base point

 N_I, E_I = Northing, easting of intersection point

 Az_{BI} = Known az from base point to intersection point

Example:


LINE	INSTRUCTIONS	DATA	KEYS	DISPLAY
1	Enter program			
2		Base N	A	
3		Base E	A	
4		Brg	B	
5		Quad	B	
6		Offst N	C	
7		Offst E	C	
8	Compute intersect coord		D	N
9			R/S	E
10	Compute distances		E	Off Dist
11			R/S	Int Dist

For new case start at line 2.

TAPING CORRECTIONS

TAPING CORRECTIONS				SURV 1-22A		
LBS PULL	TEMP	SLOPE DIST	ZNTH ANG SOLN	ΔELEV SOLN	DEL	

This program will apply corrections for tension, temperature, slope, correction index and sag to yield a corrected horizontal distance as measured with a steel tape. Inputs are slope distance and either zenith angle or difference in elevation for each unsupported successive length. Tape constants are stored in the program; however, the program can be customized for any tape by changing the constants stored in the program.

The specified tape constants stored are:

Tape Standardization Tension 20 lbs.

Tape Standardization Temperature 68°F

Tape Correction Index 0.000 ft/100 ft

Tape Unit Weight 0.014 lbs/ft

Tape Coefficient of Thermal Expansion $6.45 \times 10^{-6} \frac{^{\circ}\text{F}}{\text{ft}}$

Tape Area x Modulus of Elasticity 3.0×10^5 lbs.

To customize the program for any tape, use the following sequence to change the stored tape constants:

1. Enter program
2. Switch to program mode (W/PRGM) - 00 00 should be displayed
3. Press SST five times - 00 should be displayed
4. Press 9 DEL two times - 33 03 should be displayed
5. Press keys to enter tape standardization tension e.g., 1 8 (lbs.)
6. Press SST four times - 05 should be displayed
7. Press 9 DEL three times - 51 should be displayed
8. Press keys to enter tape area x modulus of elasticity e.g., 3 2 EX 4 (32 x 10⁶ lbs.)
9. Press SST five times - 00 should be displayed



10. Press 9 DEL four times - 81 should be displayed
11. Press keys to enter correction index per 100 ft e.g., 0 1 2 CHS (-0.012 ft/100 ft)
12. Press SST eleven times - 08 should be displayed
13. Press 9 DEL two times - 12 should be displayed
14. Press keys to enter tape standardization temperature e.g., 6 9 (69°F)
15. Press SST seven times - 08 should be displayed
16. Press 9 DEL six times - 51 should be displayed
17. Press keys to enter coefficient of thermal expansion e.g., 6 6 9 EX CHS 8 (669 x 10⁻⁶ / °ft)
18. Press SST twelve times - 04 should be displayed
19. Press 9 DEL four times - 33 06 should be displayed
20. Press keys to enter unit weight of tape e.g., 0 1 8 (.018 lbs/ft)
21. Record changed program by inserting blank card in reader slot
22. Switch to run mode
23. Enter changed program and test

NOTE: The total number of keys pressed to enter tape constants must not exceed 30. The above examples show 23.

To change program to accept vertical angles instead of zenith angles, use the following sequence:

1. Enter program
2. Press GTO D
3. Switch to program mode (W/PRGM) - 14 should be displayed
4. Press SST four times - 04 should be displayed
5. Press 9 DEL one time - 31 should be displayed
6. Press 5
7. Record changed program by entering blank card in reader slot
8. Switch to run mode
9. Enter changed program and test

Formulas used:

$$\begin{aligned} C_C &= C_1 L/100 \\ C_P &= L(P - P_o)/AE \\ C_T &= C_x L(T - T_o) \\ C_S &= W^2 L^3/24 P^2 \end{aligned}$$

$$\begin{aligned} \text{Corrected S Dist} &= S \text{ Dist} + C_C + C_P + C_T + C_S \\ H \text{ Dist} &= (\text{Corrected S Dist}) \sin (\text{Znth ang}) \\ H \text{ Dist} &= \sqrt{(\text{Corrected S Dist})^2 - (\Delta \text{ Elev})^2} \end{aligned}$$

Where: P = Tension on tape in pounds (pull)

P_o = Standard tension in pounds

A = Cross section area of tape in square inches

E = Modulus of elasticity for the tape material

C_x = Coefficient of thermal expansion for the tape

T = Temperature at time of reading in °F

T_o = Standard temperature in °F

W = Weight of tape per foot in pounds

L = Distance between supports in feet

C_C = Index correction

C_P = Correction for tension

C_T = Correction for temperature

C_S = Correction for sag

Znth ang = Zenith angle

C_1 = Tape correction index in ft/100 ft.

Example:



ZNTH ANG KNOWN

Pull = 25 lbs

Temp = 88°F

S Dist = 100'

Znth Ang = 88° 00' 00"

H Dist = 99.941

S Dist = 75.35

Znth Ang = 90° 00' 00"

H Dist = 75.355

Σ H Dist = 175.296

Δ ELEV KNOWN

Pull = 25 lbs

Temp = 88°F

S Dist = 100'

Δ Elev = 3.49

H Dist = 99.941

S Dist = 75.35

Δ Elev = 0

H Dist = 75.355

Σ H Dist = 175.296

LINE	INSTRUCTIONS	DATA	KEYS	DISPLAY
1	Enter program			
2	Optional after first entry	Pull	A	
3	Optional after first entry	Temp	B	
4		S Dist	C	
5	If zenith angle known	Zn Ang	D	H Dist
6	Optional (after line 5)		R/S	Σ H Dist
7	If elevation diff known	Δ Elev	E	H Dist
8	Optional (after line 7)		R/S	Σ H Dist

Return to line 2, 3, or 4 for next length.

For new case, press REG and start at line 2.

EDM SLOPE REDUCTION GIVEN ZENITH ANGLE

EDM SLOPE REDUCTION-GIVEN
ZENITH ANGLE
S DIST ZNTH ANG HI DM-
HT RFT HI INST-
HT TGT H DIST-
DEL SOLN

SURV 1-23A

This program reduces slope distance to horizontal distance at the instrument elevation and at sea level and gives the difference in elevation between two stations. The program will correct for the differences between the heights of the instruments and the heights of the targets. Corrections due to the curvature of the earth and the refraction of light are obtained by multiplying a derived constant times the horizontal distance. The value used for the coefficient of refraction is 0.071.

Formulas used:

$$Z_1 = Z - c + r + \sin^{-1} \left[\frac{\Delta \sin(Z - 2c + r)}{S \text{ Dist}} \right]$$

$$H \text{ Dist} = \frac{S \text{ Dist}}{\cos c} \sin(Z_1 - c) \left[\frac{R}{R + E} \right]$$

$$\Delta \text{ Elev} = \frac{S \text{ Dist}}{\cos c} \cos Z_1 + (HI \text{ DM} - HT \text{ Rft})$$

$$c = 14 \times 10^{-7} S \text{ Dist} \sin Z \text{ from } \frac{S \text{ Dist} \sin Z}{2R} \frac{180}{\pi}$$

$$r = 2 \times 10^{-7} S \text{ Dist} \sin Z \text{ from } \frac{0.071 S \text{ Dist} \sin Z}{R} \frac{180}{\pi}$$

Where: S Dist = Slope Distance

Z = Zenith angle

Z₁ = Zenith angle corrected for c & r and Δ

H Dist = Horizontal distance

Δ Elev = Difference in elevation

c = Zenith correction due to earth's curvature in degrees

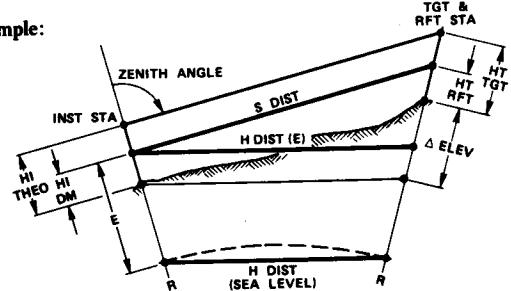
r = Correction due to refraction in degrees

R = 20,906,000 ft. (radius of earth)

E = Elevation of instrument

Δ = Height of DM-Height of Reflector-Height of Theodolite + Height of Target

Example:



Slope Distance	= 10,000 ft.
Elev at Instrument	= 5,000 ft.
Zenith Angle	= 75° 00' 00"
Height of DM	= 5.12
Height of Reflector	= 5.75
Height of Theodolite	= 5.96
Height of Target	= 5.34
Horizontal Distance (E)	= 9657.810
Horizontal Distance (SL)	= 9655.501
Elevation Difference	= 2590.681

LINE	INSTRUCTIONS	DATA	KEYS	DISPLAY
1	Enter program			
2		S Dist	A	
3		E	A	
4		Zn Ang	B	
5		HI DM	C	
6		HT Rft	C	
7		HT Theo	D	
8		HT Tgt	D	
9	Compute horizontal distance		E	H Dist (E)
10	Compute H Dist (sea level)		R/S	H Dist (SL)
11	Compute elevation difference		R/S	Δ Elev

For new case go to line 2.

EDM SLOPE REDUCTION GIVEN Δ ELEVATION

EDM SLOPE REDUCTION-
GIVEN Δ ELEVATION

SURV 1-24A

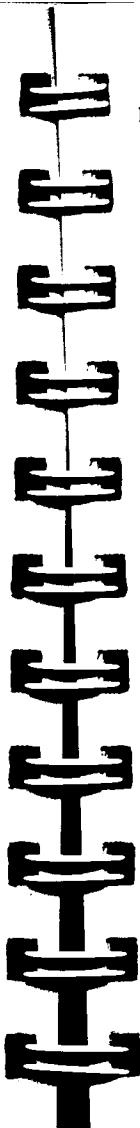
S DIST HI DM HT RFT Δ ELEV H DIST SOLN

Taking into consideration the curvature of the earth, this program reduces slope distance to horizontal distance at the instrument station elevation. The program assumes the slope distance between two points having known elevations was measured using an Electronic Distance Measuring Instrument. As options, the program will reduce the slope distance to a horizontal distance at sea level, and to a horizontal distance at any specified elevation. The value used for the radius of the earth is 20,906,000 feet.

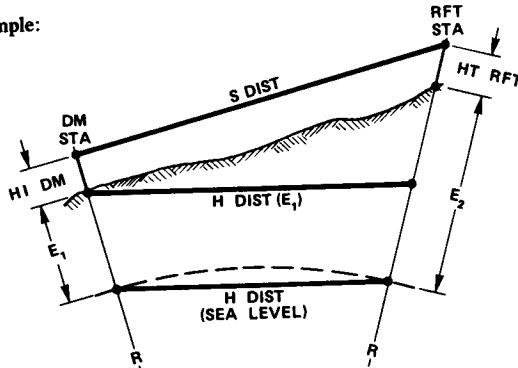
Formulas used:

$$H \text{ Dist} = \left[\frac{(S \text{ Dist})^2 - (E_2 + HT \text{ Rft} - E_1 - HI \text{ DM})^2}{(R + E_1 + HI \text{ DM})(R + E_2 + HT \text{ Rft})} \right] [R + E]$$

Where:
 S Dist = Slope Distance
 E₁ = Elevation of Instrument Station
 HI DM = Height of Instrument
 E₂ = Elevation of Reflector Station
 Ht Rft = Height of Reflector
 R = Radius of the Earth (20,906,000 ft.)
 E = Elevation of Horizontal Distance
 H Dist = Horizontal Distance



Example:



Slope Distance = 10,000 ft.
 Height of DM = 5.12
 Height of Reflector = 5.75
 Elev at DM Station = 1000.00
 Elev at Reflector Station = 3590.63
 Specified Elevation = 2000
 Horizontal Distance (E₁) = 9657.834
 Horizontal Distance (Sea Level) = 9657.372
 Horizontal Distance (E_s) = 9658.296

LINE	INSTRUCTIONS	DATA	KEYS	DISPLAY
1	Enter Program			
2		S Dist	A	
3		HI DM	B	
4		HT Rft	C	
5	Input elevation at DM station	E ₁	D	
6	Input elevation at Rft station	E ₂	D	
7	Optional	E _s	D	
8	Compute horizontal distance		E	H Dist(E ₁)
9	Optional		R/S	H Dist(SL)
10	Optional		R/S	H Dist(E _s)

For new case go to line 2.

FIELD ANGLE CHECK

FIELD ANGLE CHECK		SURV 1-25A	
REF AZ	ANGLE LT-RT	DEFL LT-RT	BEARING SOLN ANG COR SOLN

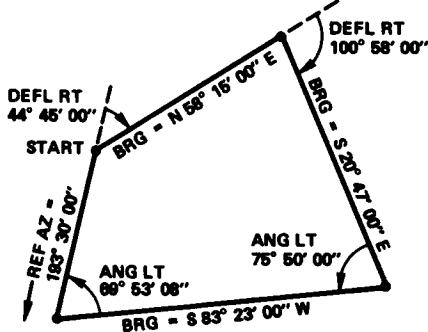
This program accepts a reference azimuth and field angles at each point in a traverse. The field angles are converted to bearings for each leg. At closing, the final leg is compared to the reference azimuth and the angular error of closure computed. The program can also handle traverses between two points.

Formulas used:

$$\text{Angular error} = (\text{Reference azimuth} - 180) - \text{Last course azimuth}$$

$$\text{Angular correction} = -\text{Angular error}/\text{Number of angles}$$

Example:



$$\text{Reference Azimuth} = 193^\circ 30' 00''$$

$$\text{Last Course Azimuth} = 13^\circ 29' 52''$$

$$\text{Angular Error} = 00^\circ 00' 08''$$

Angular Correction (to be applied to interior angles) =

$$-00^\circ 00' 02''$$

LINE	INSTRUCTIONS	DATA	KEYS	DISPLAY
1	Enter program			
2	Input Ref Az away from pt	Ref Az	A	
3	If angle right	Ang Rt	B	
4	If angle left	Ang Lt	CHS B	
5	If deflection right	Defl Rt	C	
6	If deflection left	Defl Lt	CHS C	
7	Optional: Compute course brg		D	Brg
8	Optional: Compute quad code		R/S	Quad
9	Optional: Compute azimuth (Repeat lines 3-9 for each course)		R/S	Az
10	Compute angular error		E	Ang Error
11			R/S	Ang Corr

If checking traverse between two points, the closing reference azimuth is entered via key A; angular error is then obtained at line 10.

