

HEWLETT  PACKARD

HP-35

SURVEYING PAC

INTRODUCTION

The programs contained in this booklet are a brief representation of the many problems which may be solved on the HP-35 Pocket Calculator. The intention is to provide routines for the more widely encountered areas of surveying--traverses, intersects, curves, areas, and triangles.

We hope that you find this booklet useful in your day-to-day calculations.

Civil Engineering Products

Note: ENT is used to denote the ENTER ↑ key throughout the tables in this text.

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DEGREES, MINUTES, SECONDS TO DECIMAL EQUIVALENT

LINE	DATA	OPERATIONS	DISPLAY	REMARKS
1.		<input type="text" value="6"/> <input type="text" value="0"/> <input type="text" value="STO"/> <input type="text"/>		
2.	Degrees	<input type="text" value="ENT"/> <input type="text"/>		
3.	Minutes	<input type="text" value="ENT"/> <input type="text"/>		
4.	Seconds	<input type="text" value="RCL"/> <input type="text" value="÷"/> <input type="text" value="+"/> <input type="text"/>		
5.		<input type="text" value="RCL"/> <input type="text" value="÷"/> <input type="text" value="+"/> <input type="text"/>	Decimal Degrees	Record - See Note 1

Note 1: To convert bearing to azimuth:

If bearing is SE or NW, press . Then if bearing is SE or SW, press , 180, . Then if bearing is NW, press , 360, .

DECIMAL DEGREES TO DEGREES, MINUTES, SECONDS

LINE	DATA	OPERATIONS	DISPLAY	REMARKS
1.	Decimal Degrees	<input type="text" value="ENT"/> <input type="text"/> <input type="text"/> <input type="text"/> <input type="text"/>		
2.	Integer Degrees	<input type="text"/> <input type="text"/> <input type="text"/> <input type="text"/> <input type="text"/>	Degrees	Record
3.		<input type="text" value="-"/> <input type="text" value="6"/> <input type="text" value="0"/> <input type="text" value="X"/> <input type="text"/>		
4.	Integer Minutes	<input type="text"/> <input type="text"/> <input type="text"/> <input type="text"/> <input type="text"/>	Minutes	Record
5.		<input type="text" value="-"/> <input type="text" value="6"/> <input type="text" value="0"/> <input type="text" value="X"/> <input type="text"/>	Seconds	Record

FIELD ANGLE TRAVERSE

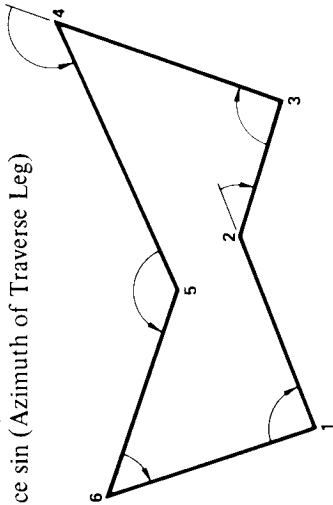
Azimuth of Traverse Leg = Reference Bearing + Field Angle

Horizontal Distance = Slope distance \sin (Zenith)

$N_n = N_o + \text{Horizontal Distance} \cos$ (Azimuth of Traverse Leg)

$E_n = E_o + \text{Horizontal Distance} \sin$ (Azimuth of Traverse Leg)

Example:



Field Data

Reference Bearing 1 \rightarrow 6: N 17° 23' 45" W

Starting Coordinates: $N_1 = 10,000.000$, $E_1 = 10,000.000$

Point	Field Angle	Zenith Angle	Slope Distance
1	87° 22' 17" Right	88° 07' 18"	745.832
2	38° 06' 54" Deflection Right	89° 54' 07"	510.089
3	92° 13' 06" Right	91° 13' 31"	853.760
4	133° 12' 46" Deflection Left	Horizontal	1053.916
5	137° 46' 30" Left	90° 48' 57"	789.671
6	53° 16' 47" Right	89° 41' 55"	784.406

1

Computed Data

Point	N	E	Point	N	E
1	10,000.000	10,000.000	5	10,487.192	10,510.672
2	10,255.251	10,700.367	6	10,748.438	9,765.552
3	10,096.859	11,185.240	1	9,999.933	10,000.107
4	10,897.362	11,481.496			

FIELD ANGLE TRAVERSE (Continued)

Computed Azimuth $6 \rightarrow 1$: $162^\circ 36' 03''$

$$\sqrt{(\text{Corr}_N)^2 + (\text{Corr}_E)^2} = 0.126$$

\therefore Angular Closure = $12''$

Position Closure (Before Adjustment of Angles): Length of Traverse $\cong 4738$

$\text{Corr}_N = +0.067$, $\text{Corr}_E = -0.107$ Precision Ratio $\cong 1/37,600$