To run another problem, press [M] [SF1] then return to line 2.

STADIA REDUCTIONS

STADIA REDUCTIONS			SURV 1-26A		
STATION ELEV-HI	ZENITH ANGLE	ROD INTERVAL	ROD READING	DIST-ELEV	SOLN

This program computes the elevation of and horizontal distance to points from an instrument station using stadia methods. Required inputs are the height of instrument, the zenith angle, the rod reading, and the rod stadia interval.

The program assumes stadia constant = 0, and stadia interval factor (K) = 100.

Slope angles are assumed to be entered as zenith angles. To change the program to use vertical angles, the following sequence must be followed:

1. Enter program
2. Press **GTO B**
3. Switch to program mode (W/PRGM) - 12 should appear in the display
4. Press **SST** (single step) 6 times - 51 should appear in the display
5. Press **S DEL** - 35 07 should appear in the display
6. Press **SST** four times - 03 should appear in the display
7. Press **S DEL** twice - 35 00 should appear in the display
8. Record changed program by inserting blank card in reader slot
9. Switch back to run mode
10. Enter changed program and test

Formulas used:

$$H \text{ Dist} = K s \cos^2 (V \text{ ANG})$$

$$V = \frac{1}{2} K s \sin 2 (V \text{ ANG})$$

$$\text{Pt Elev} = \text{HI} + V - \text{Rod reading} + \text{occupied station elevation}$$

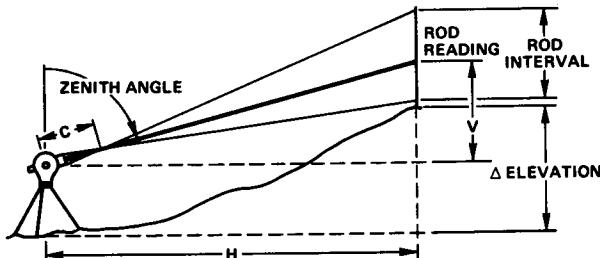
$$\text{Vert Ang} = 90^\circ - \text{Znth Ang}$$

Where: K = Stadia interval

s = Rod interval

Vert Ang = Vertical angle of line of sight (0° is horizontal)
 H Dist = Horizontal distance
 V = Vertical distance
 HI = Height of instrument

Example:



POINT NO.	HI	ZENITH ANGLE	ROD INTERVAL	ROD READING	HORIZONTAL DISTANCE	ELEVATION
Occ Sta. 5.2						491.0
1		93° 18'	3.28	7.4	326.91	469.96
2		93° 18'	3.32	8.1	330.90	469.02
3		90° 00'	4.06	8.8	406.00	487.40
4		91° 06'	4.51	5.2	460.83	482.34
5		86° 15'	1.29	5.2	128.45	499.42
6		73° 40'	1.20	8.2	110.51	520.39
7		75° 50'	1.31	5.2	123.15	522.09

LINE	INSTRUCTIONS	DATA	KEYS	DISPLAY
1	Enter program			
2		Sta El	A	
3		HI	A	
4		Zn Ang	B	
5		Intv	C	
6	If rod reading \neq HI	Reading	D	
7	Compute distance and elevation		E	H Dist
8	Optional		R/S	Pt Elev

For additional points from same instrument station, repeat lines 4-8.

For new case start at line 2.

Notes

THREE WIRE LEVELING

THREE WIRE LEVELING			SURV 1-27A	
STARTING ELEV-K	BACK SIGHT	FORE SIGHT	U.C.L READING	SOLN

After the initial entry of the starting elevation and stadia interval factor (if it is not 100), this program uses the upper stadia hair, crosshair, and lower stadia hair readings to provide the elevation difference, elevation of final point, backsight distances and foresight distances.

If no stadia interval constant, K, is entered, the value used by the calculator is 100.

Formulas used:

$$\text{Elev 2} = \text{Elev 1} + \left[\frac{U + C + L}{3} \right]_{BS} - \left[\frac{U + C + L}{3} \right]_{FS}$$

$$\text{Dist} = K [\Sigma BS \frac{1}{2} \text{ stadia intv} + \Sigma FS \frac{1}{2} \text{ stadia intv}]$$

$$\text{Check} = 2C - U - L$$

Where: U = Upper reading

C = Center reading

L = Lower reading

BS = Backsight

FS = Foresight

K = Stadia constant

Example:

NO OF STATION	U,C,L READING BACKSIGHT	% STADIA INTERVAL BACKSIGHT	U,C,L READING FORESIGHT	% STADIA INTERVAL FORESIGHT	ELEV OF STATION
ELEV 5280.000	8.266 8.105 7.940	.161 .165	3.491 3.320 3.152	.171 .166	5284.783
1	8.119 7.329 6.536	.790 .794	5.221 4.436 3.654	.786 .781	5287.674
2	6.693 6.021 5.444	.572 .577	3.172 2.831 2.085	.541 .546	5291.064
	$\Sigma =$	3.059	$\Sigma =$	2.983	

Elevation Difference from Sum of Means is 11.064

Final Elevation 5291.064

Backsight Distance 305.9

Foresight Distance 299.3

LINE	INSTRUCTIONS	DATA	KEYS	DISPLAY
1	Enter program			
2	Input starting elevation	Elev	A	
3	Optional: Input stadia interval factor	K	A	
4	If backsight		B	
5	If foresight		C	
6	Input upper reading	Upper	D	
7	Input center reading	Center	D	
8	Input lower reading	Lower	D	Check *
	(Repeat lines 4-8 for each set of backsight and foresight readings)			
9	Optional: Read elev difference		E	Δ Elev
10	Optional: Read final elev		R/S	Sta Elev
11	Optional: Read sum of BS distances		R/S	BS Dist
12	Optional: Read sum of FS distances		R/S	FS Dist
	(Repeat lines 4-12 for successive stations)			

* Difference between upper and lower stadia interval is displayed. Allows a check on accuracy of reading

For a new case press and start at line 2.

SLOPE STAKING – GIVEN CENTERLINE TERRAIN ELEVATION

SLOPE STAKING-GIVEN
CENTERLINE TERRAIN ELEVATION
HG DIST-SLOPE QT ELEV S DIST H DIST Δh SOLN

SURV 1-28A

Using a previously located center line and the design cross section to provide center line terrain and hinge point elevations, this program helps in the setting of slope stakes. The program produces a distance for the rod man to move from his present trial point to a new trial point which should be very close to the catch point.

The trial point may be entered by either of two methods—slope distance and vertical angle or horizontal distance and elevation difference. All input data is measured with reference to the center line and its terrain elevation.

Slope is entered as a ratio to 1. For example, a 1½:1 slope is entered as 1.5. Cut slopes are entered as positive and fill slopes as negative.

Formulas used:

$$E = HG \text{ Dist} + \text{Slope} (\text{T Elev} - HG \text{ Elev} + \Delta h) - H \text{ Dist};$$

$$H \text{ Dist}_{i+1} = H \text{ Dist}_i + E \text{ (until } E \leq 0.1)$$

$$\Delta h = S \text{ Dist} \sin(V \text{ ANG})$$

$$H \text{ Dist} = S \text{ Dist} \cos(V \text{ ANG})$$

Where: HG Dist = Distance from centerline to hinge point

T Elev = Terrain elevation at centerline

HG Elev = Elevation at hinge point

Δh = Elevation difference from T Elev to trial point

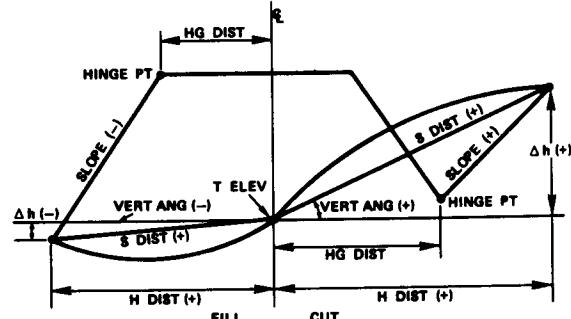
$H \text{ Dist}_i$ = Horizontal distance from centerline to trial point; it is varied until tolerance is reached.

E = Error term

$S \text{ Dist}_i$ = Slope distance from centerline to trial point.

V ANG = Vertical Angle

Example:



INPUT		FILL	CUT
Horizontal distance to hinge pt.	HG Dist	+12	+18
Slope (ratio of horizontal distance to 1)	Slope	-1.5	+1
Centerline terrain elevation	QT Elev	5280.00	5280.00
Hinge pt. elevation	HG Elev	5286.00	5282.00

TRIAL PT LOCATION (DATA FOR CATCH PT GIVEN)

Slope distance from centerline to trial pt.	S Dist	+24.0	+33.1
Vertical angle between horizontal and slope distance line	Vert Ang	-4° 46'	+25° 01'
Horizontal distance from centerline to trial pt.	H Dist	+24.0	+30.0
Elevation difference between centerline terrain elevation and trial pt. elevation	Δh	-2.0	+14.0

LINE	INSTRUCTIONS	DATA	KEYS	DISPLAY
1	Enter program			
2		HG Dist	A	
3	Ratio to 1; fill (-), cut (+)	Slope	A	
4		G T Elev	B	
5		HG Elev	B	
6	If S Dist & V Ang known	S Dist	C	
7	If S Dist & V Ang known	V Ang	C	
8	If H Dist & Δh known	H Dist	D	
9	If H Dist & Δh known	Δh	D	
10	Compute move required to reach catch pt (+ move away from G; - move toward G)			
11	Optional: Compute H Dist to G.	R/S	E	Catch Dist Dist to G

For new case start at line 2.



Notes

SLOPE STAKING— GIVEN CENTERLINE CUT/FILL

SLOPE STAKING-GIVEN
CENTERLINE CUT/FILL
HG DIST-SLOPE
E C OR F
V DROP
S DIST
VERT ANG
H DIST
 Δh
SOLN

SURV 1-29A

Using a previously located center line and the design cross section to provide cut or fill at center line and vertical drop from center line elevation to hinge point elevation, this program helps in the setting of slope stakes. The program produces a distance for the rod man to move from his present trial point to a new trial point which should be very close to the catch point.

The trial point may be entered by either of two methods—slope distance and vertical angle or horizontal distance and elevation difference. All data is measured in reference to the center line and its terrain elevation.

Slope is entered as a ratio to 1. For example, a 1½:1 slope is entered as 1.5. Cut slopes are entered as positive and fill slopes as negative.

Formulas used:

$$E = HG \text{ Dist} + \text{Slope } ((\text{cut or fill}) + V \text{ drop} + \Delta h) - H \text{ Dist}_i$$

$$H \text{ Dist}_{i+1} = H \text{ Dist}_i + E \text{ (until } E \leq 0.1)$$

$$\Delta h = S \text{ Dist} \sin(V \text{ ANG})$$

$$H \text{ Dist} = S \text{ Dist} \cos(V \text{ ANG})$$

Where: HG Dist = Distance from centerline to hinge point
Cut or fill = Depth to final grade at centerline; fill designated by negative sign

V Drop = Vertical drop from centerline elevation to hinge point

Δh = Elevation difference from centerline elevation to trial point

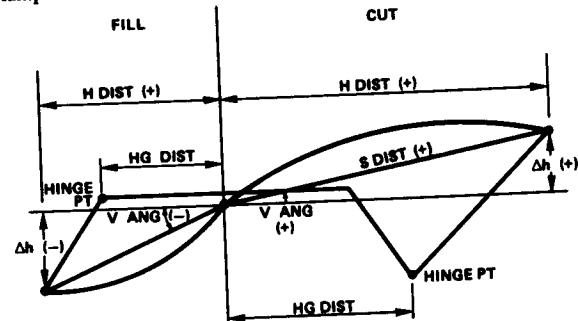
Vert ang = Vertical angle from centerline elevation to trial point

$H \text{ Dist}_i$ = Horizontal distance from centerline to trial point

$S \text{ Dist}_i$ = Slope distance from centerline to trial point.

V ANG = Vertical Angle

Example:



INPUT	FILL	CUT
Horizontal distance to hinge pt.	HG Dist 12	18
Slope (ratio to 1)	Slope -1.5	1
Centerline cut (+) or fill (-)	E C or F -3.75	-3.75
Vertical drop from C	V Drop +0.25	+4.25
CATCH PT. LOCATION		
Slope distance from centerline to trial pt.	S Dist 24.42	34.73
Vertical Angle between horizontal and slope distance line	Vert Ang -10° 37'	22° 52'
Horizontal distance from centerline to trial pt.	H Dist 24.0	+32.0
Elevation difference between centerline and trial pt.	Δh -4.5	13.5

LINE	INSTRUCTIONS	DATA	KEYS	DISPLAY
1	Enter program			
2		HG Dist	A	
3	Ratio to 1, fill (-), cut (+)	Slope	A	
4		C or F	B	
5		V Drop	B	
6	If S Dist & Vert Ang known	S Dist	C	
7	If S Dist & Vert Ang known	V Ang	C	
8	If H Dist & Δh known	H Dist	D	
9	If H Dist & Δh known	Δh	D	
10	Compute move required to reach catch pt (+ move away from C; - move toward C)		E	D to Catch
11	Optional: Compute H Dist to C		R/S	Dist to C

For new case start at line 2.



Notes

AZIMUTH OF THE SUN

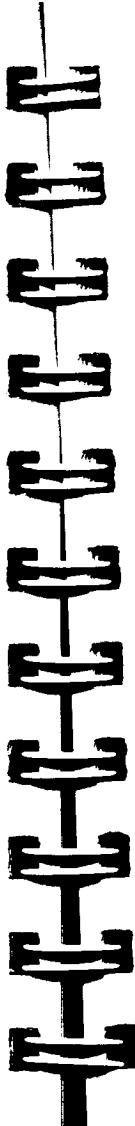
AZIMUTH OF THE SUN SURV 1-30A
 TIME- DECLIN- LATITUDE VERT ANG AZIMUTH
 T ZONE HR DIFF LATITUDE TO SUN SOLN

This program will yield azimuth of the sun from solar observations. Data which are entered here are assumed to be mean values with appropriate corrections made where necessary prior to operation of the program. Since the result is the sun's azimuth from north, it is left to the observer to add or subtract the angle turned to a backsight to determine the azimuth between two points.

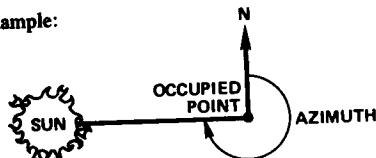
Formulas used:

$$Az = \cos^{-1} \left[\frac{\sin \delta - \sin \phi \sin (V \text{ ANG})}{\cos \phi \cos (V \text{ ANG})} \right]$$

Where: Az = Azimuth from north
 δ = Hr diff (Time + T Zone) + Declination
 ϕ = Latitude of observer's position
 Vert ang = Vertical angle to sun



Example:



Date: 18 July 1973

Time of observation: 15 hrs 38 min 37 sec (EST)

Longitude of standard meridian (time zone): 5 hrs

Declination at 0 hrs. (ephemeris): $21^\circ 05' 36''$

Hour difference in declination (ephemeris) $-00^\circ 00' 26.4''$

Latitude (ϕ): $43^\circ 00' 34''$ N

Mean corrected vertical angle to sun: $33^\circ 34' 49''$

Calculated north azimuth of sun: $268^\circ 07' 54''$

Input all angles as degrees, minutes and seconds in the form DDD.MMSS. Times are based on a 24 hour clock and are input as HH.MMSS (4 pm becomes 16 hours).

If the declination is North—it will have a positive value, and if the declination is South—it will be negative.

If the declination is on the increase, the hour difference will have a positive value, and if the declination is on the decrease, the hour difference will be negative.

LINE	INSTRUCTIONS	DATA	KEYS	DISPLAY
1	Enter program			
2	Input local std. time	Time	A	
3		T Zone	A	
4		Declin	B	
5		Hr diff	B	
6		Lat	C	
7		V Ang	D	
8	Compute north Azimuth of sun		E	Sun Az

For new case start at line 2.

PREDETERMINED AREA - LINE THRU A POINT

PREDETERMINED AREA LINE THRU A POINT		SURV 1-31B
REQUIRED POINT 1 AREA	POINT 2 N-E	BRG-QUAD N-E SOLN

This program solves one of the two cases of specifying the area of a land parcel, namely, that of hinging a side. First, the user breaks the area into a triangle and then uses this program to hinge the side to force the area to a predetermined value. Required inputs are the coordinates of the two known points, the bearing of the second side and the desired area. Outputs are coordinates of the unknown point.

In the example below, the coordinates of point 3 are unknown. A line passing through point 1 (the hinge point) will intersect at only one place on the line 2→3 which satisfies the area requirements.

Formulas used:

$$\text{Area} = \frac{1}{2} (b)(h)$$

$$h = a \sin \theta$$

$$\text{Area} = \frac{1}{2} (b)(a \sin \theta)$$

$$a = \frac{2 \text{ Area}}{b \sin \theta}$$

$$N = N_2 + a \cos (\text{Az})$$

$$E = E_2 + a \sin (\text{Az})$$

Where: b = Length of line 1→2

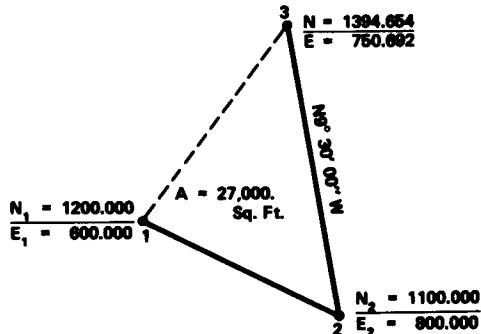
h = Height of the triangle

a = Length of line 2→3

θ = Angle 123

Az = Azimuth of line 2→3

Example:



LINE	INSTRUCTIONS	DATA	KEYS	DISPLAY
1	Enter program			
2		Area	A	
3		N ₁	B	
4		E ₁	B	
5		N ₂	C	
6		E ₂	C	
7		Brg	D	
8		Quad	D	
9	Compute solution		E	N
			R/S	E

For new case start at line 2.

PREDETERMINED AREA – TWO SIDES PARALLEL

PREDETERMINED AREA
TWO SIDES PARALLEL
REQUIRED AREA BASE 1 LENGTH ANGLE TO SIDE 1 ANGLE TO SIDE 2 SOLN

SURV 1-32A

This program solves one of the two cases of specifying the area of a land parcel, namely, that of sliding a side along a fixed bearing. First, the user breaks the area into a trapezoid and then uses this program to slide the side to force the area to a predetermined value. Computed values include the lengths of the non-parallel sides, the length of the second parallel base and the angles formed by the intersection of each non-parallel side with the second base (angles 3 and 4 in diagram).

In the diagram, base 2 (side 4-3) is the side being moved.

Formulas used:

$$\text{Area} = \frac{1}{2} (b_1 h + b_2 h)$$

$$b_2 = b_1 - h(\operatorname{ctn} \theta + \operatorname{ctn} \phi)$$

$$\text{Area} = \frac{1}{2} (b_1 h + (b_1 - h(\operatorname{ctn} \theta + \operatorname{ctn} \phi))h)$$

$$\text{Area} = b_1 h - \frac{1}{2} (\operatorname{ctn} \theta + \operatorname{ctn} \phi) h^2$$

$$h = \frac{b_1 - \sqrt{b_1^2 - 2A(\operatorname{ctn} \theta + \operatorname{ctn} \phi)}}{\operatorname{ctn} \theta + \operatorname{ctn} \phi}$$

$$r_1 = h / \sin \theta$$

$$r_2 = h / \sin \phi$$

$$\theta' = 180 - \theta$$

$$\phi' = 180 - \phi$$

Where: A = Area

b_1 = Length of base 1

b_2 = Length of base 2

h = Altitude of trapezoid

θ = Angle between base 1 and side 1 (Angle 1)

ϕ = Angle between base 1 and side 2 (Angle 2)

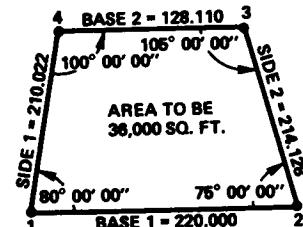
r_1 = Length of side 1

r_2 = Length of side 2

θ' = Angle between base 2 and side 1 (Angle 4)

ϕ' = Angle between base 2 and side 2 (Angle 3)

Example:



LINE	INSTRUCTIONS	DATA	KEYS	DISPLAY
1	Enter program			
2		Area	A	
3		Base 1	B	
4		Ang 1	C	
5		Ang 2	D	
6	Compute length of 2nd base		E	Base 2
7	Compute non-parallel side 1		R/S	Side 1
8	Compute non-parallel side 2		R/S	Side 2
9	Compute 2nd angle to side 1		R/S	Angle 4
10	Compute 2nd angle to side 2		R/S	Angle 3

NOTE: This program will not solve a parallelogram.

(i.e. sides 1 and 2 parallel)

For new case start at line 2.

VOLUME BY AVERAGE END AREA

VOLUME BY AVERAGE END AREA			SURV 1-33A	
ELEV FROM C	DIST FROM C	STA AREA SOLN	STATION INTERVAL	VOLUME SOLN

This program computes end area for any station, volume from previous station, and accumulated volume to the present station. Inputs are the elevations and distances from the centerline for all points of a cross section and the interval from the previous station.

When entering elevations and distances from center line for a particular station, start with center point (0,0). The storage registers must be cleared between successive problems.

Formulas used:

$$V_{avg} = (Area_i + Area_{i-1}) I/2$$

$$\begin{aligned} \text{Area} &= \frac{1}{2} [Elev_1 (H\ Dist_2 - H\ Dist_n) + \\ &\quad Elev_2 (H\ Dist_3 - H\ Dist_1) + \\ &\quad \dots + Elev_n (H\ Dist_1 - H\ Dist_{n-1})] \end{aligned}$$

Where: V_{avg} = Average volume between two stations

Area = Cross sectional area at a station

H Dist = Horizontal distance from centerline at cross section

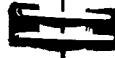
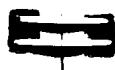
Elev = Elevation at a point on the cross section

I = Interval between stations

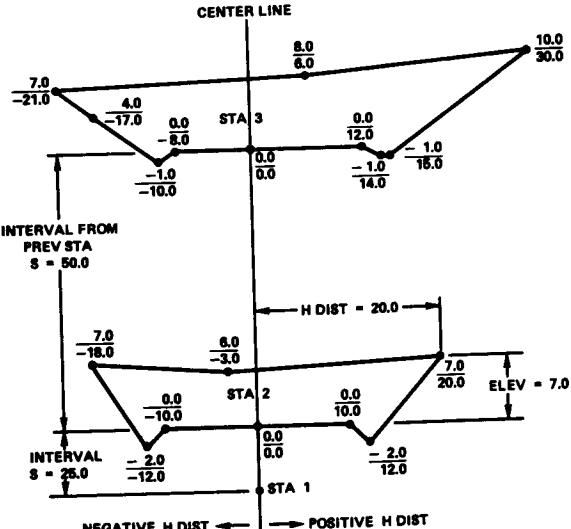
Subscript i refers to current point

Subscript n refers to last point

Numeric subscript refers to point number



Example:



STA	AREA	INTERVAL (Ft)	VOLUME (cubic feet)	Σ VOLUME (cubic yards)
1	0			100
2	216	25	2,700	597.7
3	321.5	50	13,437.5	

NOTE: Traverse sections in clockwise direction to insure positive areas and volumes.

LINE	INSTRUCTIONS	DATA	KEYS	DISPLAY
1	Enter program			
2	If station has zero area	0	A	
3	If station has zero area go to			
	line 6			
4	First and last point input			
	must be 0 elev at 0 dist	Elev	A	
5		Dist	B	
	(Return to line 4 for next pt.)			
	Continue to line 6 when cross			
	section complete)			
6	Compute station end area		C	End Area
	(If station is first station in			
	problem, go to line 4 and input			
	data for second station)			
7		Interval	D	
8	Optional: Volume from			
	previous station		E	Sta Vol
9	Optional: Accumulated volume		R/S	Cu Ft
10	Optional: Accumulated volume		R/S	Cu Yds

For new case, press **REG**, and start at line 2.

Notes

VOLUME OF BORROW PIT

VOLUME OF BORROW PIT SURV 1-34A
BASE-^AHT W-L ELEV GRID SEC ACC VOL VOL SOLN SOLN

This program calculates volume of fill which can be taken from a borrow pit given grid dimensions and elevations at the grid intersections. Volume is available for each grid section and also as an accumulative volume for all previous sections.

If several grid blocks have the same horizontal dimensions, the sum of the volumes of all these blocks can be calculated at once. This is done by entering all of the elevations using the "C" key before pressing the "D" key to compute the volume. For example, if three rectangular blocks have the same dimensions, the 12 elevations are entered before pressing the "D" key.

Formulas used:

$$\text{Vol}_\Delta = \frac{1}{2} (\text{Base}) (\text{Ht}) (\text{Elev})$$

$$\text{Vol}_\Delta = (\text{Width})(\text{Length})(\text{Elev})$$

Where: Vol_A = Volume of triangular grid section

Base = Base of triangle

Ht = Height of triangle

Alt = Height of triangle
Elev = Elevation of grid

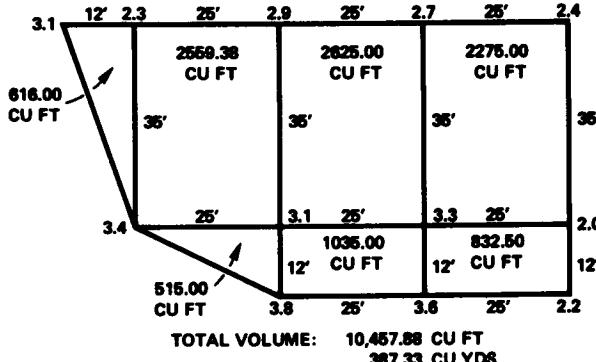
Elev = Elevation of grid section (depth or cut)
Val = Value of contour interval

Vol. = Volume of reagent

Width = Width of rectangle

Length = Length of rectangle

Example:



LINE	INSTRUCTIONS	DATA	KEYS	DISPLAY
1	Enter program		RTN R/S	
2	If triangular area	Base	A	
3	If triangular area	Height	A	
4	If rectangular area	Width	B	
5	If rectangular area	Length	B	
6		Elev	C	
	(Input as many elevations as			
	needed to describe each corner			
	pressing <input type="checkbox"/> after each			
	entry)			
7	Compute grid section volume		D	Cu Ft
8	Compute accumulated volume		E	Cu Ft
9	Optional		R/S	Cu Yds

For next grid section, return to line 2.

For new case, press **ENTER** and start at line 2.