LINE	DATA	OPERATIONS	DISPLAY	REMARKS
1.	Reference Bearing Degrees	ENT <input type="text"/> <input type="text"/> <input type="text"/> <input type="text"/>		
2.	Minutes	ENT <input type="text"/> <input type="text"/> <input type="text"/> <input type="text"/>		
3.	Seconds	ENT <input type="text"/> 6 <input type="text"/> 0 <input type="text"/> \div <input type="text"/> +		
4.		<input type="text"/> 6 <input type="text"/> 0 <input type="text"/> \div <input type="text"/> + <input type="text"/>	Decimal Ref. Bearing	See Note 1
5.		STO <input type="text"/> <input type="text"/> <input type="text"/> <input type="text"/> <input type="text"/>	Decimal Ref. Azimuth	
6.	Field Angle Degrees	ENT <input type="text"/> <input type="text"/> <input type="text"/> <input type="text"/>		
7.	Minutes	ENT <input type="text"/> <input type="text"/> <input type="text"/> <input type="text"/>		
8.	Seconds	ENT <input type="text"/> 6 <input type="text"/> 0 <input type="text"/> \div <input type="text"/> +		

9.			6	0	÷	+			Decimal Field Angle	See Note 2
10.			RCL	+						See Note 3
11.			STO						Decimal Azimuth of Traverse Leg	See Note 4
12.	Zenith (Vert) Angle Degrees		ENT							
13.	Minutes		ENT							
14.	Seconds		ENT	6	0	÷	+			
15.			6	0	÷	+			Decimal Zenith (Vert.) Angle	See Note 5
16.			SIN							
17.	Slope Distance		X						Horizontal Distance	
18.			RCL	ENT	COS	X↕Y	SIN			
19.			R↓	X					Latitude	
20.	Previous Northing		+						Current Northing	Record
21.			R↓	X					Departure	
22.	Previous Easting		+						Current Easting	Record See Notes 6 & 7

FIELD ANGLE TRAVERSE (Continued)

- Note 1: If the first field angle is an angle right or angle left, the ref. bearing direction is **AWAY** from the first point. If the first field angle is a deflection right or left, the ref. bearing direction is **TOWARDS** the first point. For SE or NW ref. bearing, depress $\boxed{\text{CHS}}$. Then for SE or SW ref. bearing, depress $\boxed{\text{ENTER} \downarrow}$, $\boxed{180}$, $\boxed{+}$ or for NW ref. bearing, depress $\boxed{\text{ENTER} \downarrow}$, $\boxed{360}$, $\boxed{+}$. See Note 8.
- Note 2: Depress $\boxed{\text{CHS}}$ for angle left or deflection left.
- Note 3: If display is greater than 360, depress $\boxed{360}$, $\boxed{-}$. If display is less than zero, depress $\boxed{360}$, $\boxed{+}$. See Note 8.
- Note 4: If a slope distance is to be entered, continue on line 12. If a horizontal distance is to be entered, enter the horizontal distance, skip to line 18 and continue.
- Note 5: If vertical angles are observed instead of zenith angles, depress $\boxed{\text{COS}}$ instead of $\boxed{\text{SIN}}$ in line 16.
- Note 6: If the next field angle is an angle right or angle left, depress $\boxed{\text{CHS}}$, then if display becomes 1) greater than 180, depress $\boxed{180}$, $\boxed{-}$; or 2) less than 180, depress $\boxed{180}$, $\boxed{+}$. Then return to line 5 and continue; or if the next field angle is a deflection right or left, return to line 6 and continue.
- Note 7: After the last coordinates are computed, a check on the angular closure can be made as follows: Depress $\boxed{\text{CHS}}$ and convert the displayed decimal angle to degrees, minutes and seconds. This computed closing azimuth can then be checked against the actual closing azimuth.
- Note 8: If a surveyor does not feel uncomfortable with azimuths greater than 360° or with negative azimuths, the statements about adding (or subtracting) 360 in notes (1) and (3) can be ignored. These operations were employed solely to keep the azimuth values in the range most used by the surveyor, i.e., in the range 0° to 360° . These "corrections" are not really necessary when using the Model 35.

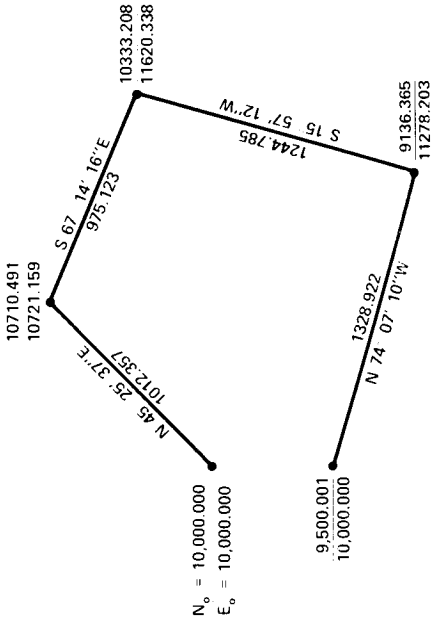
NOTES

BEARING TRAVERSE

$$N_{n+1} = N_n + \text{Distance} \cos(\text{Bearing})$$

$$E_{n+1} = E_n + \text{Distance} \sin(\text{Bearing})$$

Example:



LINE	DATA	OPERATIONS	DISPLAY	REMARKS
1.	Beginning North (N_0)	STO [] [] [] []		
2.	Beginning East (E_0)	ENT [] [] [] []		
3.	Bearing Degrees	ENT [] [] [] []		
4.	Minutes	ENT 6 0 ÷ +		
5.	Seconds	ENT 3 6 0 0		
6.		÷ + [] [] [] []	Decimal Bearing	See Note 1
7.		ENT SIN X↕Y COS [] []		
8.	Distance	X RCL + STO [] []	New Northing	Record
9.	Distance	X + [] [] [] []	New Easting	Record
10.		[] [] [] []		Go To Line 3 For Next Leg

Note 1: If bearing is SE or NW, press CHS . Then if bearing is SE or SW, press ENTER , 180, +. Then proceed to next line.

INVERSE - DISTANCE AND BEARING FROM COORDINATES

$$\text{Bearing} = \tan^{-1} \left(\frac{E_2 - E_1}{N_2 - N_1} \right)$$

$$\text{Distance} = \sqrt{(E_2 - E_1)^2 + (N_2 - N_1)^2}$$

14 *Example:*

$$N_1 = 10,000$$

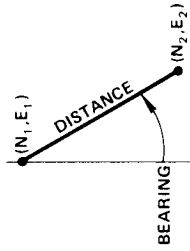
$$E_1 = 10,000$$

$$N_2 = 9,000$$

$$E_2 = 10,500$$

$$\text{Distance} = 1118.034$$

$$\text{Bearing} = \text{S } 26^{\circ} 33' 54'' \text{E}$$



LINE	DATA	OPERATIONS	DISPLAY	REMARKS
1.	Easting ₂	<input type="button" value="ENT"/> <input type="text"/> <input type="text"/>		
2.	Easting ₁	<input type="button" value="-"/> <input type="button" value="ENT"/> <input type="button" value="X"/> <input type="button" value="STO"/> <input type="text"/>		
3.	Northing ₂	<input type="button" value="ENT"/> <input type="text"/> <input type="text"/>		
4.	Northing ₁	<input type="button" value="-"/> <input type="button" value="ENT"/> <input type="button" value="X"/> <input type="button" value="RCL"/> <input type="text"/>		
5.		<input type="button" value="+"/> <input type="button" value="√X"/> <input type="text"/>	Distance	Record
6.		<input type="button" value="R↓"/> <input type="button" value="÷"/> <input type="button" value="ARC"/> <input type="button" value="TAN"/> <input type="text"/>	Decimal Bearing	See Note 1
7.		<input type="button" value="ENT"/> <input type="text"/> <input type="text"/>		
8.	Integer Degrees	<input type="text"/> <input type="text"/>	Bearing Degrees	Record
9.		<input type="button" value="-"/> <input type="button" value="6"/> <input type="button" value="0"/> <input type="button" value="STO"/> <input type="button" value="X"/> <input type="text"/>		
10.	Integer Minutes	<input type="text"/> <input type="text"/>	Bearing Minutes	Record
11.		<input type="button" value="-"/> <input type="button" value="RCL"/> <input type="button" value="X"/> <input type="text"/>	Bearing Seconds	Record
12.		<input type="text"/> <input type="text"/>		Return to Line 1

Note 1: If decimal bearing is positive, bearing is NE or SW. If decimal bearing is negative, bearing is SE or NW. If bearing is negative, press before proceeding to next line.

AREA OF A TRAVERSE FROM COORDINATES

$$A = \frac{1}{2} \left[E_1 (N_2 - N_n) + [E_2 (N_3 - N_1) + E_3 (N_4 - N_2) + \dots + E_{n-1} (N_n - N_{n-2})] + E_n (N_1 - N_{n-1}) \right]$$

Example:

	E	N
1	100.29	491.72
2	447.68	823.14
3	774.43	648.49
4	753.48	318.75
5	610.91	72.23
6	229.34	223.35
1	100.29	491.72

Area = 328,277.19

LINE	DATA	OPERATIONS				DISPLAY	REMARKS
1.		CLR					
2.	Starting Easting	ENT					
3.	Starting Northing	ENT					
4.	Next Easting	ENT	R↓	X	RCL	X↑Y	
5.		-	STO				
6.	Next Northing	ENT	R↓	X	RCL	+	
7.		STO	R↓	X↑Y			See Note 1
8.		RCL	ENT	2	÷	Area	See Note 2/Record

Note 1: Return to line 4 until starting coordinates have been re-entered, then proceed through to line 8 to obtain area.