**ABBREVIATIONS**

AAS	(Triangle) — Angle—Angle—Side
ACC	Accumulated
ADJ	Adjusted
AL, Ang Lt	Angle left
ANG	Angle
AR, Ang Rt	Angle right
ASA	(Triangle) — Angle—Side—Angle
AZ	Azimuth
BEG	Beginning
BRG	Bearing
BS	Backsight
C	Center stadia reading on level rod; also cut or chord length
COORD	Centerline
CORR	Coordinate
DECLIN	Correction
DEFL	Declination
DEP	Deflection
DIFF	Departure
DIST	Difference
DL	Distance
DM	Deflection left
DR	Distance Meter
E	Deflection right
EL	Easting
ELEV	Elevation
F	Elevation
FIL	Fill
FS	Fillet
H	Foresight
H DIST, HD	Height
HI	Horizontal distance
HG DIST	Height of instrument
	Horizontal distance from centerline to hinge point

HG ELEV	Hinge point elevation
HR	Hour
HT	Height of target; also height
INST	Instrument (Theodolite or Transit only)
INT	Intersection
INTV	Interval
K	Stadia interval factor
L	Length; also lower stadia reading on level rod or arc length
LAT	Latitude
LBS	Pounds
LT	Left
MAX	Maximum
MIN	Minimum
N	Northing
OCC	Occupied
OFFSET, OFF	Offset distance
PC	Point of curvature
PRCSN	Precision ratio
PT	Point
QUAD	Quadrant code
R	Radius
REF	Reference
RFT	Reflector
RT	Right
SAS	(Triangle) – Side–Angle–Side
SEC	Section, also sector
SEG	Segment
S DIST, SD	Slope distance
SOLN	Solution
SSA	(Triangle) – Side–Side–Angle
SSS	(Triangle) – Side–Side–Side
STA	Station
T	(Curve) Tangent distance; also terrain
T ZONE	Time zone
TGT	Target
TEMP	Temperature



TOT
 TRNSFRMD
 U
 UNADJ
 V
 VERT
 VOL
 W
 ZA
 ZNTH, ZN
 Δ

Total
 Transformed
 Upper stadia reading on level rod
 Unadjusted
 Vertical
 Vertical
 Volume
 Width
 Zenith angle
 Zenith
 Difference or change in quantity or measurement; also triangle or central angle
 Rectangle

PROGRAM LISTINGS

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FIELD ANGLE TRAVERSE

CODE	KEYS	CODE	KEYS	CODE	KEYS
23	LBL	00	0	33	STO
11	A	24	RTN	61	+
31	f	23	LBL	04	4
43	REG	14	D	34 07	RCL 7
33 08	STO 8	34	RCL	84	R/S
33 06	STO 6	09	9	34 04	RCL 4
33 03	STO 3	35 07	g x ² y	02	2
24	RTN	32	f ⁻¹	81	÷
23	LBL	03	→D.MS	35	9
11	A	31	f	06	ABS
33 07	STO 7	04	SIN	84	R/S
33 05	STO 5	71	x	04	4
24	RTN	24	RTN	03	3
23	LBL	23	LBL	05	5
11	A	15	E	06	6
23	LBL	33	STO	00	0
12	B	61	+	81	÷
01	1	02	2	24	RTN
08	8	34 01	RCL 1	35 01	g NOP
00	0	35 07	g x ² y	35 01	g NOP
31	f	32	f ⁻¹	35 01	g NOP
02	D.MS+	01	R→P	35 01	g NOP
23	LBL	33	STO	35 01	g NOP
13	C	61	+	35 01	g NOP
32	f ⁻¹	08	8	35 01	g NOP
03	→D.MS	35 07	g x ² y	35 01	g NOP
34 01	RCL 1	33	STO	35 01	g NOP
61	+	61	+	35 01	g NOP
33 01	STO 1	07	7	35 01	g NOP
24	RTN	34 03	RCL 3	35 01	g NOP
23	LBL	34 08	RCL 8	35 01	g NOP
14	D	84	R/S	35 01	g NOP
33	STO	33 03	STO 3	35 01	g NOP
09	9	61	+	35 01	g NOP
09	9	71	x	35 01	g NOP

R ₁ Azimuth	R ₄ Area Factor	R ₇ Current E
R ₂ ΣH Dist	R ₅ Beg E	R ₈ Current N
R ₃ Previous N	R ₆ Beg N	R ₉ Used

BEARING TRAVERSE

CODE	KEYS	CODE	KEYS	CODE	KEYS
23	LBL	83	INT	61	+
11	A	01	1	08	8
33 08	STO 8	08	8	35 07	g x ² y
33 06	STO 6	00	0	33	STO
33 03	STO 3	71	x	61	+
24	RTN	61	+	07	7
23	LBL	33 01	STO 1	34 03	RCL 3
11	A	24	RTN	34 08	RCL 8
33 07	STO 7	23	LBL	84	R/S
33 06	STO 5	14	D	33 03	STO 3
24	RTN	33	STO	61	+
23	LBL	09	9	71	x
12	B	09	9	33	STO
32	f ⁻¹	00	0	61	+
03	→D.MS	03	→D.MS	04	4
24	RTN	24	RTN	34 07	RCL 7
23	LBL	23	LBL	84	R/S
13	C	14	D	34 04	RCL 4
02	2	34	RCL	02	2
81	÷	09	9	81	÷
41	↑	12	B	35	g
31	f	31	f	06	ABS
83	INT	04	SIN	84	R/S
35 21	g x ² y	71	x	04	4
22	GTO	24	RTN	03	3
01	1	23	LBL	05	5
35 09	g R ↑	15	E	06	6
35 09	g R ↑	33	STO	00	0
42	CHS	61	+	81	÷
35 09	g R ↑	02	2	24	RTN
35 09	g R ↑	34 01	RCL 1	35 07	g x ² y
23	LBL	32	f ⁻¹	01	→P
01	1	01	R→P	33	STO
35 08	g R ↓	31	f		

R ₁ Azimuth	R ₄ Area Factor	R ₇ Current E
R ₂ ΣH Dist	R ₅ Beg E	R ₈ Current N
R ₃ Previous N	R ₆ Beg N	R ₉ Used

**CLOSURE FOR FIELD ANGLE
AND BEARING TRAVERSES**

CODE	KEYS	CODE	KEYS	CODE	KEYS
23	LBL	44	CLX	14	D
11	A	35 24	g > y	34 02	RCL 2
33 06	STO 6	03	3	24	RTN
24	RTN	06	6	23	LBL
23	LBL	00	0	15	E
11	A	61	+	34 02	RCL 2
33 05	STO 5	41	↑	34 03	RCL 3
24	RTN	41	↑	24	RTN
23	LBL	09	9	35 01	g NOP
12	B	00	0	35 01	g NOP
34 04	RCL 4	81	÷	35 01	g NOP
02	2	01	1	35 01	g NOP
81	÷	61	+	35 01	g NOP
35	g	31	f	35 01	g NOP
06	ABS	83	INT	35 01	g NOP
84	R/S	33	STO	35 01	g NOP
04	4	09	9	35 01	g NOP
03	3	02	2	35 01	g NOP
05	5	81	÷	35 01	g NOP
06	6	31	f	35 01	g NOP
00	0	83	INT	35 01	g NOP
81	÷	01	1	35 01	g NOP
24	RTN	08	8	35 01	g NOP
23	LBL	00	0	35 01	g NOP
13	C	71	x	35 01	g NOP
34 07	RCL 7	51	-	35 01	g NOP
34 05	RCL 5	35	g	35 01	g NOP
51	-	08	ABS	35 01	g NOP
34 08	RCL 8	31	f	35 01	g NOP
34 06	RCL 6	03	→D.MS	35 01	g NOP
51	-	84	R/S	35 01	g NOP
31	f	34	RCL	35 01	g NOP
01	R→P	09	9	35 01	g NOP
84	R/S	24	RTN	23	LBL
33 03	STO 3	23	LBL		

R ₁ Current Az	R ₄ Area	R ₇ Current E
R ₂ ΣH Dist	R ₅ Beg E	R ₈ Current N
R ₃ Closure Dist	R ₆ Beg N	R ₉ Used

INVERSE FROM COORDINATES

CODE	KEYS	CODE	KEYS	CODE	KEYS
23	LBL	02	2	34 05	RCL 5
11	A	24	RTN	33 03	STO 3
31	f	23	LBL	61	+
43	REG	14	D	34 01	RCL 1
33 05	STO 5	44	CLX	71	x
33 03	STO 3	35 24	g > y	33	STO
24	RTN	03	3	61	+
23	LBL	06	6	04	4
11	A	00	0	34 07	RCL 7
33 06	STO 6	61	+	84	R/S
24	RTN	41	↑	34 08	RCL 8
23	LBL	41	↑	24	RTN
12	B	09	9	23	LBL
34 05	RCL 5	00	0	15	E
51	-	81	÷	34 04	RCL 4
33	STO	01	1	02	2
61	+	61	+	81	÷
05	5	31	f	35	g
24	RTN	83	INT	06	ABS
23	LBL	33	STO 8	84	R/S
12	B	02	2	04	4
34 06	RCL 6	81	÷	03	3
51	-	31	f	05	5
33	STO	83	INT	06	6
61	+	01	1	00	0
06	6	08	8	81	÷
33 01	STO 1	00	0	84	R/S
24	RTN	71	x	34 02	RCL 2
23	LBL	51	-	24	RTN
13	C	35	g	35 01	g NOP
35 07	g > y	06	ABS		
31	f	31	f		
01	R→P	03	→D.MS		
33	STO	33 07	STO 7		
61	+	34 03	RCL 3		

R ₁ Current dep	R ₄ Area Factor	R ₇ BRG
R ₂ Σ H Dist	R ₅ Beg N	R ₈ QUAD
R ₃ Previous N	R ₆ Beg E	R ₉ Used

SIDESHOTS

CODE	KEYS	CODE	KEYS	CODE	KEYS
23	LBL	24	RTN	35 07	g x \rightarrow y
11	A	23	LBL	32	f $^{-1}$
32	f $^{-1}$	11	A	03	\rightarrow D.MS
03	\rightarrow D.MS	33 07	STO 7	31	f
24	RTN	24	RTN	04	SIN
23	LBL	23	LBL	71	x
11	A	12	B	24	RTN
02	2	01	1	23	LBL
81	\div	08	8	15	E
41	\uparrow	00	0	35 09	g R \uparrow
31	f	31	f	35 07	g x \rightarrow y
83	INT	02	D.MS+	32	f $^{-1}$
35 21	g x \neq y	23	LBL	01	R \rightarrow P
22	GTO	13	C	34 08	RCL 8
01	1	32	f $^{-1}$	61	+
35 09	g R \uparrow	03	\rightarrow D.MS	84	R/S
35 09	g R \uparrow	34 01	RCL 1	35 07	g x \rightarrow y
42	CHS	61	+	34 07	RCL 7
35 09	g R \uparrow	24	RTN	61	+
35 09	g R \uparrow	23	LBL	24	RTN
23	LBL	14	D	35 01	g NOP
01	1	33	STO	35 01	g NOP
35 08	g R \downarrow	09	9	35 01	g NOP
31	f	44	CLX	35 01	g NOP
83	INT	03	3	35 01	g NOP
01	1	00	0	35 01	g NOP
08	8	41	\uparrow	35 01	g NOP
00	0	41	\uparrow	35 01	g NOP
71	x	61	+	35 01	g NOP
61	+	61	+	35 01	g NOP
33 01	STO 1	24	RTN	35 01	g NOP
24	RTN	23	LBL		
23	LBL	14	D		
11	A	34	RCL		
33 08	STO 8	09	9		

R ₁	Current Az.	R ₄	Area Factor	R ₇	Current E
R ₂	Σ H Dist	R ₅	Beg E	R ₈	Current N
R ₃	Previous N	R ₆	Beg N	R ₉	Used



COORDINATE TRANSFORMATION

CODE	KEYS	CODE	KEYS	CODE	KEYS
23	LBL	51	-	24	RTN
11	A	24	RTN	35 01	g NOP
33 01	STO 1	23	LBL	35 01	g NOP
24	RTN	14	D	35 01	g NOP
23	LBL	11	A	35 01	g NOP
33 02	STO 2	33 02	STO 2	35 07	g x \rightarrow y
35 07	g x \rightarrow y	24	RTN	31	f
24	RTN	23	LBL	01	R \rightarrow P
11	A	11	A	34 06	RCL 6
51	-	51	-	35 01	g NOP
33 03	STO 3	33 03	STO 3	35 01	g NOP
35 07	g x \rightarrow y	35 07	g x \rightarrow y	35 01	g NOP
24	RTN	24	RTN	35 01	g NOP
23	LBL	32	f $^{-1}$	35 01	g NOP
11	A	01	R \rightarrow P	34 05	RCL 5
51	-	34 01	RCL 1	35 01	g NOP
33 04	STO 4	61	+	35 01	g NOP
01	1	34 03	RCL 3	35 01	g NOP
24	RTN	24	RTN	35 01	g NOP
23	LBL	51	-	35 01	g NOP
12	B	33 07	STO 7	35 01	g NOP
32	f $^{-1}$	35 07	g x \rightarrow y	35 01	g NOP
03	\rightarrow D.MS	34 02	RCL 2	35 01	g NOP
33 05	STO 5	33 05	STO 5	61	+
01	1	34 04	RCL 4	35 01	g NOP
24	RTN	51	-	35 01	g NOP
23	LBL	33 08	STO 8	35 01	g NOP
13	C	44	CLX	35 01	g NOP
33 06	STO 6	24	RTN	35 01	g NOP
24	RTN	23	LBL	35 01	g NOP
23	LBL	15	E		
14	D	34 07	RCL 7		
34 01	RCL 1	84	R/S		
		34 08	RCL 8		

R ₁	N _P	R ₄	T _E	R ₇	New N
R ₂	E _P	R ₅	ϕ	R ₈	New E
R ₃	T _N	R ₆	Scale Factor	R ₉	Used

COMPASS RULE ADJUSTMENT

CODE	KEYS	CODE	KEYS	CODE	KEYS
23	LBL	61	+	34 01	RCL 1
11	A	02	2	35 01	g NOP
33	STO	35 07	g x \neq y	36 01	g NOP
09	9	34 05	RCL 5	35 01	g NOP
31	f	51	-	35 01	g NOP
61	TF 1	33	STO	35 01	g NOP
84	R/S	61	+	35 01	g NOP
84	R/S	01	1	35 01	g NOP
34 05	RCL 5	31	f	35 01	g NOP
33 01	STO 1	01	R-P	35 01	g NOP
34 07	RCL 7	33	STO	35 01	g NOP
51	-	09	9	35 01	g NOP
34 02	RCL 2	34 03	RCL 3	35 01	g NOP
81	\div	71	x	35 01	g NOP
33 03	STO 3	33	STO	35 01	g NOP
34 06	RCL 6	61	+	35 01	g NOP
34 08	RCL 8	01	1	35 01	g NOP
51	-	34	RCL	35 01	g NOP
34 02	RCL 2	09	9	35 01	g NOP
81	\div	34 04	RCL 4	35 01	g NOP
33 04	STO 4	71	x	35 01	g NOP
34 06	RCL 6	33	STO	35 01	g NOP
33 02	STO 2	61	+	35 01	g NOP
31	f	02	2	35 01	g NOP
51	SF 1	34 08	RCL 8	35 01	g NOP
84	R/S	33 06	STO 6	35 01	g NOP
23	LBL	34 07	RCL 7	35 01	g NOP
12	B	33 05	STO 5	35 01	g NOP
33 07	STO 7	84	R/S	35 01	g NOP
34	RCL	23	LBL	35 01	g NOP
09	9	13	C	35 01	g NOP
33 08	STO 8	34 02	RCL 2	35 01	g NOP
34 06	RCL 6	24	RTN	35 01	g NOP
51	-	23	LBL	14	D
33	STO	14	D	34 07	RCL 7

R ₁	Adj E	R ₄	$\Delta N/\Sigma$ Dist	R ₇	Closing E
R ₂	Adj N	R ₅	Beg E	R ₈	Closing N
R ₃	$\Delta E/\Sigma$ Dist	R ₆	Beg N	R ₉	Used



TRANSIT RULE ADJUSTMENT

CODE	KEYS	CODE	KEYS	CODE	KEYS
23	LBL	34 08	RCL 8	32	f ⁻¹
11	A	11	-	61	TF 1
44	CLX	33	STO	33 06	STO 8
33 01	STO 1	61	+	36 01	g NOP
33 02	STO 2	08	8	51	-
34 07	RCL 7	35	g	41	\uparrow
34 05	RCL 5	06	ABS	33	STO
33 07	STO 7	51	-	61	+
33 03	STO 3	33 08	STO 8	02	2
34 08	RCL 8	34 06	RCL 6	24	RTN
34 06	RCL 6	23	LBL	23	LBL
33 08	STO 7	15	E	15	E
34 05	RCL 5	34 05	RCL 5	32	f ⁻¹
33 04	STO 4	34 04	RCL 4	71	x
24	RTN	35	TF1	51	-
23	LBL	33 07	STO 7	33	STO
12	B	35 01	g NOP	61	+
24	RTN	51	-	08	8
23	LBL	41	\uparrow	31	f
13	C	33	STO	51	SF 1
24	RTN	61	+	34 08	RCL 8
23	LBL	05	5	84	R/S
14	D	35	g	34 07	RCL 7
34 07	RCL 7	06	ABS	24	RTN
51	-	34 01	RCL 1	35 01	g NOP
33	STO	81	\div	35 01	g NOP
61	+	34 03	RCL 3	35 01	g NOP
07	7	71	x	35 01	g NOP
35	g	51	-	35 01	g NOP
06	ABS	33	STO	35 01	g NOP
33	STO	61	+	35 01	g NOP
61	+	07	7	35 01	g NOP
01	1	35 07	g x \neq y	34 06	RCL 6
35 07	g x \neq y				

R ₁	$\Sigma Dep $	R ₄	Closing Lat	R ₇	Adj Easting
R ₂	$\Sigma Lat $	R ₅	Beg Easting	R ₈	Adj Northing
R ₃	Closing Dep	R ₆	Beg Northing	R ₉	



TWO INSTRUMENT RADIAL SURVEY

CODE	KEYS	CODE	KEYS	CODE	KEYS
23	LBL	33 03	STO 3	01	R→P
12	B	24	RTN	24	RTN
32	f ⁻¹	23	LBL	23	LBL
51	SF 1	12	B	15	E
02	2	33 04	STO 4	34 03	RCL 3
81	÷	24	RTN	61	+
41	↑	23	LBL	34 05	RCL 5
31	f	13	C	61	+
83	INT	24	RTN	02	2
35 21	g x ² y	23	LBL	81	÷
31	f	13	C	84	R/S
51	SF 1	12	B	34 05	RCL 5
01	1	24	RTN	51	—
08	8	23	LBL	35 07	g x ² y
00	0	13	C	34 04	RCL 4
71	x	32	f ⁻¹	61	+
35 09	g R↑	01	R→P	34 06	RCL 6
32	f ⁻¹	34 01	RCL 1	61	+
03	→D.MS	61	+	02	2
32	f ⁻¹	33 05	STO 5	81	÷
61	TF 1	35 08	g R↓	84	R/S
42	CHS	34 02	RCL 2	34 06	RCL 6
35 01	g NOP	61	+	51	—
61	+	33 06	STO 6	31	f
24	RTN	24	RTN	01	R→P
23	LBL	23	LBL	02	2
11	A	14	D	71	x
33 01	STO 1	24	RTN	24	RTN
24	RTN	23	LBL	35 01	g NOP
23	LBL	14	D	35 01	g NOP
12	B	12	B	32	f ⁻¹

R ₁	Point 1 N	R ₄	Point 2 E	R ₇
R ₂	Point 1 E	R ₅	First Calc N	R ₈
R ₃	Point 2 N	R ₆	First Calc E	R ₉ Used

CURVE SOLUTION – GIVEN Δ & R OR Δ & T

CODE	KEYS	CODE	KEYS	CODE	KEYS
23	LBL	71	x	15	E
11	A	34 06	RCL 6	34 01	RCL 1
33 02	STO 2	71	x	84	R/S
32	f ⁻¹	09	9	34 02	RCL 2
03	→D.MS	00	0	84	R/S
02	2	81	÷	34 06	RCL 6
81	÷	33 05	STO 5	31	f
33 06	STO 6	24	RTN	03	→D.MS
84	R/S	23	LBL	84	R/S
23	LBL	14	D	34 03	RCL 3
12	B	34 06	RCL 5	84	R/S
35 07	g x ² y	34 01	RCL 1	34 04	RCL 4
31	f	71	x	84	R/S
06	TAN	02	2	34 05	RCL 5
71	x	81	÷	84	R/S
34 06	RCL 6	33 07	STO 7	35 01	g NOP
35 07	g x ² y	84	R/S	35 01	g NOP
23	LBL	34 06	RCL 6	35 01	g NOP
13	C	31	f	35 01	g NOP
33 04	STO 4	05	COS	35 01	g NOP
35 07	g x ² y	34 01	RCL 1	35 01	g NOP
31	f	71	x	35 01	g NOP
06	COS	34 03	RCL 3	35 01	g NOP
71	x	71	x	35 01	g NOP
33 03	STO 3	02	2	35 01	g NOP
33	STO	81	÷	35 01	g NOP
61	+	51	—	35 01	g NOP
03	3	84	R/S	35 01	g NOP
34 06	RCL 6	34 04	RCL 4	35 01	g NOP
31	f	34 01	RCL 1	35 01	g NOP
04	SIN	71	x	35 01	g NOP
81	÷	34 07	RCL 7	35 01	g NOP
33 01	STO 1	51	—	35 01	g NOP
35	g	24	RTN	35 01	g NOP
02	π	23	LBL	35 01	g NOP

R ₁	R	R ₄	T	R ₇	Sector Area
R ₂	Δ	R ₅	L	R ₈	
R ₃	C	R ₆	½ Δ	R ₉	Used

CURVE SOLUTION - GIVEN R & T OR R & L

CODE	KEYS	CODE	KEYS	CODE	KEYS
23	LBL	71	x	24	RTN
11	A	33 04	STO 4	23	LBL
33 01	STO 1	34 06	RCL 6	15	E
24	RTN	31	f	34 01	RCL 1
23	LBL	05	COS	84	R/S
12	B	71	x	34 06	RCL 6
35 07	g x ² y	02	2	02	2
81	÷	71	x	71	x
32	f ⁻¹	33 03	STO 3	31	f
06	TAN	24	RTN	03	→D.MS
09	9	23	LBL	84	R/S
00	0	14	D	34 06	RCL 6
81	÷	34 05	RCL 5	31	f
35	g	34 01	RCL 1	03	→D.MS
02	π	71	x	84	R/S
71	x	02	2	34 03	RCL 3
34 01	RCL 1	81	÷	84	R/S
71	x	33 07	STO 7	34 04	RCL 4
34 01	RCL 1	84	R/S	84	R/S
35 07	g x ² y	34 06	RCL 6	34 05	RCL 5
23	LBL	31	f	34 06	RCL 6
13	C	05	COS	31	f
33 05	STO 5	34 01	RCL 1	06	TAN
09	9	71	x	71	x
00	0	34 03	RCL 3	33 04	STO 4
71	x	71	x	34 06	RCL 6
35	g	02	2	09	9
02	π	81	÷	00	0
81	÷	51	—	81	÷
35 07	g x ² y	84	R/S	35 01	g NOP
81	÷	34 04	RCL 4	35 01	g NOP
33 06	STO 6	34 01	RCL 1	35 01	g NOP
31	f	71	x	35 01	g NOP
06	TAN	34 07	RCL 7	35 01	g NOP
34 01	RCL 1	51	—	35 01	g NOP

R ₁	R	R ₄	T	R ₇	Sector Area
R ₂		R ₅	L	R ₈	
R ₃	C	R ₆	½ Δ	R ₉	Used

CURVE SOLUTION - GIVEN Δ & C OR R & C

CODE	KEYS	CODE	KEYS	CODE	KEYS
23	LBL	23	LBL	34 04	RCL 4
11	A	13	C	34 01	RCL 1
33 03	STO 3	02	2	71	x
24	RTN	71	x	34 07	RCL 7
23	LBL	81	÷	51	—
12	B	32	f ⁻¹	24	RTN
33 02	STO 2	04	SIN	23	LBL
32	f ⁻¹	02	2	15	E
02	2	31	f	34 01	RCL 1
81	÷	03	→D.MS	84	R/S
33 06	STO 6	34 03	RCL 3	34 02	RCL 2
31	f	35 07	g x ² y	84	R/S
04	SIN	12	B	34 06	RCL 6
81	÷	84	R/S	03	→D.MS
02	2	23	LBL	84	R/S
81	÷	14	D	34 03	RCL 3
33 01	STO 1	34 05	RCL 5	84	R/S
34 06	RCL 6	34 01	RCL 1	34 04	RCL 4
31	f	71	x	84	R/S
06	TAN	02	2	34 05	RCL 5
71	x	81	÷	84	R/S
33 04	STO 4	33 07	STO 7	35 01	g NOP
34 06	RCL 6	84	R/S	35 01	g NOP
09	9	34 06	RCL 6	35 01	g NOP
00	0	31	f	35 01	g NOP
81	÷	05	COS	35 01	g NOP
35	g	34 01	RCL 1	35 01	g NOP
02	π	71	x	34 03	RCL 3
71	x	34 01	RCL 1	84	R/S
34 01	RCL 1	71	x	02	2
71	x	81	÷	33 05	STO 5
33 05	STO 5	44	CLX	51	—
24	RTN	24	RTN	84	R/S

R ₁	R	R ₄	T	R ₇	Sector Area
R ₂		R ₅	L	R ₈	
R ₃	C	R ₆	½ Δ	R ₉	Used

ELEVATIONS ALONG A VERTICAL CURVE

CODE	KEYS	CODE	KEYS	CODE	KEYS
23	LBL	81	÷	71	x
11	A	23	LBL	34	06 RCL 6
41	↑	01	1	61	+
33 01	STO 1	33 04	STO 4	24	RTN
24	RTN	41	↑	35 01	g NOP
23	LBL	32	f ⁻¹	35 01	g NOP
11	A	09	✓x	35 01	g NOP
35 07	g x ² y	34 03	RCL 3	35 01	g NOP
51	-	71	x	35 01	g NOP
05	5	35 07	g x ² y	35 01	g NOP
00	0	34 01	RCL 1	35 01	g NOP
71	x	71	x	35 01	g NOP
33 03	STO 3	61	+	35 01	g NOP
44	CLX	34 02	RCL 2	35 01	g NOP
24	RTN	61	+	35 01	g NOP
23	LBL	33 05	STO 5	35 01	g NOP
12	B	44	CLX	35 01	g NOP
33 06	STO 6	84	R/S	35 01	g NOP
24	RTN	23	LBL	35 01	g NOP
23	LBL	14	D	35 01	g NOP
33 02	STO 2	34 01	RCL 1	35 01	g NOP
24	RTN	42	CHS	35 01	g NOP
23	LBL	02	2	35 01	g NOP
12	B	81	÷	35 01	g NOP
33	STO	34 03	RCL 3	35 01	g NOP
81	÷	81	÷	35 01	g NOP
03	3	22	GTO	35 01	g NOP
24	RTN	01	1	35 01	g NOP
23	LBL	23	LBL	35 01	g NOP
13	C	15	E	35 01	g NOP
34 06	RCL 6	34 05	RCL 5	35 01	g NOP
51	-	84	R/S	34 04	RCL 4
43	EEX	34 04	RCL 4	43	EEX
02	2	02	2	02	2

R ₁ Grade 1	R ₄ No of Stations	R ₇
R ₂ Beg Elevation	R ₅ Elev at Sta	R ₈
R ₃ A/2	R ₆ Beg Sta	R ₉