Note 2: Negative values may result. Absolute value is recorded.

SLOPE DISTANCE REDUCTION

$$S = \left[(\text{Ht. of D. M.}) - (\text{Ht. of Theo.}) - (\text{Ht. of D. M. target}) + (\text{Ht. of Theo. target}) \right]$$

$$k = S \cdot \sin (\text{Zenith})$$

$$p = S \cdot \cos (\text{Zenith})$$

$$\text{Horizontal Distance} = \left(\sqrt{(\text{Slope distance})^2 - k^2} + p \right) (\sin (\text{Zenith}))$$

Example:

Ht. of D.M. = 5.87

Ht. of Theo. = 5.12

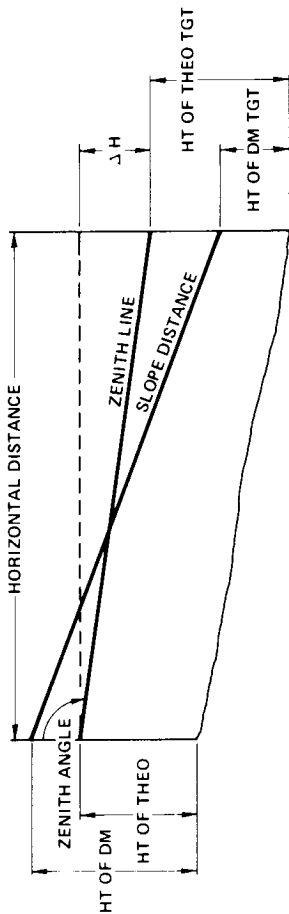
Ht. of D.M. Tgt. = 4.91

Ht. of Theo. Tgt. = 5.17

Zenith Angle = $93^{\circ} 13' 00''$

Slope Distance = 487.132

Horizontal Distance = 486.307



SLOPE DISTANCE REDUCTION (Continued)

LINE	DATA	OPERATIONS				DISPLAY	REMARKS
1.		6	0	STO	<input type="text"/>	<input type="text"/>	
2.	Zenith Degrees	ENT	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	
3.	Minutes	ENT	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	
4.	Seconds	RCL	÷	+	RCL	÷	
5.		+	ENT	ENT	<input type="text"/>	<input type="text"/>	
6.	Ht. D.M.	ENT	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	
7.	Ht. Theo.	-	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	
8.	Ht. D.M. Tgt.	-	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	
9.	Ht. Theo. Tgt.	+	STO	R↓	<input type="text"/>	<input type="text"/>	
10.		COS	RCL	X	<input type="text"/>	<input type="text"/>	See Note 1/Record

11.		<input type="button" value="R↓"/>	<input type="button" value="SIN"/>	<input type="button" value="RCL"/>	<input type="button" value="X"/>	<input type="text"/>	k		See Note 1/Record
12.		<input type="button" value="X↔Y"/>	<input type="button" value="SIN"/>	<input type="button" value="STO"/>	<input type="text"/>	<input type="text"/>			
13.	Slope Distance	<input type="button" value="ENT"/>	<input type="button" value="X"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>			
14.	k	<input type="button" value="ENT"/>	<input type="button" value="X"/>	<input type="text" value="-"/>	<input type="text" value="√X"/>	<input type="text"/>			
15.	p	<input type="button" value="+"/>	<input type="button" value="RCL"/>	<input type="button" value="X"/>	<input type="text"/>	<input type="text"/>	Horizontal Dist.	Record	

Note 1: Values of p and k may be negative. Be sure to retain sign when reentering at lines 14 and 15.

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NOTES

DISTANCE - DISTANCE INTERSECT

Example:

$$N_1 = 1000$$

$$E_1 = 1000$$

$$N_2 = 1250$$

$$E_2 = 2000$$

$$N_3 = 1614.409$$

$$E_3 = 1657.649$$

$$N_4 = 767.353$$

$$E_4 = 1869.411$$

$$B = 500$$

$$A = 900$$

$$\phi = 29.017^\circ$$

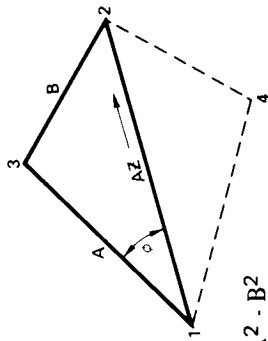
$$\text{Azimuth}_{1 \rightarrow 2} = 75^\circ 57' 50''$$

$$\text{Distance}_{1 \rightarrow 2} = 1030.776$$

$$\phi = \cos^{-1} \frac{(\text{Distance}_{1-2})^2 + A^2 - B^2}{2(A)(\text{Distance}_{1-2})}$$

$$N = N_1 + A \cos(Az \pm \phi)$$

$$E = E_1 + A \sin(Az \pm \phi)$$



DISTANCE - DISTANCE INTERSECT (Continued)

LINE	DATA	OPERATIONS						DISPLAY	REMARKS
1.	N_2	ENT							
2.	N_1	-	ENT	X					
3.	E_2	ENT							
4.	E_1	-	ENT	X	+	STO	$(\text{Distance}_{1,2})^2$		
5.		RCL							
6.	Distance B	ENT	X	-					
7.	Distance A	ENT	ENT	R↓	X	+			
8.		RCL	√X	÷	2	÷			
9.		X↔Y	÷	ARC	COS	STO			
10.	Azimuth 1 → 2 Degrees	ENT							

11.	Minutes	ENT							
12.	Seconds	ENT	6	0	÷	+			
13.		6	0	÷	+	RCL			See Note 1
14.		+	ENT	SIN	X \uparrow Y	COS			
15.	Distance A	STO	X						
16.	N ₁	+						N ₃	Record
17.		RCL	X \uparrow Y	R \downarrow	X				
18.	E ₁	+						E ₃	Record

Note 1: If solution desired is to left of line 1 \rightarrow 2, press \boxed{CHS} before proceeding to line 14.

NOTES

ANGLE - ANGLE INTERSECT

Example:

$$A = 76^{\circ} 30' 00''$$

$$N_B = 3200.000$$

$$B = 38^{\circ} 20' 00''$$

$$E_B = 4200.000$$

$$N_A = 5200.000$$

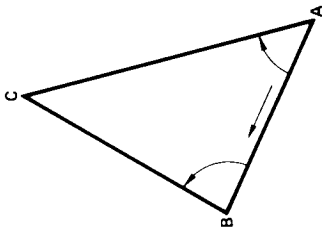
$$N_C = 6143.552$$

$$E_A = 6100.000$$

$$E_C = 4467.774$$

$$N_C = \frac{E_A - E_B + N_B \cot A + N_A \cot B}{\cot A + \cot B}$$

$$E_C = \frac{N_B - N_A + E_B \cot A + E_A \cot B}{\cot A + \cot B}$$



ANGLE - ANGLE INTERSECT (Continued)

LINE	DATA	OPERATIONS	DISPLAY	REMARKS
1.		6 0 STO		
2.	Angle B Degrees	ENT		
3.	Minutes	ENT		
4.	Seconds	RCL ÷ +		
5.		RCL ÷ + TAN 1/X		
6.	Angle A Degrees	ENT		
7.	Minutes	RCL ÷ +		
8.	Seconds	RCL ÷ RCL ÷ +		
9.		TAN 1/X STO R↓		
10.		ENT ENT		

11.	E_A	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>		
12.	N_A	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>		
13.	E_B	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>		
14.	N_B	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>
15.		<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	E_C	Record
16.		<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>		
17.	E_A	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>		
18.	N_A	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>		
19.	E_B	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>		
20.	N_B	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>
21.		<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>	N_C	Record

TRIANGLE SOLUTION - GIVEN THREE SIDES

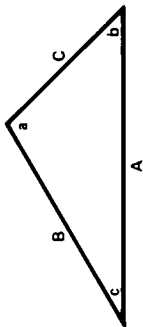
Example:

$$\begin{aligned} A &= 2489.621 & a &= 48^{\circ} 00' 00'' \\ B &= 2543.150 & b &= 49^{\circ} 23' 13'' \\ C &= 3322.312 & c &= 82^{\circ} 36' 47'' \end{aligned}$$

$$c = 2 \operatorname{TAN}^{-1} \left(\frac{r}{S-C} \right)$$

$$r = \sqrt{\frac{(S-A)(S-B)(S-C)}{S}}$$

$$S = \frac{1}{2} (A + B + C)$$



LINE	DATA	OPERATIONS	DISPLAY	REMARKS
1.	Side A	ENT <input type="text"/> <input type="text"/>		
2.	Side B	ENT R↓ <input type="text"/> + <input type="text"/>		
3.	Side C	STO + 2 <input type="text"/> ÷ <input type="text"/> RCL <input type="text"/>		
4.		X↑Y STO X↑Y <input type="text"/> - <input type="text"/> ENT <input type="text"/>		
5.		R↓ <input type="text"/> RCL X↑Y <input type="text"/> - <input type="text"/>		
6.		X↑Y RCL X↑Y <input type="text"/> - <input type="text"/>		
7.		X <input type="text"/> X RCL <input type="text"/> ÷ <input type="text"/> √X <input type="text"/>		
8.		X↑Y ÷ <input type="text"/> ARC TAN <input type="text"/> 2 <input type="text"/>		
9.		X <input type="text"/> <input type="text"/> <input type="text"/> <input type="text"/>	Decimal Angle c	See Note 1
10.	Integer Degrees	<input type="text"/> <input type="text"/> <input type="text"/> <input type="text"/>	Degrees	Record
11.		- <input type="text"/> 6 <input type="text"/> 0 <input type="text"/> X <input type="text"/>		
12.	Integer Minutes	<input type="text"/> <input type="text"/> <input type="text"/> <input type="text"/>	Minutes	Record
13.		- <input type="text"/> 6 <input type="text"/> 0 <input type="text"/> X <input type="text"/>	Seconds	Record

Note 1: Angle b may be obtained by reversing the data entries at lines 2 and 3.