HORIZONTAL CURVE LAYOUT

CODE	KEYS	CODE	KEYS	CODE	KEYS
23	LBL	34 04	RCL 4	35 01	g NOP
11	A	31	f	35 01	g NOP
33 01	STO 1	03	→D.MS	35 01	g NOP
35	g	24	RTN	35 01	g NOP
02	π	23	LBL	35 01	g NOP
71	x	15	E	35 01	g NOP
35	g	34 05	RCL 5	35 01	g NOP
04	1/x	24	RTN	35 01	g NOP
09	9	35 01	g NOP	35 01	g NOP
00	0	35 01	g NOP	35 01	g NOP
71	x	33 02	STO 2	35 01	g NOP
33 02	STO 2	24	RTN	35 01	g NOP
24	RTN	23	LBL	35 01	g NOP
12	B	12	B	35 01	g NOP
33 03	STO 3	33 03	STO 3	35 01	g NOP
24	RTN	24	RTN	35 01	g NOP
23	LBL	23	LBL	35 01	g NOP
13	C	13	C	35 01	g NOP
34 03	RCL 3	34 03	RCL 3	35 01	g NOP
51	-	51	-	35 01	g NOP
34 02	RCL 2	34 02	RCL 2	35 01	g NOP
71	x	71	x	35 01	g NOP
33 04	STO 4	33 04	STO 4	35 01	g NOP
31	f	31	f	35 01	g NOP
04	SIN	04	SIN	35 01	g NOP
34 01	RCL 1	34 01	RCL 1	35 01	g NOP
71	x	71	x	35 01	g NOP
02	2	02	2	35 01	g NOP
71	x	33 05	STO 5	35 01	g NOP
33 05	STO 5	44	CLX	35 01	g NOP
24	RTN	24	RTN	35 01	g NOP
23	LBL	23	LBL	35 01	g NOP
14	D	14	D	35 01	g NOP

R ₁ Radius	R ₄ Defl Ang	R ₇
R ₂ Defl/Ft	R ₅ Chord	R ₈
R ₃ PC Sta	R ₆	R ₉ Used

TRIANGLE SOLUTION – GIVEN SSS OR SAS

CODE	KEYS	CODE	KEYS	CODE	KEYS
23	LBL	51	–	84	R/S
11	A	31	f	33 05	STO 5
33 01	STO 1	09	\sqrt{x}	34 02	RCL 2
84	R/S	33 03	STO 3	34 01	RCL 1
23	LBL	23	LBL	33 02	STO 2
12	B	13	C	35 07	$g x^2 y$
32	f^{-1}	34 02	RCL 2	33 01	STO 1
03	$\rightarrow D.MS$	34 03	RCL 3	13	C
33 06	STO 6	31	f	33 06	STO 6
84	R/S	01	$R \rightarrow P$	84	R/S
23	LBL	32	f^{-1}	23	LBL
11	A	09	\sqrt{x}	15	E
33 02	STO 2	34 01	RCL 1	34 02	RCL 2
84	R/S	84	R/S	34 03	RCL 3
23	LBL	32	f^{-1}	71	x
11	A	09	\sqrt{x}	02	2
33 03	STO 3	51	–	81	\div
84	R/S	34 02	RCL 2	34 06	RCL 6
23	LBL	34 03	RCL 3	32	f^{-1}
14	D	02	2	03	$\rightarrow D.MS$
34 01	RCL 1	71	x	31	f
34 02	RCL 2	71	x	04	SIN
31	f	81	\div	71	x
01	$R \rightarrow P$	32	f^{-1}	24	RTN
32	f^{-1}	06	COS	35 01	$g NOP$
09	\sqrt{x}	31	f	35 01	$g NOP$
34 01	RCL 1	03	$\rightarrow D.MS$	35 01	$g NOP$
34 02	RCL 2	24	RTN	35 01	$g NOP$
02	2	33 04	STO 4	35 01	$g NOP$
71	x	34 03	RCL 3	35 01	$g NOP$
71	x	34 01	RCL 1	33 03	STO 3
34 06	RCL 6	33 03	STO 3	36 07	$g x^2 y$
31	f	36 07	$g x^2 y$	33 01	STO 1
06	COS	33 01	STO 1	13	C
71	x				

R ₁	Side 3	R ₄	Angle	R ₇	
R ₂	Side 2	R ₅	Angle	R ₈	
R ₃	Side 1	R ₆	Angle	R ₉	Used

TRIANGLE SOLUTION – GIVEN SSA

CODE	KEYS	CODE	KEYS	CODE	KEYS
23	LBL	09	\sqrt{x}	34 05	RCL 5
11	A	51	–	84	R/S
33 01	STO 1	31	f	31	\sqrt{x}
84	R/S	09	\sqrt{x}	02	D.MS +
23	LBL	31	f	34 03	RCL 3
11	A	61	TF 1	84	R/S
33 02	STO 2	35 01	$g NOP$	44	CLX
84	R/S	42	CHS	01	1
23	LBL	35 09	$g R \uparrow$	08	8
12	B	61	+	00	0
33 05	STO 5	33 03	STO 3	35 07	$g x^2 y$
84	R/S	34 02	RCL 2	32	f^{-1}
23	LBL	31	f	02	D.MS +
13	C	01	$R \rightarrow P$	84	R/S
31	f	32	f^{-1}	23	LBL
51	SF 1	09	\sqrt{x}	15	E
22	GTO	34 01	RCL 1	34 01	RCL 1
01	1	84	R/S	34 03	RCL 3
23	LBL	32	f^{-1}	34 05	RCL 5
14	D	09	\sqrt{x}	32	f^{-1}
32	f^{-1}	51	–	03	$\rightarrow D.MS$
51	SF 1	34 02	RCL 2	31	f
23	LBL	34 03	RCL 3	04	SIN
01	1	71	x	71	x
34 02	RCL 2	81	\div	71	x
32	f^{-1}	02	2	02	2
09	\sqrt{x}	81	\div	81	\div
34 05	RCL 5	32	f^{-1}	84	R/S
32	f^{-1}	05	COS	35 01	$g NOP$
03	$\rightarrow D.MS$	31	f	36 01	$g NOP$
34 01	RCL 1	03	$\rightarrow D.MS$		
32	f^{-1}	84	R/S		
01	$R \rightarrow P$	34 02	RCL 2		
35 08	$g R \downarrow$	84	R/S		
32	f^{-1}	44	CLX		

R ₁	Side 1	R ₄		R ₇	
R ₂	Side 2	R ₅	Angle 2	R ₈	
R ₃	Side 3	R ₆	Angle 3	R ₉	Used

TRIANGLE SOLUTION – GIVEN ASA OR AAS

CODE	KEYS	CODE	KEYS	CODE	KEYS
23	LBL	02	D.MS +	84	R/S
12	B	34 05	RCL 5	34 06	RCL 6
33 04	STO 4	32	f ⁻¹	84	R/S
84	R/S	02	D.MS +	23	LBL
23	LBL	33 06	STO 6	15	E
12	B	32	f ⁻¹	34 01	RCL 1
33 06	STO 6	03	→D.MS	34 03	RCL 3
84	R/S	31	f	34 07	RCL 7
23	LBL	04	SIN	71	x
11	A	34 03	RCL 3	71	x
33 03	STO 3	35 07	g x ² y	02	2
84	R/S	81	÷	81	÷
23	LBL	33 07	STO 7	84	R/S
12	B	34 04	RCL 4	35 01	g NOP
33 05	STO 5	32	f ⁻¹	35 01	g NOP
84	R/S	03	→D.MS	35 01	g NOP
23	LBL	31	f	35 01	g NOP
14	D	04	SIN	35 01	g NOP
01	1	71	x	35 01	g NOP
08	8	84	R/S	35 01	g NOP
00	0	33 01	STO 1	35 01	g NOP
34 04	RCL 4	34 04	RCL 4	35 01	g NOP
32	f ⁻¹	34 07	RCL 7	35 01	g NOP
02	D.MS +	34 05	RCL 5	35 01	g NOP
34 06	RCL 6	32	f ⁻¹	35 01	g NOP
02	D.MS +	03	→D.MS	35 01	g NOP
33 05	STO 5	31	f	35 01	g NOP
23	LBL	04	SIN	35 01	g NOP
13	C	33 07	STO 7	35 01	g NOP
01	1	71	x	35 01	g NOP
08	8	84	R/S		
00	0	34 06	RCL 5		
34 04	RCL 4	84	R/S		
32	f ⁻¹	34 03	RCL 3		

R ₁ Side 1	R ₄ Angle 1	R ₇ Used
R ₂	R ₅ Angle 2	R ₈
R ₃ Side 3	R ₆ Angle 3	R ₉ Used

BEARING – BEARING INTERSECT

CODE	KEYS	CODE	KEYS	CODE	KEYS
23	LBL	22	GTO	23	LBL
11	A	01	1	15	E
33 01	STO 1	34 05	RCL 5	34 04	RCL 4
84	R/S	42	CHS	34 03	RCL 3
23	LBL	33 05	STO 5	34 06	RCL 6
11	A	23	LBL	71	x
33 02	STO 2	01	1	51	–
84	R/S	84	R/S	34 02	RCL 2
23	LBL	23	LBL	34 01	RCL 1
12	B	14	D	34 06	RCL 5
33 03	STO 3	32	f ⁻¹	71	x
84	R/S	03	→D.MS	51	–
23	LBL	31	f	33 07	STO 7
12	B	06	TAN	51	–
33 04	STO 4	33 06	STO 6	34 05	RCL 5
84	R/S	35 00	g LST X	34 06	RCL 6
23	LBL	84	R/S	51	–
13	C	23	LBL	81	÷
32	f ⁻¹	14	D	84	R/S
03	→D.MS	41	↑	34 05	RCL 5
31	f	01	1	71	x
06	TAN	35 23	g x = y	34 07	RCL 7
33 05	STO 5	22	GTO	61	+
35 00	g LST X	02	2	84	R/S
84	R/S	44	CLX	35 01	g NOP
23	LBL	03	3	35 01	g NOP
13	C	35 23	g x = y	35 01	g NOP
41	↑	22	GTO	35 01	g NOP
01	1	02	2	35 01	g NOP
35 23	g x = y	34 06	RCL 6		
22	GTO	42	CHS		
01	1	33 06	STO 6		
44	CLX	23	LBL		
03	3	02	2		
35 23	g x = y	84	R/S		

R ₁ Point 1N	R ₄ Point 2E	R ₇ Used
R ₂ Point 1E	R ₅ Line 1 TAN (AZ)	R ₈
R ₃ Point 2N	R ₆ Line 2 TAN (AZ)	R ₉ Used

BEARING - DISTANCE INTERSECT

CODE	KEYS	CODE	KEYS	CODE	KEYS
23	LBL	35 09	g R↑	34 07	RCL 7
11	A	35 09	g R↑	32	f⁻¹
33 01	STO 1	23	LBL	01	R→P
84	R/S	01	1	35 07	g x \leftrightarrow y
23	LBL	44	CLX	32	f⁻¹
11	A	01	1	09	\sqrt{x}
33 02	STO 2	08	8	34 06	RCL 6
84	R/S	00	0	32	f⁻¹
23	LBL	71	x	09	\sqrt{x}
12	B	61	+	35 07	g x \leftrightarrow y
33 03	STO 3	33 05	STO 5	51	-
84	R/S	84	R/S	31	f
23	LBL	23	LBL	09	\sqrt{x}
12	B	14	D	61	+
33 04	STO 4	33 06	STO 6	34 06	RCL 5
84	R/S	84	R/S	35 07	g x \leftrightarrow y
23	LBL	23	LBL	32	f⁻¹
13	C	15	E	01	R→P
32	f⁻¹	34 04	RCL 4	01	RCL 1
03	→D.MS	34 02	RCL 2	61	+
84	R/S	51	-	84	R/S
23	LBL	34 03	RCL 3	35 07	g x \leftrightarrow y
13	C	34 01	RCL 1	34 02	RCL 2
02	2	51	-	61	+
81	÷	31	f	84	R/S
41	↑	01	R→P	35 01	g NOP
31	f	33 07	STO 7	35 01	g NOP
83	INT	44	CLX	35 01	g NOP
35 07	g x \leftrightarrow y	35 24	g x \leftrightarrow y	35 01	g NOP
35 21	g x \leftrightarrow y	03	3	35 01	g NOP
22	GTO	06	6	35 01	g NOP
01	1	00	0	35 01	g NOP
36 09	g R↑	61	+	34 05	RCL 5
35 09	g R↑	34 05	RCL 5	51	-
42	CHS				

R ₁ Point 1N	R ₄ Point 2E	R ₇ Dist 1→2
R ₂ Point 1E	R ₅ Line 1Az	R ₈
R ₃ Point 2N	R ₆ Line 2-Dist	R ₉ Used

DISTANCE - DISTANCE INTERSECT

CODE	KEYS	CODE	KEYS	CODE	KEYS
23	LBL	32	f⁻¹	35 01	g NOP
11	A	09	\sqrt{x}	35 01	g NOP
33 01	STO 1	34 05	RCL 5	35 01	g NOP
84	R/S	32	f⁻¹	35 01	g NOP
23	LBL	09	\sqrt{x}	35 01	g NOP
12	B	61	+	35 01	g NOP
33 02	STO 2	34 06	RCL 6	35 01	g NOP
84	R/S	32	f⁻¹	35 01	g NOP
23	LBL	09	\sqrt{x}	35 01	g NOP
12	B	51	-	35 01	g NOP
33 03	STO 3	02	2	35 01	g NOP
84	R/S	81	÷	35 01	g NOP
23	LBL	34 07	RCL 7	35 01	g NOP
12	B	34 05	RCL 5	35 01	g NOP
33 04	STO 4	71	x	35 01	g NOP
84	R/S	81	÷	35 01	g NOP
23	LBL	32	f⁻¹	35 01	g NOP
13	C	05	COS	35 01	g NOP
33 05	STO 5	51	-	35 01	g NOP
84	R/S	34 05	RCL 5	35 01	g NOP
23	LBL	32	f⁻¹	35 01	g NOP
14	D	01	R→P	35 01	g NOP
33 06	STO 6	34 01	RCL 1	35 01	g NOP
84	R/S	61	+	35 01	g NOP
23	LBL	84	R/S	35 01	g NOP
15	E	35 07	g x \leftrightarrow y	35 01	g NOP
34 04	RCL 4	34 02	RCL 2	35 01	g NOP
34 02	RCL 2	61	+	35 01	g NOP
51	-	84	R/S	35 01	g NOP
34 03	RCL 3	35 01	g NOP	35 01	g NOP
34 01	RCL 1	35 01	g NOP	35 01	g NOP
51	-	35 01	g NOP	35 01	g NOP
31	f	35 01	g NOP	35 01	g NOP
01	R→P	35 01	g NOP	35 01	g NOP
33 07	STO 7	35 01	g NOP	35 01	g NOP