TRIANGLE SOLUTION - GIVEN TWO ANGLES AND INCLUDED SIDE

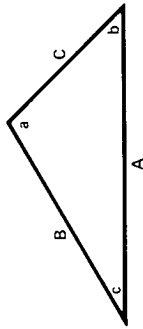
Example:

$$\begin{array}{ll} A = 2489.621 & a = 48^{\circ} 00' 00'' \\ B = 2543.150 & b = 49^{\circ} 23' 13'' \\ C = 3322.312 & c = 82^{\circ} 36' 47'' \end{array}$$

$$A = \frac{B \sin a}{\sin b}$$

$$C = \frac{B \sin c}{\sin b}$$

(LAW OF SINES)



LINE	DATA	OPERATIONS				DISPLAY	REMARKS
1.		CLR	6	0	STO		
2.	Angle a Degrees	ENT					
3.	Minutes	ENT					
4.	Seconds	RCL	÷	+			
5.		RCL	÷	+			
6.	Angle c Degrees	ENT					
7.	Minutes	RCL	÷	+			
8.	Seconds	RCL	÷	RCL	÷	+	
9.		ENT	R↓	+	SIN		
10.	Side B	X↕Y	÷	X↕Y	SIN	X↕Y	
11.		ENT	R↓	X			Record
12.		R↓	SIN	X			Record

TRIANGLE SOLUTION

GIVEN TWO SIDES & ANGLE OPPOSITE ONE OF THEM

Example:

$A = 6.00$	$a = 30^\circ 23' 17''$	$A = 6.00$	$a = 30^\circ 23' 17''$
$B = 10.70$	$b = 64^\circ 26' 11''$	$B = 10.70$	$b = 115^\circ 33' 49''$
$C = 11.82$	$c = 85^\circ 10' 32''$	$C = 6.64$	$c = 34^\circ 02' 54''$

$$b = \sin^{-1} \left(\frac{B \sin a}{A} \right)$$

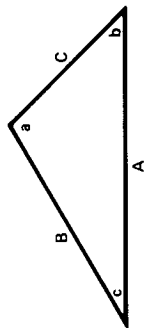
Obtuse Angle b

$$c = 180 - (a + b)$$

$$C = \frac{A \sin c}{\sin a}$$

(LAW OF SINES)

Acute Angle b



LINE	DATA	OPERATIONS			DISPLAY	REMARKS
1.		CLR	6	0	STO	
2.	Angle a Degrees	ENT				
3.	Minutes	RCL	÷	+		
4.	Seconds	RCL	÷	RCL	÷	+
5.		STO	SIN			
6.	Side B	ENT	R↓	X	X↗Y	+
7.	Side A	÷	ENT	ARC	SIN	
8.		RCL	+			Angle b Decimal
9.		1	8	0	X↗Y	-
10.		SIN	X↗Y	÷	X	Side C

Note 1: To solve the problem where angle b is obtuse, press:
 180, $\boxed{\text{D}}$, $\boxed{\text{D}}$, - before proceeding to line 8.

Note 2: Since the sum of angles of a triangle must be 180° , the sum of angles b and a cannot be greater than 180 . If the display exceeds 180° there is only one solution, with angle b acute.

AREA OF A TRIANGLE - GIVEN THREE SIDES

Example:

$$\text{Area} = \sqrt{S(S-A)(S-B)(S-C)}$$

$$\text{Where } S = \frac{1}{2} (A + B + C)$$

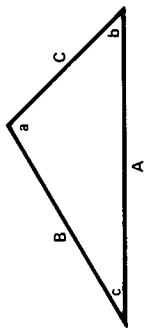
A, B, C = Lengths of Individual Sides

$$A = 2489.621$$

$$B = 2543.150$$

$$C = 3322.312$$

$$\text{Area} = 3139465.857$$



LINE	DATA	OPERATIONS	DISPLAY	REMARKS
1.	Side A	ENT [] [] [] []		
2.	Side B	ENT [] [] [] []		
3.	Side C	STO X \leftrightarrow Y ENT R \downarrow +		
4.		X \leftrightarrow Y ENT R \downarrow + 2		
5.		\div RCL X \leftrightarrow Y STO X \leftrightarrow Y		
6.		- RCL X X RCL X \leftrightarrow Y		
7.		R \downarrow X \leftrightarrow Y - X \leftrightarrow Y RCL		
8.		X \leftrightarrow Y - X X \sqrt{X}	Area	Record