R ₁ Point 1 N	R ₄ Point 2 E	R ₇ Dist 1→2
R ₂ Point 1 E	R ₅ Dist 1	R ₈
R ₃ Point 2 N	R ₆ Dist 2	R ₉ Used

DISTANCE FROM A POINT TO A LINE

CODE	KEYS	CODE	KEYS	CODE	KEYS
23	LBL	23	LBL	33 03	STO 3
11	A	13	C	84	R/S
31	f	33 04	STO 4	23	LBL
43	REG	84	R/S	15	E
33 01	STO 1	23	LBL	34 04	RCL 4
84	R/S	13	C	34 08	RCL 8
23	LBL	33 05	STO 5	51	-
11	A	84	R/S	34 05	RCL 5
33 02	STO 2	23	LBL	34 03	RCL 3
84	R/S	14	D	51	-
23	LBL	34 02	RCL 2	31	f
12	B	34 01	RCL 1	01	R→P
32	f ⁻¹	34 03	RCL 3	84	R/S
03	→D.MS	71	x	34 01	RCL 1
31	f	51	-	34 08	RCL 8
06	TAN	33 07	STO 7	51	-
33 03	STO 3	34 06	RCL 5	34 02	RCL 2
84	R/S	34 04	RCL 4	34 03	RCL 3
23	LBL	34 03	RCL 3	51	-
12	B	81	÷	31	f
02	2	61	+	01	R→P
81	÷	51	-	24	RTN
32	f ⁻¹	34 03	RCL 3	35 01	g NOP
83	INT	41	↑	35 01	g NOP
83	.	35	g	35 01	g NOP
04	4	04	1/k	35 01	g NOP
35 22	g x≤y	61	+	35 01	g NOP
22	GTO	42	CHS	35 01	g NOP
01	1	81	÷	35 01	g NOP
34 03	RCL 3	33 08	STO 8	35 01	g NOP
42	CHS	84	R/S		
33 03	STO 3	34 03	RCL 3		
23	LBL	71	x		
01	1	34 07	RCL 7		
84	R/S	61	+		

R ₁	Point 1 N	R ₄	Point 2 N	R ₇	Used
R ₂	Point 1 E	R ₅	Point 2 E	R ₈	Point 3 N
R ₃	Point 3 E	R ₆		R ₉	Used

TAPING CORRECTIONS

CODE	KEYS	CODE	KEYS	CODE	KEYS	CODE	KEYS
23	LBL	33 02	STO 2	22	GTO		
11	A	84	R/S	01	1		
33 03	STO 3	23	LBL	23	LBL		
02	2	13	C	15	E		
00	0	33 06	STO 6	41	↑		
51	-	83	·	71	x		
03	3	00	0	42	CHS		
43	EEX	01	1	34 06	RCL 6		
05	5	04	4	41	↑		
81	÷	71	x	71	x		
83	·	34 03	RCL 3	61	+		
00	0	81	÷	31	f		
00	0	41	↑	09	√x		
41	↑	71	x	23	LBL		
43	EEX	02	2	01	1		
02	2	04	4	33	STO		
81	÷	81	÷	61	+		
61	+	42	CHS	05	5		
33 01	STO 1	34 02	RCL 2	84	R/S		
84	R/S	01	1	34 05	RCL 5		
23	LBL	61	+	24	RTN		
12	B	61	+	35 01	g NOP		
06	6	34 06	RCL 6	35 01	g NOP		
08	8	71	x	35 01	g NOP		
51	-	33 06	STO 6	35 01	g NOP		
06	6	44	CLX	35 01	g NOP		
04	4	84	R/S	35 01	g NOP		
05	5	23	LBL	35 01	g NOP		
43	EEX	14	D	36 01	g NOP		
42	CHS	32	f ⁻¹	35 01	g NOP		
08	8	03	→D.MS	36 01	g NOP		
71	x	31	f	36 01	g NOP		
34 01	RCL 1	04	SIN	35 01	g NOP		
61	+	34 06	RCL 6	36 01	g NOP		
		71	x	35 01	g NOP		

R ₁	Used	R ₄		R ₇	
R ₂	Used	R ₅	Σ H Dist	R ₈	
R ₃	Lbs Pull	R ₆	S Dist	R ₉	

EDM SLOPE REDUCTION - GIVEN ZENITH ANGLE

CODE	KEYS	CODE	KEYS	CODE	KEYS
23	LBL	51	-	33	STO
11	A	34 06	RCL 6	61	+
33 01	STO 1	02	2	02	2
84	R/S	43	EEX	24	RTN
23	LBL	42	CHS	23	LBL
11	A	07	7	15	E
02	2	71	X	34 01	RCL 1
00	0	61	+	34 04	RCL 4
09	9	33 02	STO 2	31	f
00	0	24	RTN	05	COS
06	6	23	LBL	81	÷
43	EEX	13	C	33 01	STO 1
03	3	84	R/S	34 02	RCL 2
61	+	23	LBL	34 04	RCL 4
35 00	g LST X	13	C	51	-
81	÷	51	-	31	f
33 05	STO 5	33 06	STO 6	04	SIN
24	RTN	84	R/S	71	X
23	LBL	23	LBL	84	R/S
12	B	14	D	34 05	RCL 5
32	f ⁻¹	51	-	81	÷
03	→D.MS	84	R/S	84	R/S
41	↑	23	LBL	34 01	RCL 1
31	f	14	D	34 02	RCL 2
04	SIN	61	+	31	f
34 01	RCL 1	34 01	RCL 1	05	COS
71	X	81	÷	71	X
33 06	STO 6	34 02	RCL 2	34 06	RCL 6
01	1	34 04	RCL 4	61	+
04	4	51	-	84	R/S
43	EEX	31	f		
42	CHS	04	SIN		
07	7	71	X		
71	X	32	f ⁻¹		
33 04	STO 4	04	SIN		

R_1 S Dist/used	R_4 c	R_7
R_2 Z ₁ /used	R_5 (R + E) / R	R_8
R_3	R_6 Used	R_9 Used

EDM SLOPE REDUCTION - GIVEN Δ ELEVATION

CODE	KEYS	CODE	KEYS	CODE	KEYS
23	LBL	14	D	34 04	RCL 4
11	A	33 04	STO 4	34 05	RCL 5
33 01	STO 1	24	RTN	61	+
02	2	23	LBL	71	X
00	0	15	E	24	RTN
09	9	34 01	RCL 1	35 01	g NOP
00	0	32	f ⁻¹	35 01	g NOP
06	6	09	✓X	34 03	RCL 3
00	0	34 02	RCL 2	35 01	g NOP
00	0	51	-	35 01	g NOP
33 05	STO 5	32	f ⁻¹	35 01	g NOP
24	RTN	09	✓X	35 01	g NOP
23	LBL	51	-	35 01	g NOP
12	B	34 05	RCL 5	35 01	g NOP
33 02	STO 2	34 02	RCL 2	35 01	g NOP
24	RTN	61	+	35 01	g NOP
23	LBL	81	÷	35 01	g NOP
13	C	34 05	RCL 5	35 01	g NOP
33 03	STO 3	34 03	RCL 3	35 01	g NOP
24	RTN	61	+	35 01	g NOP
23	LBL	81	÷	35 01	g NOP
14	D	31	f	35 01	g NOP
33 07	STO 7	09	✓X	35 01	g NOP
84	R/S	33 06	STO 6	35 01	g NOP
23	LBL	34 05	RCL 5	35 01	g NOP
14	D	34 07	RCL 7	35 01	g NOP
33	STO	61	+	35 01	g NOP
61	+	71	X	35 01	g NOP
03	3	84	R/S	35 01	g NOP
84	R/S	34 06	RCL 6	35 01	g NOP
23	LBL	34 05	RCL 5		

R_1 S Dist	R_4 E _s	R_7 E ₁
R_2 HI DM + E ₁	R_5 R	R_8
R_3 HT Rft + E ₂	R_6 Used	R_9

FIELD ANGLE CHECK

CODE	KEYS	CODE	KEYS	CODE	KEYS
23	LBL	83	DS Z	24	RTN
11	A	01	1	23	LBL
32	f ⁻¹	32	f ⁻¹	14	D
03	→D.MS	01	R→P	34	04 RCL 4
01	1	31	f	31	f
08	8	01	R→P	03	→D.MS
00	0	44	CLX	84	R/S
51	—	35	24 g x>y	34	03 RCL 3
31	f	03	3	84	R/S
61	TF 1	06	6	34	02 RCL 2
22	GTO	00	0	31	f
01	1	61	+	03	→D.MS
31	f	33	02 STO 2	84	R/S
43	REG	09	9	23	LBL
33 02	STO 2	00	0	15	E
23	LBL	81	÷	34	01 RCL 1
01	1	01	1	34	02 RCL 2
33 01	STO 1	61	+	51	—
31	f	31	f	31	f
51	SF 1	83	INT	03	→D.MS
24	RTN	33	03 STO 3	84	R/S
23	LBL	02	2	32	f ⁻¹
12	B	81	÷	03	→D.MS
01	1	31	f	34	08 RCL 8
08	8	83	INT	81	÷
00	0	01	1	31	f
31	f	08	8	03	→D.MS
02	D.MS +	00	0	32	f ⁻¹
23	LBL	71	x	51	SF 1
13	C	34	02 RCL 2	24	RTN
32	f ⁻¹	51	—		
03	→D.MS	35	g		
34 02	RCL 2	06	ABS		
61	+	33	04 STO 4		
35	g	44	CLX		

R ₁ Ref Az -180	R ₄ Bearing	R ₇
R ₂ Current Az	R ₅	R ₈ Counter
R ₃ Quad Code	R ₆	R ₉ Used

STADIA REDUCTIONS

CODE	KEYS	CODE	KEYS	CODE	KEYS
23	LBL	32	f ⁻¹	35 01	g NOP
11	A	09	✓x	35 01	g NOP
33 05	STO 5	34 03	RCL 3	35 01	g NOP
84	R/S	71	x	35 01	g NOP
23	LBL	01	1	35 01	g NOP
11	A	00	0	35 01	g NOP
33 01	STO 1	00	0	35 01	g NOP
33 04	STO 4	71	x	35 01	g NOP
84	R/S	84	R/S	35 01	g NOP
23	LBL	02	2	35 01	g NOP
12	B	71	x	35 01	g NOP
32	f ⁻¹	31	f	35 01	g NOP
03	→D.MS	04	SIN	35 01	g NOP
09	9	05	5	35 01	g NOP
00	0	00	0	35 01	g NOP
35 07	g x>y	71	x	35 01	g NOP
51	—	33 02	STO 2	35 01	g NOP
35 00	g LST X	34 03	RCL 3	35 01	g NOP
31	f	71	x	35 01	g NOP
03	→D.MS	34 04	RCL 4	35 01	g NOP
84	R/S	51	—	35 01	g NOP
23	LBL	34 01	RCL 1	35 01	g NOP
13	C	33 04	STO 4	35 01	g NOP
33 03	STO 3	61	+	35 01	g NOP
84	R/S	34 05	RCL 5	35 01	g NOP
23	LBL	61	+	35 01	g NOP
14	D	84	R/S	35 01	g NOP
33 04	STO 4	35 01	g NOP	35 01	g NOP
84	R/S	35 01	g NOP	35 01	g NOP
23	LBL	35 01	g NOP	35 01	g NOP
15	E	35 01	g NOP	35 01	g NOP
34 02	RCL 2	35 01	g NOP	35 01	g NOP
31	f	35 01	g NOP	35 01	g NOP
05	COS	35 01	g NOP	35 01	g NOP

R ₁ Ht Instrument	R ₄ Rod Reading	R ₇
R ₂ Vertical Angle	R ₅ Sta Elev	R ₈
R ₃ Rod Inter	R ₆	R ₉ Used

THREE WIRE LEVELING

CODE	KEYS	CODE	KEYS
23	LBL	14	D
11	A	33	STO
33 01	STO 1	61	+
01	1	07	7
00	0	51	-
00	0	61	+
33 08	STO 8	35 00	g LST X
84	R/S	02	2
23	LBL	71	x
11	A	35 07	g x ² y
33 08	STO 8	51	-
84	R/S	35 00	g LST X
23	LBL	34 07	RCL 7
12	B	03	3
31	f	81	÷
51	SF 1	31	f
84	R/S	61	TF 1
23	LBL	22	GTO
13	C	01	1
32	f ⁻¹	33	STO
51	SF 1	61	+
84	R/S	05	5
23	LBL	35 08	g R ↓
14	D	33	STO
33 07	STO 7	61	+
84	R/S	06	6
23	LBL	35 08	g R ↓
14	D	84	R/S
33	STO	23	LBL
61	+	01	1
07	7	33	STO
51	-	61	+
35 00	g LST X	02	2
84	R/S	35 08	g R ↓
23	LBL	33	STO

R ₁ Elev	R ₄	R ₇ Used
R ₂ Σ BS Means	R ₅ Σ FS Means	R ₈ Stadia Intr K
R ₃ Σ BS Intervals	R ₆ Σ FS Intervals	R ₉