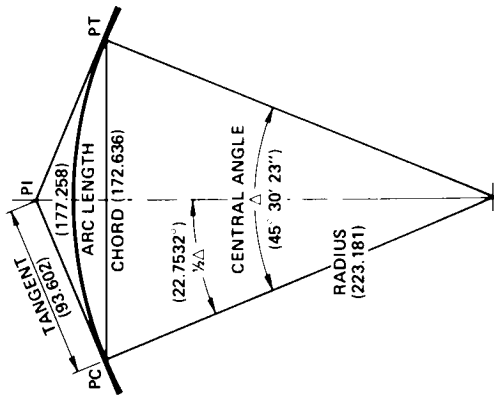
CURVE SOLUTION - GIVEN CENTRAL ANGLE AND TANGENT DISTANCE

Example:

$$R = \text{Tangent} / \tan (\Delta / 2)$$

$$\text{Chord} = 2R \sin (\Delta / 2)$$

$$\text{Arc Length} = R \Delta \pi / 180$$



LINE	DATA	OPERATIONS				DISPLAY	REMARKS
1.		6	0	STO			
2.	Δ Degrees	ENT					
3.	Minutes	ENT					
4.	Seconds	RCL	\div	+	RCL	\div	
5.		+	2	\div	STO	Decimal $\frac{1}{2}$ Δ	
6.	Tangent Distance	ENT	RCL	TAN	\div	Radius	
7.		ENT	ENT	RCL	SIN	X	
8.		2	X			Chord	
9.		R \downarrow	RCL	X			
10.		π	X	9	0	\div	
						Record	

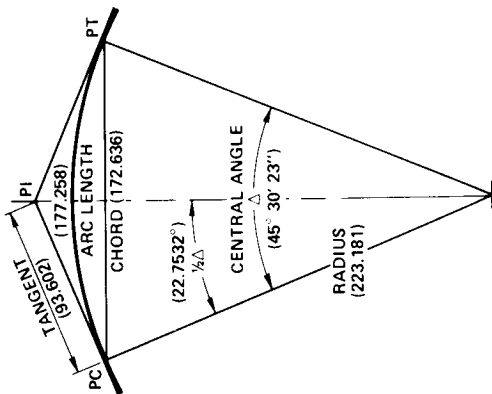
CURVE SOLUTION - GIVEN CENTRAL ANGLE & RADIUS

Example:

$$\text{Chord} = 2 R \sin (\Delta / 2)$$

$$\text{Tangent} = R \tan (\Delta / 2)$$

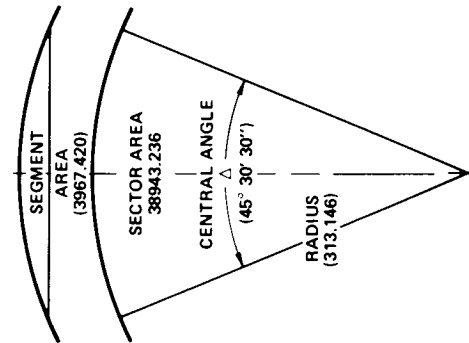
$$\text{Arc Length} = R \Delta \pi / 180$$



LINE	DATA	OPERATIONS	DISPLAY	REMARKS
1.	Δ Degrees	ENT <input type="text"/> <input type="text"/> <input type="text"/>		
2.	Minutes	ENT <input type="text"/> <input type="text"/> <input type="text"/>		
3.	Seconds	ENT 6 0 STO <input type="text"/>		
4.		\div + RCL \div + <input type="text"/>		
5.		2 \div <input type="text"/> <input type="text"/>	Decimal $\frac{1}{2}$ Δ	
6.		ENT ENT TAN <input type="text"/> <input type="text"/>		
7.	Radius	STO X <input type="text"/> <input type="text"/>	Tangent Distance	Record
8.		R \downarrow SIN RCL X 2 <input type="text"/>		
9.		X <input type="text"/> <input type="text"/> <input type="text"/>	Chord	Record
10.		R \downarrow RCL X π X <input type="text"/>		
11.		9 0 \div <input type="text"/>	Arc Length	Record

CURVE AREA - GIVEN CENTRAL ANGLE & RADIUS

Example:



$$\text{Segment Area} = \pi R^2 \left(\frac{\Delta^\circ}{360^\circ} \right) - \frac{1}{2} R^2 \sin(\Delta^\circ)$$

$$\text{Sector Area} = \pi R^2 \left(\frac{\Delta^\circ}{360^\circ} \right)$$

LINE	DATA	OPERATIONS	DISPLAY	REMARKS
1.		6 0 STO		
2.	Δ Degrees	ENT		
3.	Minutes	ENT		
4.	Seconds	RCL \div + RCL \div		
5.		+ ENT ENT π X		
6.		3 6 0 \div		
7.	Radius	ENT X ENT R \downarrow X	Sector Area	Record
8.		X \uparrow Y SIN X \uparrow Y R \downarrow X		
9.		2 \div X \uparrow Y R \downarrow -	Segment Area	Record

CURVE LAYOUT - DEFLECTION ANGLES FROM TANGENT

Deflection/ft = $180/(2\pi R)$

Deflection Angle = Arc X Deflection/ft.