SLOPE STAKING – GIVEN CENTERLINE
TERRAIN ELEVATION

CODE	KEYS	CODE	KEYS	CODE	KEYS
23	LBL	71	x	01	1
11	A	33 04	STO 4	84	R/S
84	R/S	33 05	STO 5	23	LBL
23	LBL	22	GTO	15	E
11	A	01	1	34 05	RCL 5
33 01	STO 1	23	LBL	34 04	RCL 4
84	R/S	14	D	51	-
23	LBL	33 04	STO 4	84	R/S
12	B	33 05	STO 5	34 05	RCL 5
84	R/S	84	R/S	24	RTN
23	LBL	23	LBL	35 01	g NOP
12	B	14	D	35 01	g NOP
51	-	35 07	g x ² y	35 01	g NOP
71	x	81	÷	35 01	g NOP
61	+	34 01	RCL 1	35 01	g NOP
33 02	STO 2	71	x	35 01	g NOP
84	R/S	01	1	35 01	g NOP
23	LBL	51	-	35 01	g NOP
13	C	33 03	STO 3	35 01	g NOP
84	R/S	23	LBL	35 01	g NOP
23	LBL	01	1	35 01	g NOP
13	C	34 02	RCL 2	35 01	g NOP
32	f ⁻¹	34 03	RCL 3	35 01	g NOP
03	→D.MS	34 05	RCL 5	35 01	g NOP
31	f	71	x	35 01	g NOP
05	COS	61	+	35 01	g NOP
35 00	g LST X	33	STO	35 01	g NOP
31	f	61	+	35 01	g NOP
06	TAN	05	5	35 01	g NOP
34 01	RCL 1	35	g	35 01	g NOP
71	x	06	ABS	35 01	g NOP
01	1	83	*	35 01	g NOP
51	-	01	1	35 01	g NOP
33 03	STO 3	35 22	g x ² y	35 01	g NOP
g R ↓		22	GTO	35 01	g NOP

R ₁ Slope	R ₄ H Dist	R ₇
R ₂ Used	R ₅ H Dist	R ₈
R ₃ Used	R ₆	R ₉ Used

SLOPE STAKING – GIVEN CENTERLINE CUT/FILL

CODE	KEYS	CODE	KEYS	CODE	KEYS
23	LBL	71	x	01	1
11	A	33 04	STO 4	84	R/S
84	R/S	33 05	STO 5	23	LBL
23	LBL	22	GTO	15	E
11	A	01	1	34 05	RCL 5
33 01	STO 1	23	LBL	34 04	RCL 4
84	R/S	14	D	51	–
23	LBL	33 04	STO 4	84	R/S
12	B	33 05	STO 5	34 05	RCL 5
84	R/S	84	R/S	24	RTN
23	LBL	23	LBL	35 01	g NOP
12	B	14	D	35 01	g NOP
61	+	35 07	g x \neq y	35 01	g NOP
71	x	81	÷	35 01	g NOP
61	+	34 01	RCL 1	35 01	g NOP
33 02	STO 2	71	x	35 01	g NOP
84	R/S	01	1	35 01	g NOP
23	LBL	51	–	35 01	g NOP
13	C	33 03	STO 3	35 01	g NOP
84	R/S	23	LBL	35 01	g NOP
23	LBL	01	1	35 01	g NOP
13	C	34 02	RCL 2	35 01	g NOP
32	f ⁻¹	34 03	RCL 3	35 01	g NOP
03	→D.MS	34 05	RCL 5	35 01	g NOP
31	f	71	x	35 01	g NOP
05	COS	61	+	35 01	g NOP
35 00	gLST X	33	STO	35 01	g NOP
31	f	61	+	35 01	g NOP
06	TAN	05	5	35 01	g NOP
34 01	RCL 1	35	9	35 01	g NOP
71	x	06	ABS	35 01	g NOP
01	1	83	•	01	1
51	–	01	1	35 22	g x \leq y
33 03	STO 3	35 22	g x \leq y	22	GTO
35 08	g R↓	22	GTO	01	1

R ₁	Slope	R ₄	H Dist	R ₇
R ₂	Used	R ₅	H Dist	R ₈
R ₃	Used	R ₆	Used	R ₉



AZIMUTH OF THE SUN

CODE	KEYS	CODE	KEYS	CODE	KEYS
23	LBL	33 03	STO 3	24	RTN
11	A	34 01	RCL 1	23	LBL
33 04	STO 4	31	f	01	1
24	RTN	04	SIN	35 08	g R↑
23	LBL	34 02	RCL 2	35 08	g R↓
11	A	31	f	42	CHS
31	f	04	SIN	41	↑
02	D.MS+	34 03	RCL 3	03	3
32	f ⁻¹	31	f	06	6
03	→D.MS	04	SIN	00	0
24	RTN	71	x	61	+
23	LBL	51	–	31	f
12	B	34 02	RCL 2	03	→D.MS
32	f ⁻¹	31	f	24	RTN
03	→D.MS	05	COS	35 01	g NOP
35 07	g x \neq y	34 03	RCL 3	35 01	g NOP
24	RTN	31	f	35 01	g NOP
23	LBL	05	COS	35 01	g NOP
12	B	71	x	35 01	g NOP
32	f ⁻¹	81	÷	35 01	g NOP
03	→D.MS	24	RTN	35 01	g NOP
71	x	23	LBL	35 01	g NOP
61	+	15	E	35 01	g NOP
33 01	STO 1	32	f ⁻¹	35 01	g NOP
24	RTN	05	COS	35 01	g NOP
23	LBL	34 04	RCL 4	35 01	g NOP
13	C	01	1	35 01	g NOP
32	f ⁻¹	02	2	35 01	g NOP
03	→D.MS	35 22	g x \leq y	35 01	g NOP
33 02	STO 2	22	GTO	35 01	g NOP
24	RTN	01	1	35 01	g NOP
23	LBL	35 08	g R↑	35 01	g NOP
14	D	35 08	g R↓	35 01	g NOP
32	f ⁻¹	31	f	35 01	g NOP
03	→D.MS	03	→D.MS	35 01	g NOP

R ₁	Declination (δ)	R ₄	Local time	R ₇
R ₂	Latitude (ϕ)	R ₅		R ₈
R ₃	Vert ang (h)	R ₆		R ₉

PREDETERMINED AREA - LINE THRU A POINT

CODE	KEYS	CODE	KEYS	CODE	KEYS
23	LBL	00	0	33 04	STO 4
11	A	61	+	34 03	RCL 3
02	2	33 03	STO 3	51	-
71	x	24	RTN	31	f
33 01	STO 1	23	LBL	04	SIN
24	RTN	14	D	35	g
23	LBL	32	f ⁻¹	06	ABS
12	B	03	-D.MS	34 02	RCL 2
24	RTN	24	RTN	35 07	g x \neq y
23	LBL	23	LBL	81	\div
12	B	14	D	33 02	STO 2
24	RTN	41	\uparrow	24	RTN
23	LBL	02	2	23	LBL
13	C	81	\div	15	E
33 06	STO 6	41	\uparrow	34 04	RCL 4
35 07	g x \neq y	31	f	31	f
24	RTN	83	INT	05	COS
23	LBL	35 21	g x \neq y	71	x
13	C	22	GTO	34 06	RCL 6
33 05	STO 5	01	1	61	+
51	-	35 09	g R \uparrow	84	R/S
35 08	g R \downarrow	35 09	g R \uparrow	34 02	RCL 2
51	-	42	CHS	34 04	RCL 4
35 09	g R \uparrow	35 09	g R \uparrow	31	f
35 07	g x \neq y	35 09	g R \uparrow	04	SIN
31	f	23	LBL	71	x
01	R \rightarrow P	01	1	34 05	RCL 5
34 01	RCL 1	35 08	g R \downarrow	61	+
35 07	g x \neq y	31	f	84	R/S
81	\div	83	INT	35 01	g NOP
33 02	STO 2	01	1		
44	CLX	08	8		
35 24	g x \neq y	00	0		
03	3	71	x		
06	6	61	+		

R ₁ 2 x Area (2A)	R ₄ Az 2 → 3	R ₇
R ₂ 2A/Base	R ₅ Point 2 E	R ₈
R ₃ Az 2 → 1	R ₆ Point 2 N	R ₉ Used

PREDETERMINED AREA - TWO SIDES PARALLEL

CODE	KEYS	CODE	KEYS	CODE	KEYS
23	LBL	06	TAN	34	RCL
11	A	35	g	09	9
33 01	STO 1	04	1/x	34 04	RCL 4
24	RTN	33	STO	33 02	STO 2
23	LBL	61	+	81	\div
12	B	05	5	33 04	STO 4
33 02	STO 2	34 02	RCL 2	44	CLX
24	RTN	41	\uparrow	24	RTN
23	LBL	32	f ⁻¹	23	LBL
13	C	09	\sqrt{x}	15	E
33 06	STO 6	34 01	RCL 1	34 07	RCL 7
32	f ⁻¹	02	2	84	R/S
03	-D.MS	71	x	34 03	RCL 3
41	\uparrow	34 05	RCL 5	84	R/S
31	f	71	x	34 04	RCL 4
04	SIN	51	-	84	R/S
33 03	STO 3	31	f	34 06	RCL 6
35 07	g x \neq y	09	\sqrt{x}	23	LBL
31	f	51	-	01	1
06	TAN	34 05	RCL 5	42	CHS
35	g	41	\div	01	1
04	1/x	33	STO	08	8
33 05	STO 5	09	9	00	0
24	RTN	34 05	RCL 5	31	f
23	LBL	71	x	02	D.MS +
14	D	34 02	RCL 2	84	R/S
33 08	STO 8	35 07	g x \neq y	34 08	RCL 8
32	f ⁻¹	51	-	22	GTO
03	-D.MS	33 07	STO 7	01	1
41	\uparrow	34	RCL	35 01	g NOP
31	f	09	9		
04	SIN	34 03	RCL 3		
33 04	STO 4	33 01	STO 1		
35 07	g x \neq y	81	\div		
31	f	33 03	STO 3		

R ₁ Area/SIN <1	R ₄ SIN <2/Side 2	R ₇ Base 2
R ₂ Base 1/SIN <2	R ₅ CTN <1 + CTN <2	R ₈ ϕ
R ₃ SIN <1/Side 1	R ₆ θ	R ₉ Used

VOLUME BY AVERAGE END AREA

CODE	KEYS	CODE	KEYS	CODE	KEYS
23	LBL	33	STO	61	+
11	A	61	+	08	8
34 06	RCL 6	06	6	33	STO
33 07	STO 7	34 03	RCL 3	09	9
44	CLX	33 01	STO 1	44	CLX
33 06	STO 6	34 04	RCL 4	84	R/S
84	R/S	33 02	STO 2	23	LBL
23	LBL	34 05	RCL 5	15	E
12	B	33 03	STO 3	34	RCL
33 01	STO 1	84	R/S	09	9
84	R/S	23	LBL	84	R/S
23	LBL	11	A	34 08	RCL 8
11	A	33 04	STO 4	84	R/S
33 02	STO 2	84	R/S	02	2
84	R/S	23	LBL	07	7
23	LBL	12	B	81	÷
12	B	33 05	STO 5	24	RTN
33 03	STO 3	22	GTO	35 01	g NOP
84	R/S	01	1	35 01	g NOP
23	LBL	23	LBL	35 01	g NOP
11	A	13	C	35 01	g NOP
33 04	STO 4	34 06	RCL 6	35 01	g NOP
84	R/S	35	9	35 01	g NOP
23	LBL	06	ABS	35 01	g NOP
12	B	33 06	STO 6	35 01	g NOP
33 05	STO 5	84	R/S	35 01	g NOP
23	LBL	23	LBL	35 01	g NOP
01	1	14	D	35 01	g NOP
34 02	RCL 2	34 06	RCL 6	35 01	g NOP
34 05	RCL 5	34 07	RCL 7	35 01	g NOP
34 01	RCL 1	81	+	35 01	g NOP
51	-	71	x		
71	x	02	2		
02	2	81	÷		
81	÷	33	STO		

R_1 Used	R_4 Used	R_7 Last Area
R_2 Used	R_5 Used	R_8 Σ Volume
R_3 Used	R_6 Area	R_9 Used

VOLUME OF BORROW PIT

CODE	KEYS	CODE	KEYS	CODE	KEYS
31	f	71	x	35 01	g NOP
43	REG	33	STO	35 01	g NOP
84	R/S	61	+	35 01	g NOP
23	LBL	02	2	35 01	g NOP
11	A	84	R/S	35 01	g NOP
84	R/S	23	LBL	35 01	g NOP
23	LBL	15	E	35 01	g NOP
11	A	34 02	RCL 2	35 01	g NOP
71	x	84	R/S	35 01	g NOP
06	6	02	2	35 01	g NOP
81	÷	07	7	35 01	g NOP
33 03	STO 3	81	÷	35 01	g NOP
22	GTO	84	R/S	35 01	g NOP
01	1	35 01	g NOP	35 01	g NOP
23	LBL	35 01	g NOP	35 01	g NOP
12	B	35 01	g NOP	35 01	g NOP
84	R/S	35 01	g NOP	35 01	g NOP
23	LBL	35 01	g NOP	35 01	g NOP
12	B	35 01	g NOP	35 01	g NOP
71	x	35 01	g NOP	35 01	g NOP
04	4	35 01	g NOP	35 01	g NOP
81	÷	35 01	g NOP	35 01	g NOP
33 03	STO 3	35 01	g NOP	35 01	g NOP
23	LBL	35 01	g NOP	35 01	g NOP
01	1	35 01	g NOP	35 01	g NOP
44	CLX	35 01	g NOP	35 01	g NOP
41	↑	35 01	g NOP	35 01	g NOP
84	R/S	35 01	g NOP	35 01	g NOP
23	LBL	35 01	g NOP	35 01	g NOP
13	C	35 01	g NOP	35 01	g NOP
61	+	35 01	g NOP	35 01	g NOP
84	R/S	35 01	g NOP	35 01	g NOP
23	LBL	35 01	g NOP	35 01	g NOP
14	D	35 01	g NOP	35 01	g NOP
34 03	RCL 3	35 01	g NOP	35 01	g NOP

R_1	R_4	R_7
R_2 Σ Vol.	R_5	R_8
R_3 Grid Area	R_6	R_9