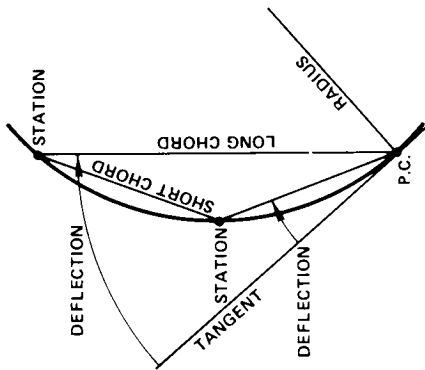
Long Chord = 2 Radius Sin (Deflection Angle)

Example:

Radius = 900.00 Ft.

Station	Arc Length	Deflection	Long Chord
12 + 57.00	(Point of Curvature, P.C.)		
12 + 75.00	18.00	00° 34' 23"	18.00
12 + 88.50	31.50	01° 00' 10"	31.50
13 + 00.00	43.00	01° 22' 07"	43.00
13 + 25.00	68.00	02° 09' 52"	67.98
13 + 50.00	93.00	02° 57' 37"	92.96

Arc Length = Difference in Stations



LINE	DATA	OPERATIONS	DISPLAY	REMARKS
1.	Radius	ENT 2 X ENT ENT		
2.		1 8 0 ENT π		
3.		\div X \div Y \div STO		
4.		RCL		
5.	Arc Length From P.C.	X	Decimal Deflection	
6.		ENT ENT		
7.	Integer Degrees		Deflection Degrees	Record
8.		- 6 0 X		
9.	Integer Minutes		Deflection Minutes	Record
10.		- 6 0 X	Deflection Seconds	Record
11.		R \downarrow		
12.		SIN X	Long Chord	See Note 1
13.		CLX		Return to Line 4

Note 1: Computation of the long chord can be omitted if regular intervals are used for which the short chord remains constant. Calculation then only needed for odd intervals.

ELEVATIONS ALONG A VERTICAL CURVE

$$E_s = E_o + G_1(\text{Distance in Stations}) + \left[\frac{50(G_2 - G_1)}{L} \right] (\text{Distance in Stations})^2$$

Example:

Beginning Grade (G_1) = -1.065%

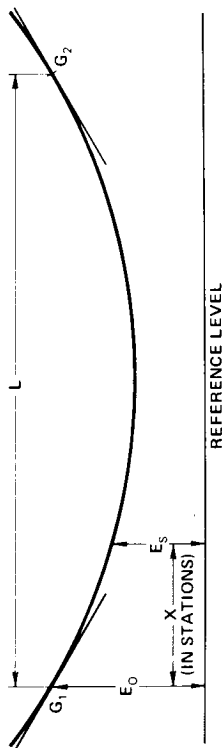
Ending Grade (G_2) = +1.600%

Elevation at Beginning (E_o) = 614.00 Ft.

Length of Curve (L) = 340 Ft.

Stationing Intervals = 100 Ft.

STATION	ELEVATION (E_s)
17 + 00.00	614.000
18 + 00.00	613.327
19 + 00.00	613.438
20 + 00.00	614.332
20 + 40.00	614.910



LINE	DATA	OPERATIONS	DISPLAY	REMARKS
1.	G_2	ENT <input type="text"/> <input type="text"/> <input type="text"/>		Grades in %
2.	G_1	- <input type="text"/> 5 <input type="text"/> 0 <input type="text"/> X <input type="text"/>		
3.	Length of Curve (L)	÷ <input type="text"/> STO <input type="text"/> <input type="text"/>		
4.	Beginning Elevation (E_0)	ENT <input type="text"/> <input type="text"/> <input type="text"/>		
5.	Distance in Stations	ENT <input type="text"/> ENT <input type="text"/> X <input type="text"/> RCL <input type="text"/> X <input type="text"/>		
6.		X \leftrightarrow Y <input type="text"/> <input type="text"/> <input type="text"/>		
7.	G_1	X <input type="text"/> + <input type="text"/> + <input type="text"/>	Elevation (E_S)	Record
8.		CLX <input type="text"/> <input type="text"/> <input type="text"/>		Return to step 5

NOTES



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